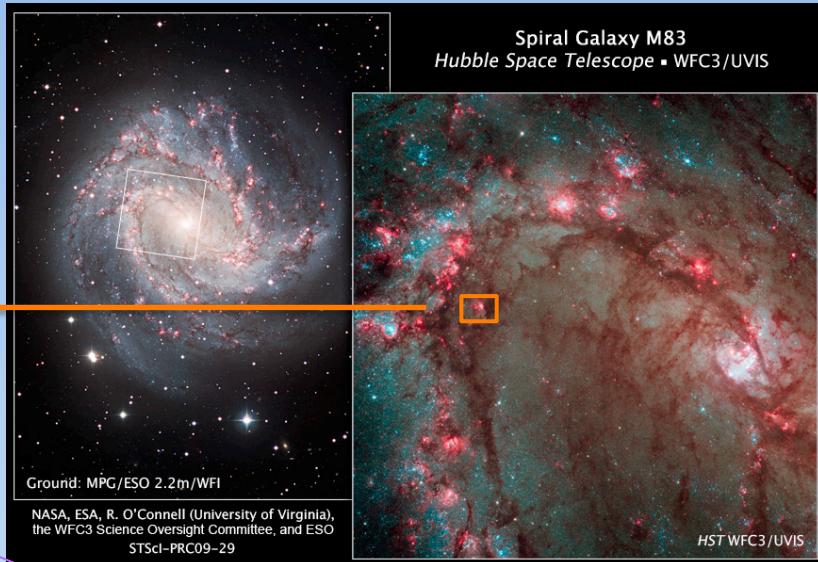
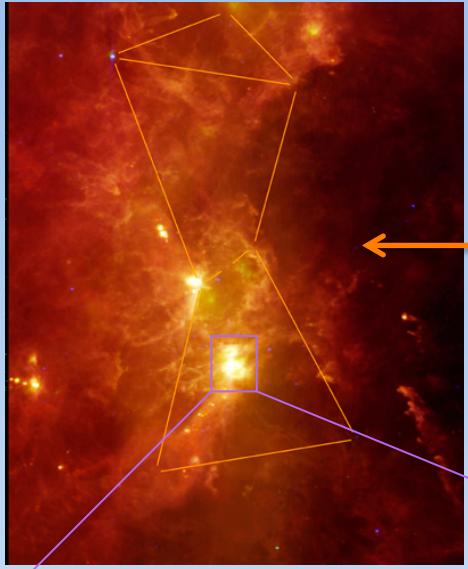


# *Star Formation and “Feedback”*

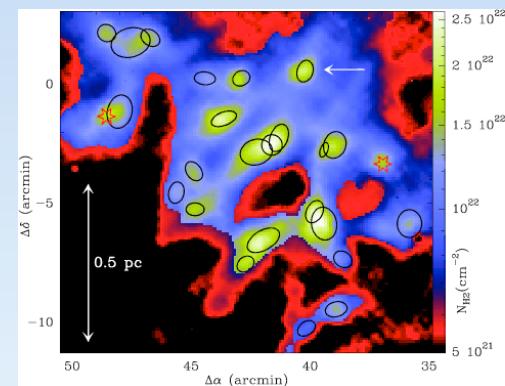
**Eve Ostriker**  
*Princeton University*



HL Tauri (ALMA/HST)



The Orion Nebula and Trapezium Cluster  
(VLT ANTU + ISAAC)



Könyves et al (2010)

# Star formation and the life-cycle of the interstellar medium

- Star formation begins with the condensation of diffuse, turbulent interstellar gas ( $\langle n \rangle \sim 1 \text{ cm}^{-3}$ ) into giant molecular clouds
  - GMC:  $M \sim 10^4\text{-}10^6 M_{\odot}$ ,  $\langle n \rangle \sim 100 \text{ cm}^{-3}$ ,  $T \sim 10\text{K}$
- Supersonic turbulent motions within GMCs create shocks that drives gas to higher density
- Densest regions within filaments in GMCs contract gravitationally to make **prestellar cores**
  - core:  $M \sim 0.1\text{-}10 M_{\odot}$ ,  $n \sim 10^4\text{-}10^6 \text{ cm}^{-3}$

# Star formation and the life-cycle of the interstellar medium

- Prestellar cores collapse to make star ( $n \sim 10^{24} \text{ cm}^{-3}$ )/disk system; disks evolve into planets
- Massive stars emit copious radiation (luminosity  $L \propto M^{3.5}$ ), including UV that ionizes and strongly heats ( $T \sim 10^4 \text{ K}$ ) the near environment
- High-pressure ionized gas rapidly expands
- Momentum carried by stellar FUV radiation directly pushes on the surrounding dusty gas
- Stars with  $M > 8M_{\odot}$  end as supernovae; blast wave created by explosion expands into ISM

# Star formation and the life-cycle of the interstellar medium

- The momentum and energy injected by massive stars disperses GMCs
- “Feedback” from massive stars also heats and stirs up turbulence in the diffuse ISM
- When gravitational energy exceeds kinetic energy locally in the ISM, a new cycle of GMC formation and then star formation begins

## 1. Formation of stars

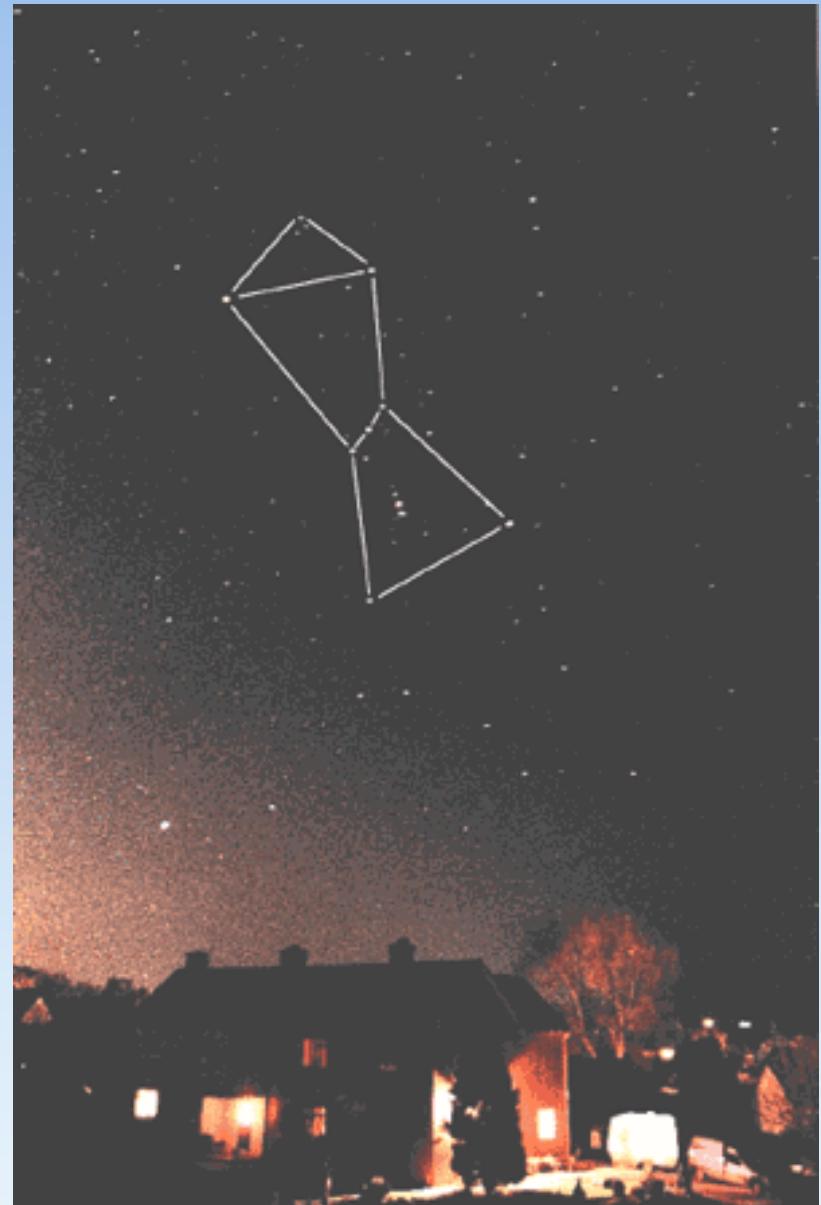
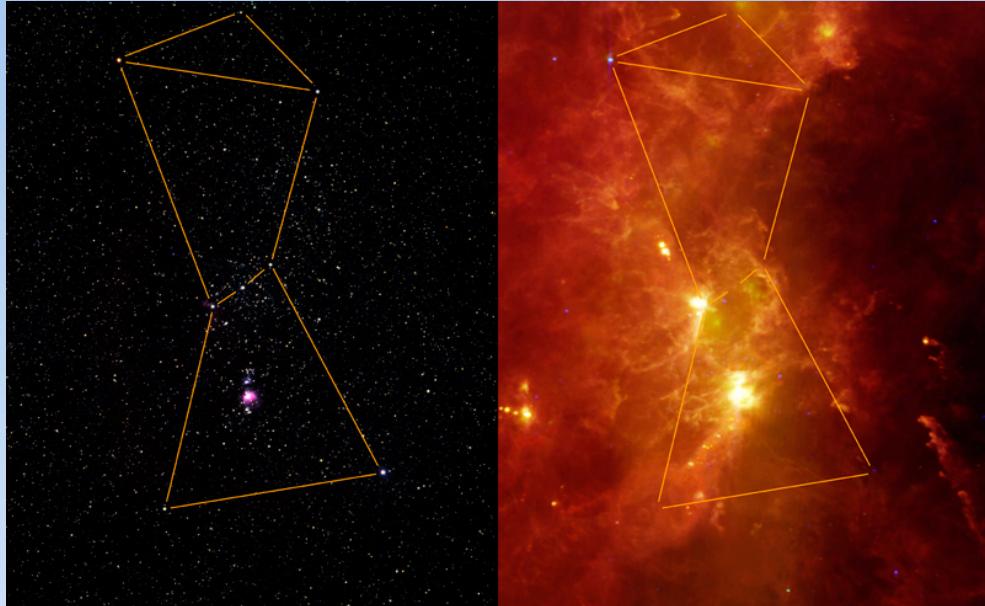
- Roles of turbulence, thermal pressure, magnetic fields

## 2. Quantifying “feedback”

- Radiation
- Supernovae

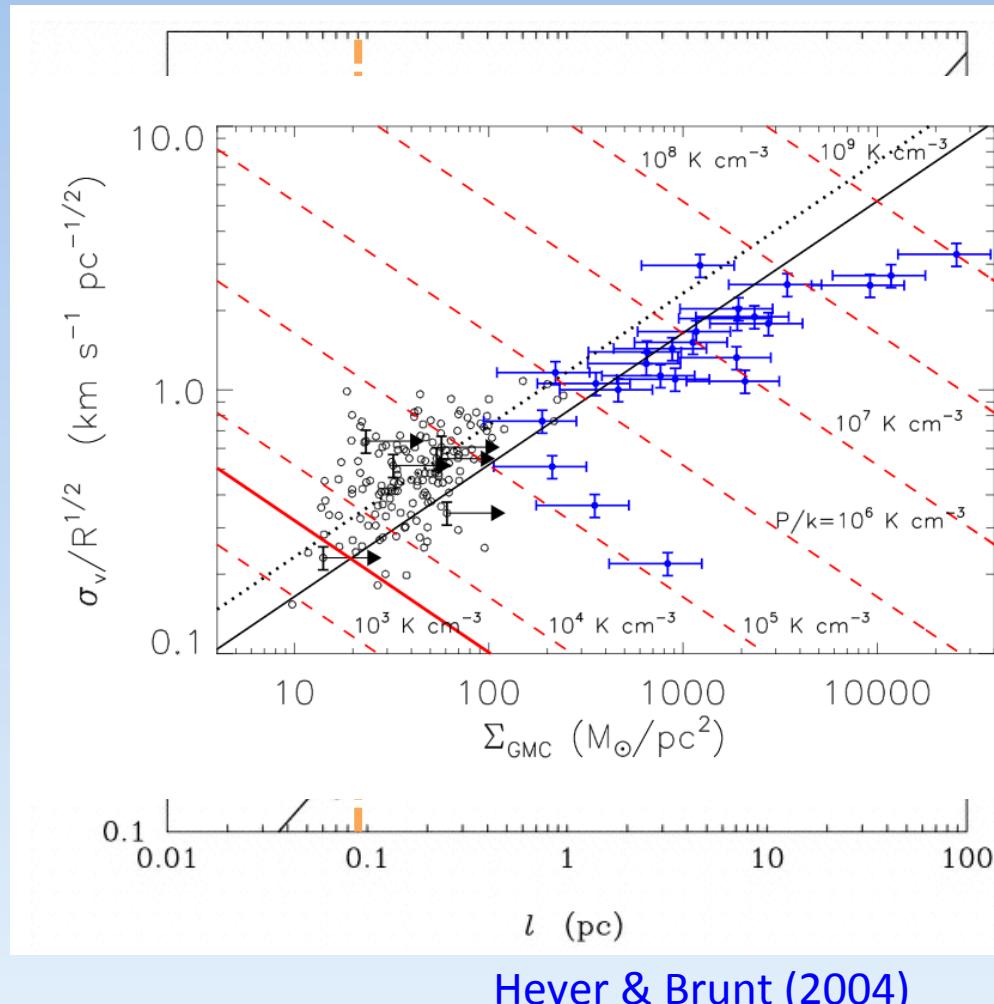
## 3. Self-regulated star formation

# Orion: optical, IR, radio

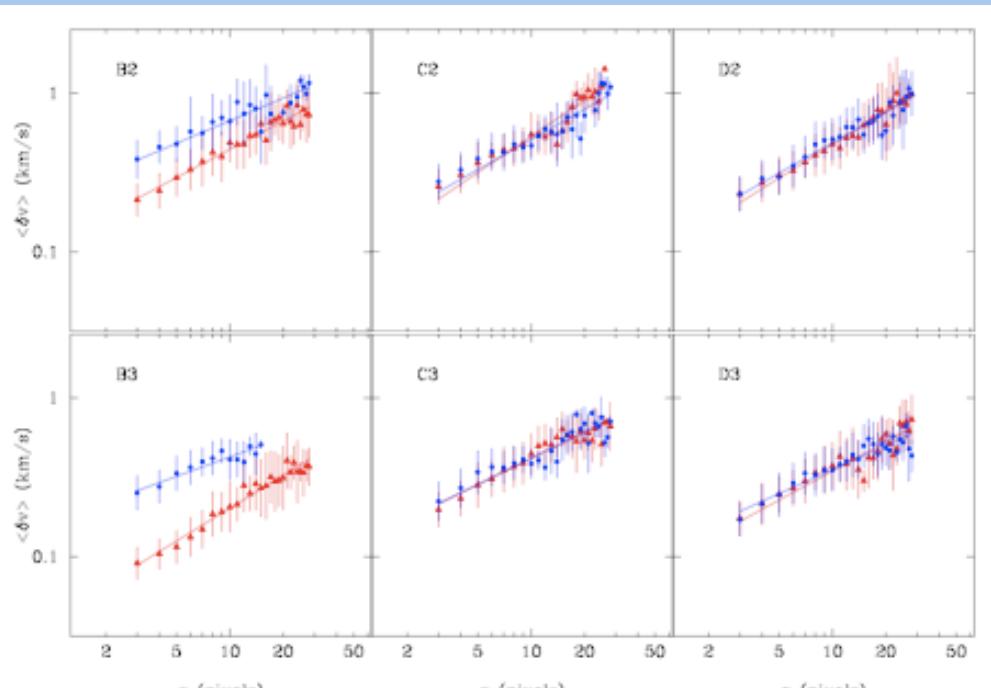


# GMC Turbulence

- On large scales, GMCs are self-gravitating and have  $E_g \sim E_k$   
 $GM^2/R \sim M \delta v^2$   
 $G\Sigma_{\text{gas}}^2 \sim \rho \delta v^2 \gg P_{\text{diffuse ISM}}$
- $\delta v(s) \propto s^{1/2}$  linewidth-size relation inside GMCs is consistent with Burgers spectrum
- Cloud scale:  
 $\delta v^2(R) \sim GM/R \sim G(\Sigma R^2)/R \sim G\Sigma R$   
 sub-cloud scales:  
 $\delta v(s) \sim (G\Sigma R)^{1/2} (s/R)^{1/2}$
- Sonic scale, where  
 $\delta v(L_{\text{sonic}}) = c_s = 0.2 \text{ km s}^{-1}$   
 is  $L_{\text{sonic}} \sim 0.1 \text{ pc}$
- Simulations reproduce observed velocity scalings, anisotropy

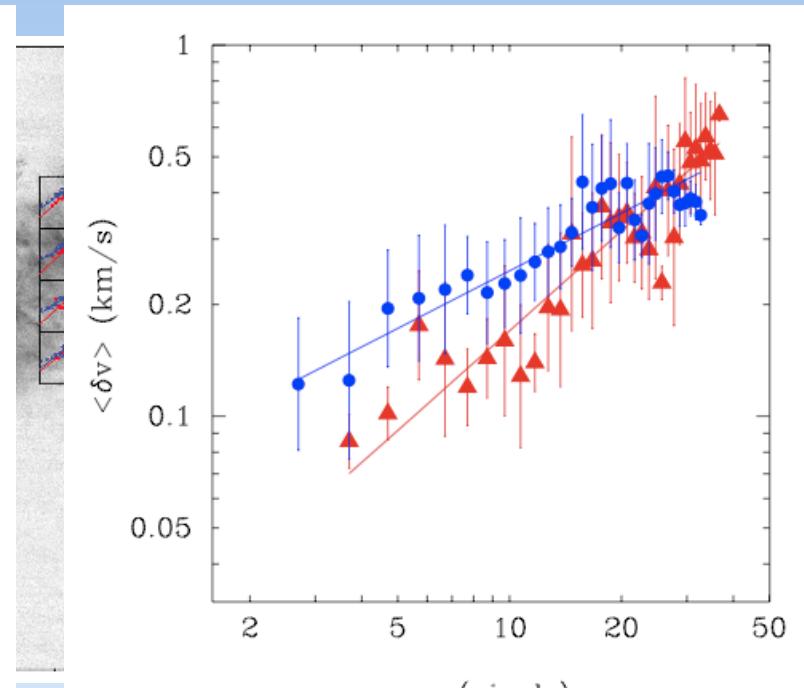


$$\sigma_v = 0.7 (\Sigma_{\text{GMC}} / 100 M_\odot \text{ pc}^{-2})^{1/2} (R / 1 \text{ pc})^{1/2} \text{ km s}^{-1}$$



Velocity vs. size scale (synthetic CO observation based on simulations)

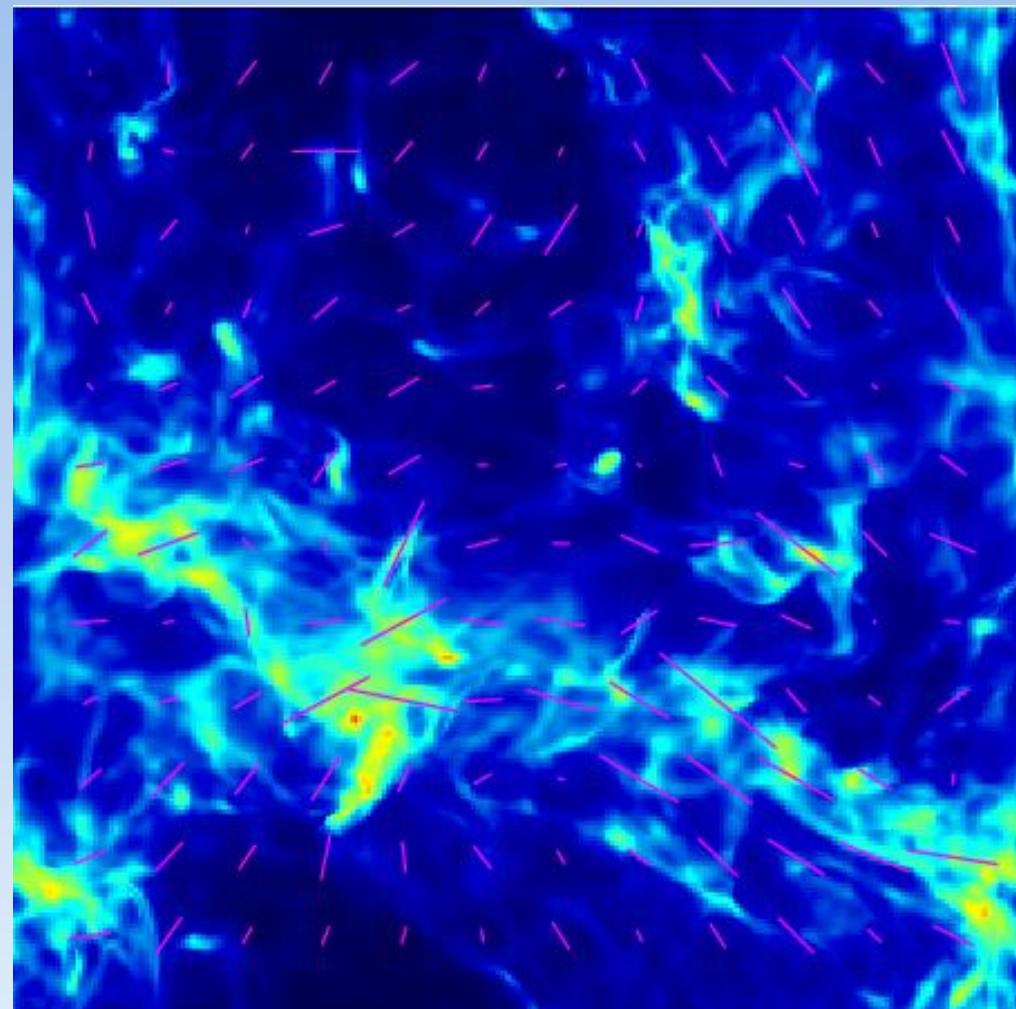
Heyer et al (2008); Heyer & Brunt (2012)



Velocity vs. size scale (CO observation in Taurus)

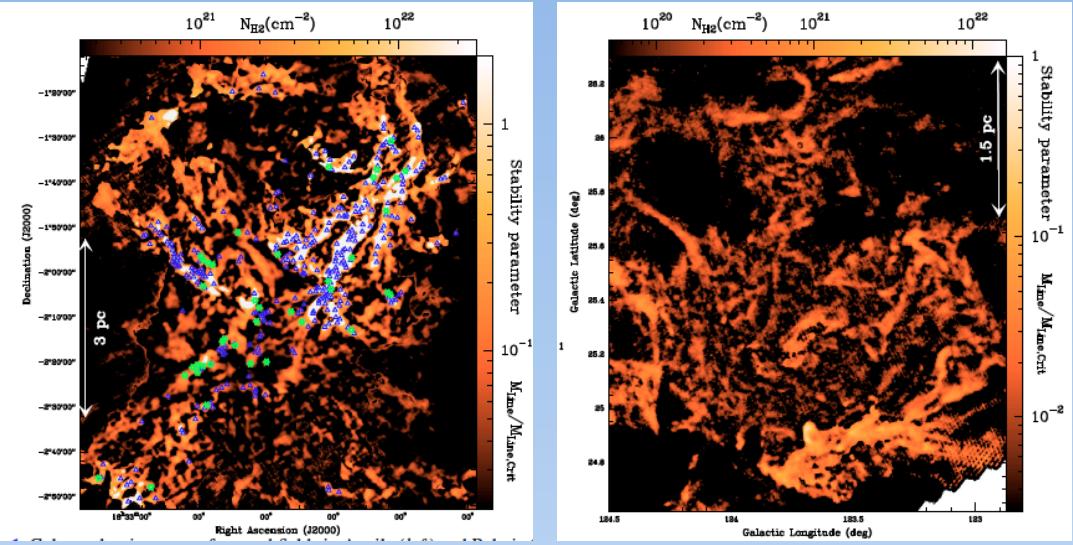
# Turbulence and density structure

- Because compression is due to turbulence, and largest-scale velocities dominate the turbulence  
    ⇒ the largest scales also dominate the density structure
- This has important consequence that star formation lies along **filaments** and is **clustered**

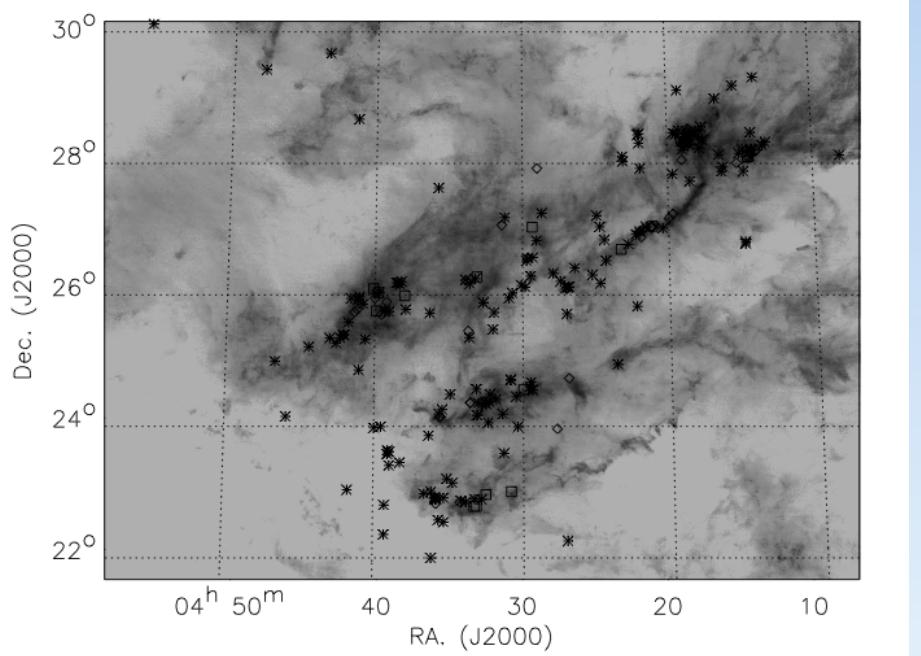


Ostriker, Stone & Gammie (2001)

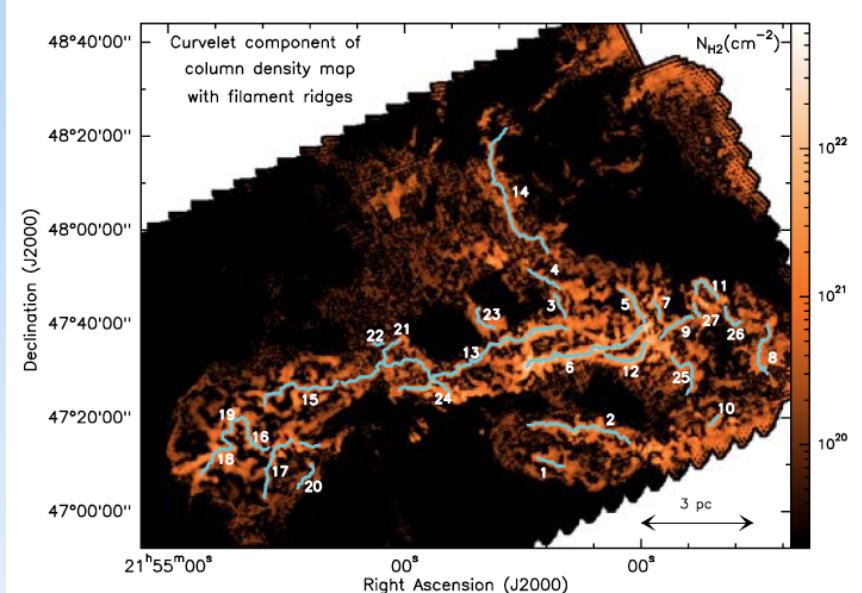
# Filaments in molecular clouds



Herschel: Aquila; Polaris Flare (Andre et al 2010)

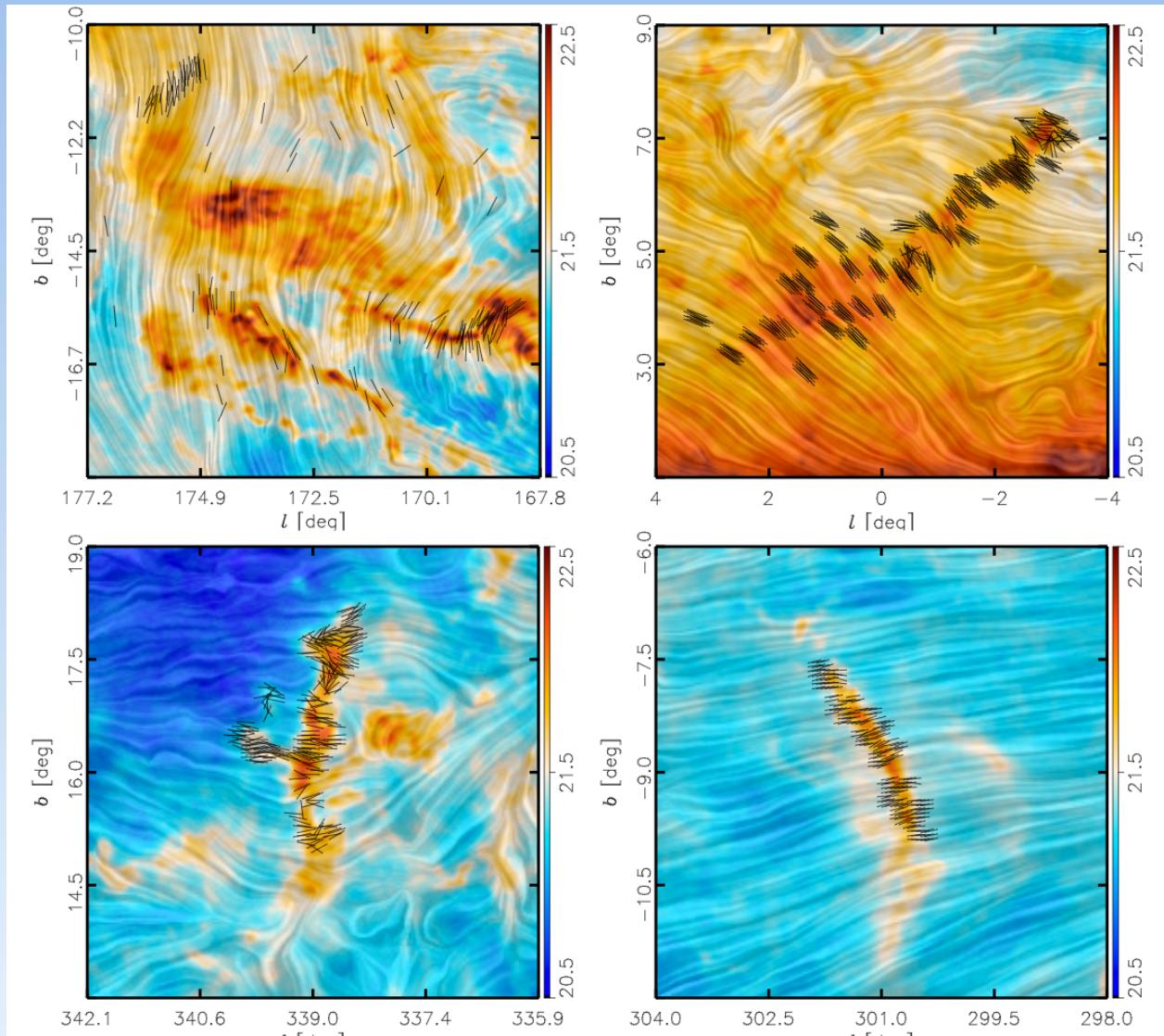


CO: Taurus cloud (Goldsmith et al 2008)



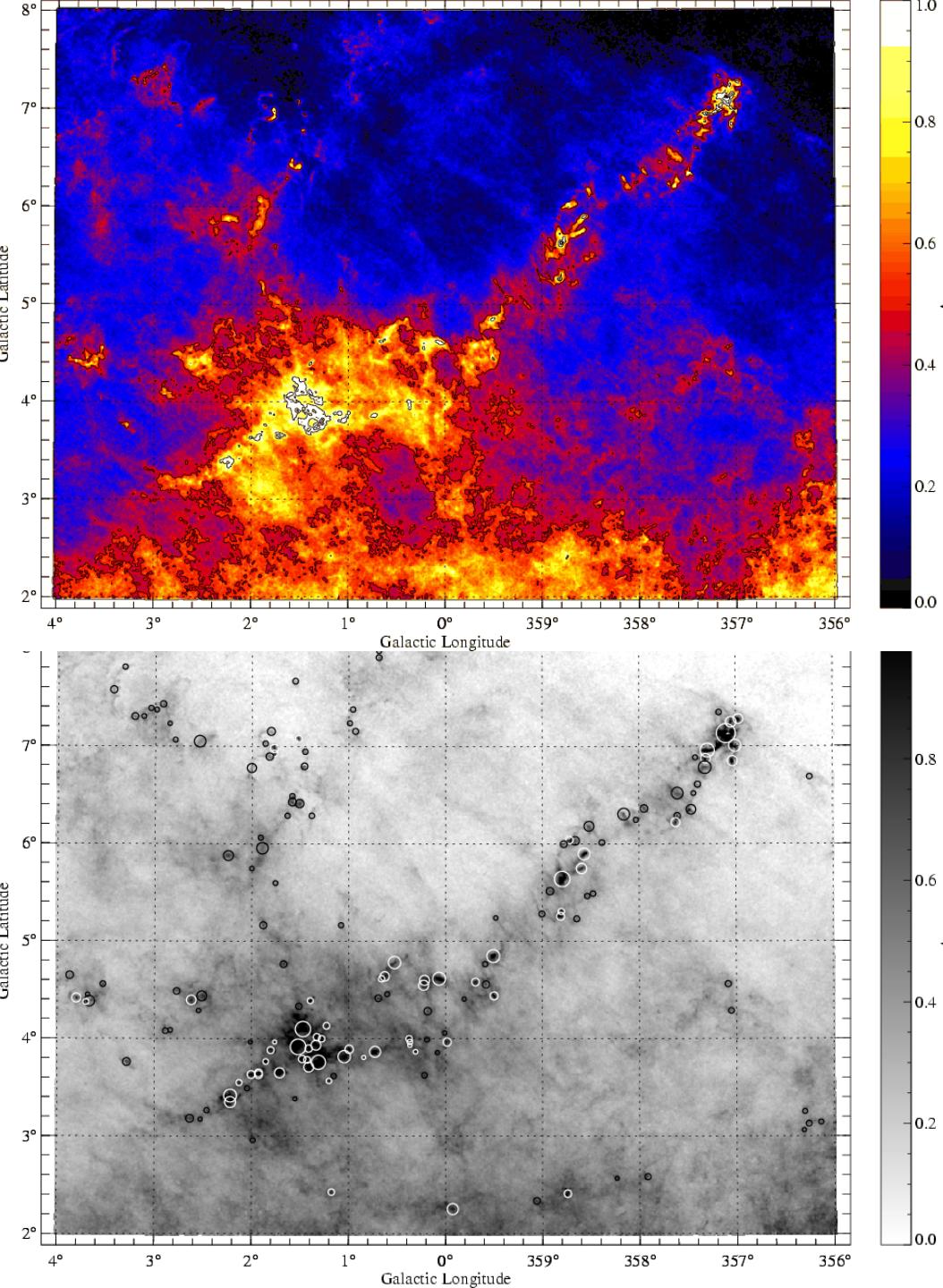
Herschel: IC 5146 (Arzoumanian et al 2011)

# Magnetic Field from Polarization



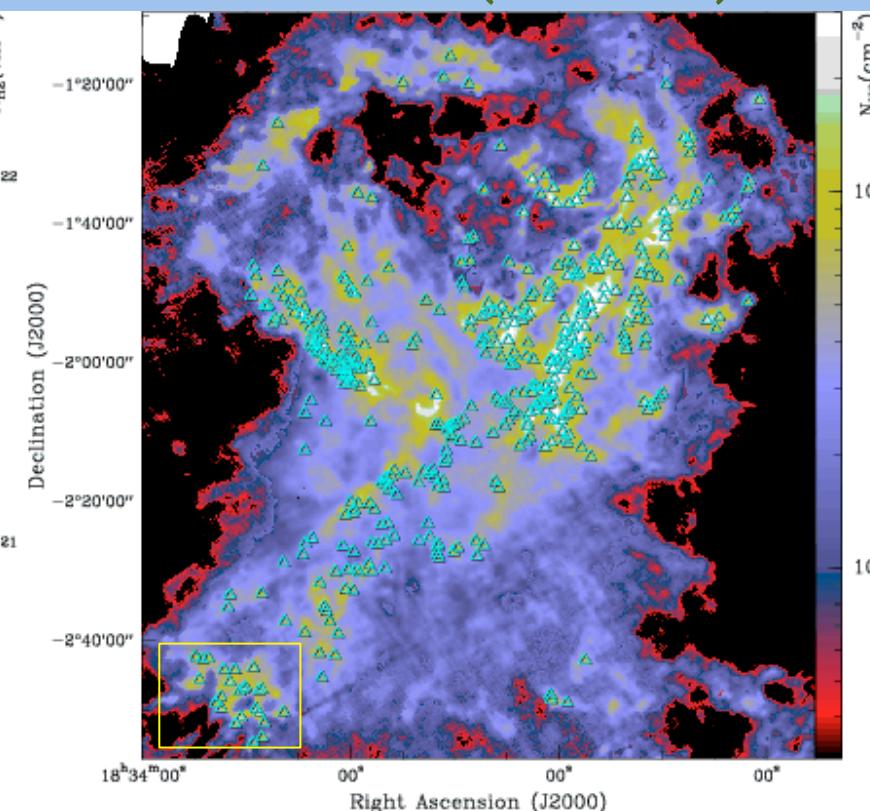
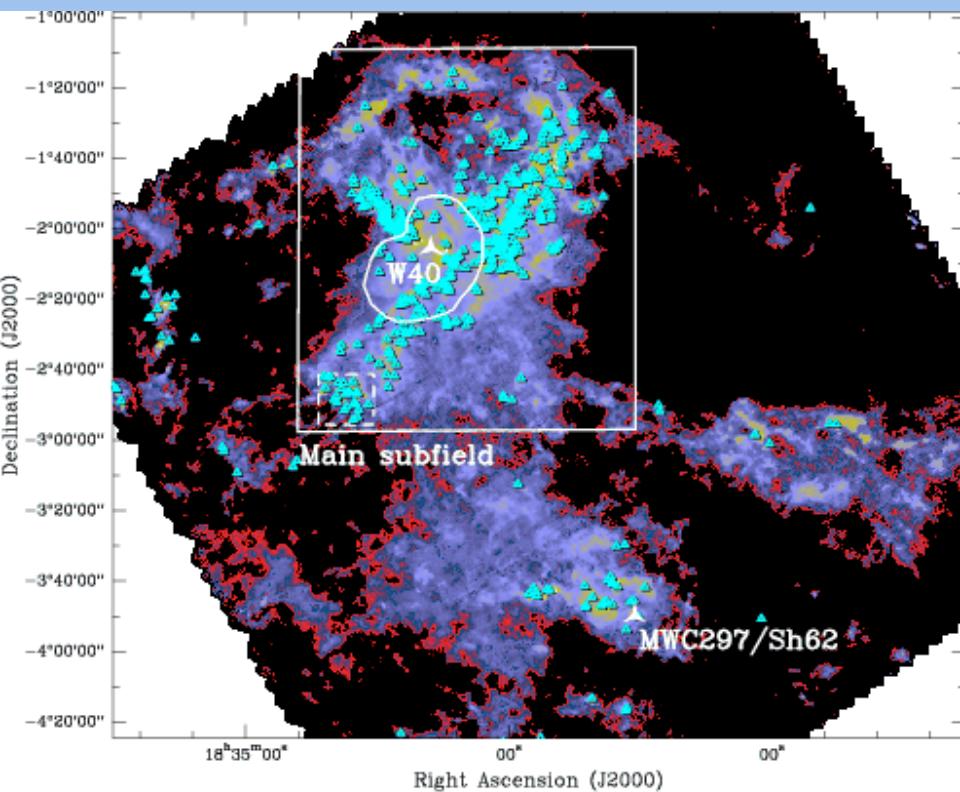
# Molecular cores

- Molecular cores ( $n > 10^4 \text{ cm}^{-3}$ ) are identified and observed using dense molecular tracers ( $\text{NH}_3$ ,  $\text{CS}$ ,  $\text{C}^{18}\text{O}$ , etc), mm, sub-mm, far-IR continuum, and extinction mapping

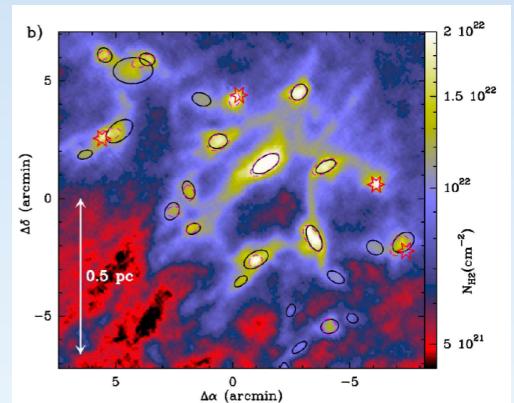


Pipe nebula extinction map and cores (Alves et al 2007)

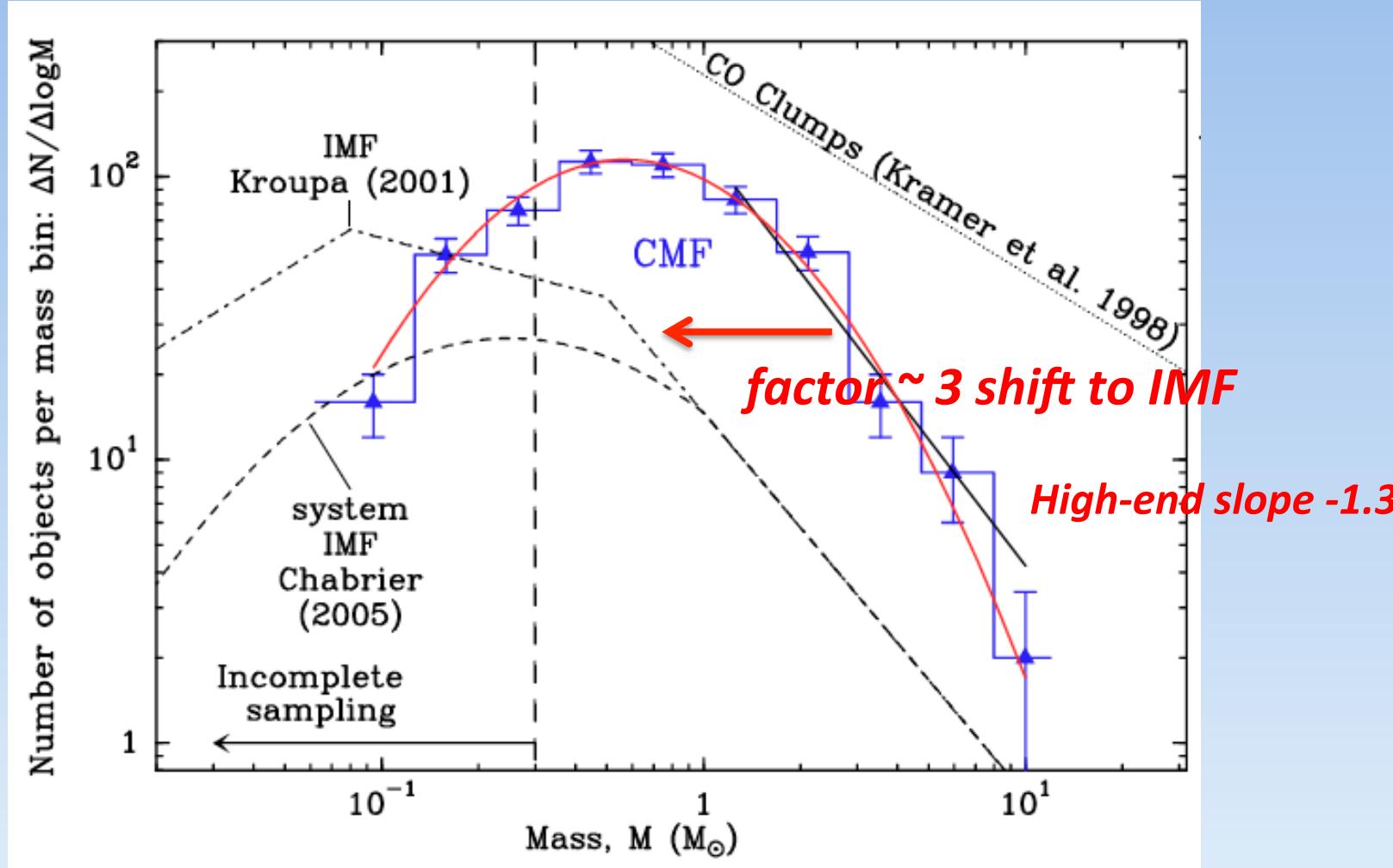
# Prestellar Core Mass Function (CMF)



Konyves et al (2010): Aquila cloud map with core positions from *Herschel* Gould Belt survey



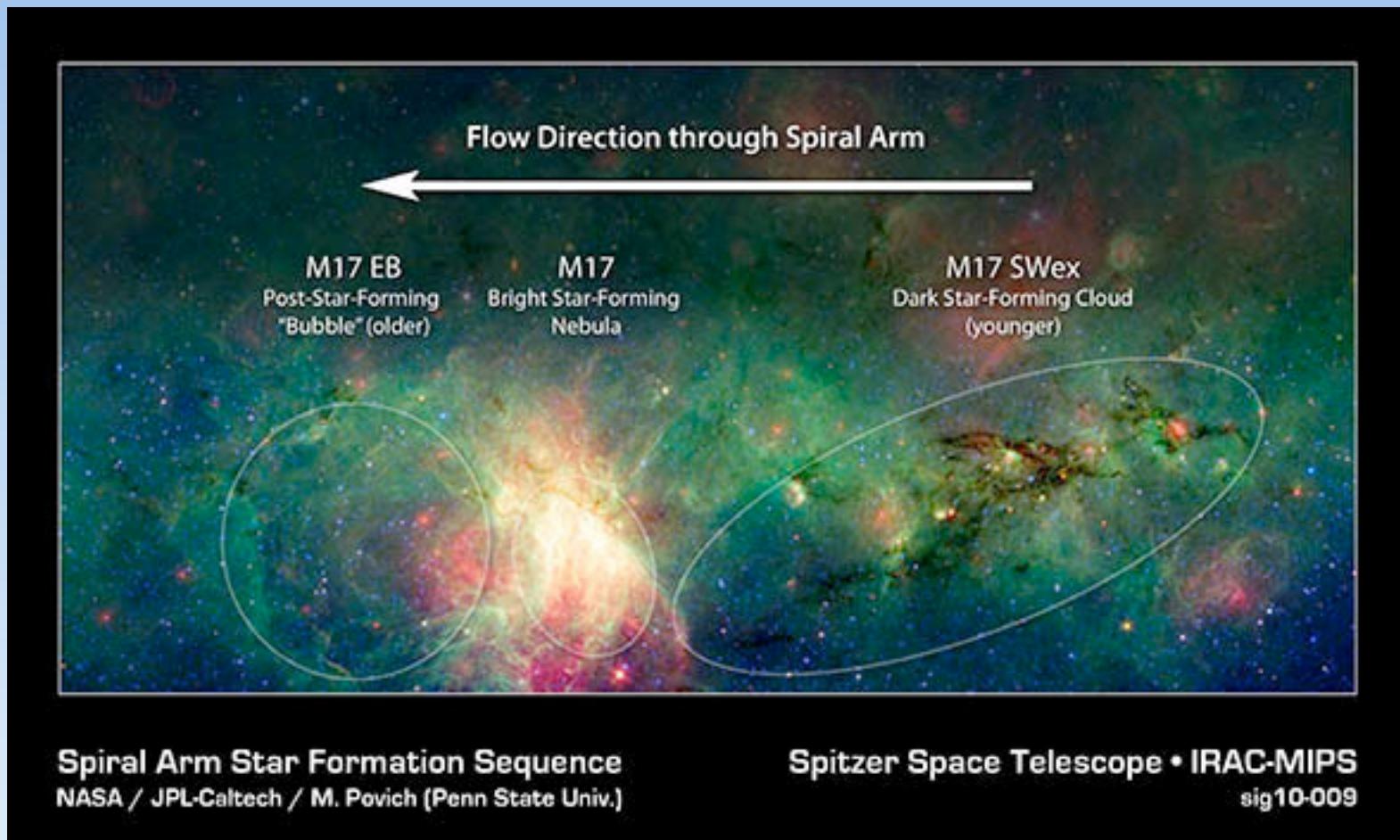
# Prestellar Core Mass Function (CMF)

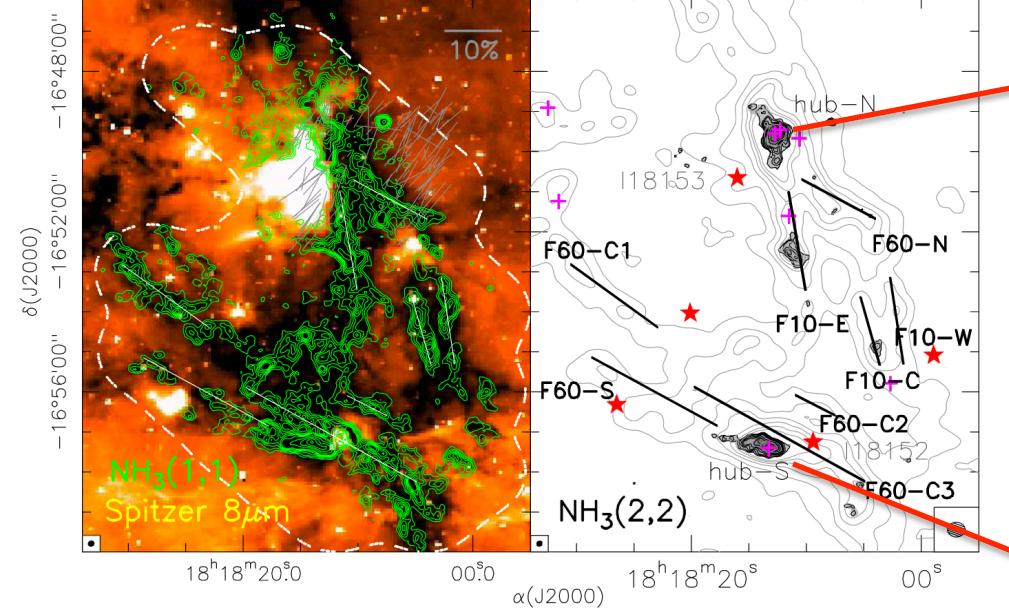


Konyves et al (2010): CMF in Aquila from *Herschel*

See also.: Motte et al (1998), Testi & Sargent (1998), Johnstone et al (2000), Onishi et al (2002), Enoch et al (2006), Alves et al (2007), Nutter & Ward-Thompson (2007)

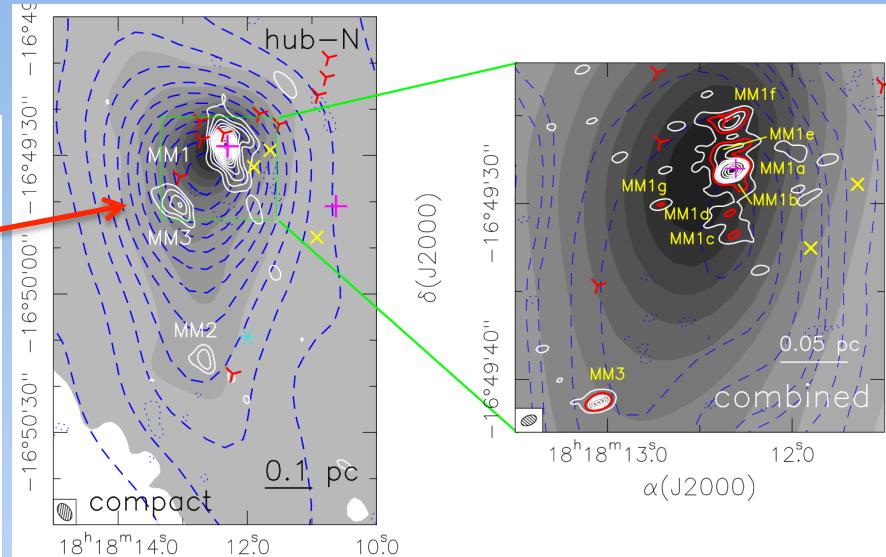
# IRDCs





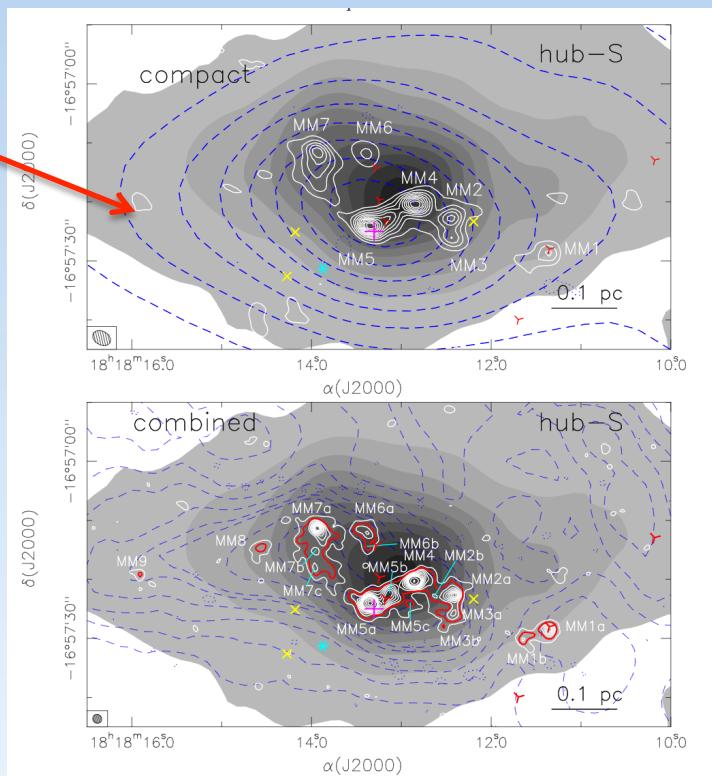
Busquet et al (2013)

- “Hubs” at high resolution break into cores with  $M \sim M_J$



7/26/16

Busquet et al (2016)



# Prestellar core properties

- High density:  $n \gtrsim 10^4 \text{ cm}^{-3}$
- Centrally concentrated; consistent with isothermal equilibrium “Bonnor Ebert” sphere

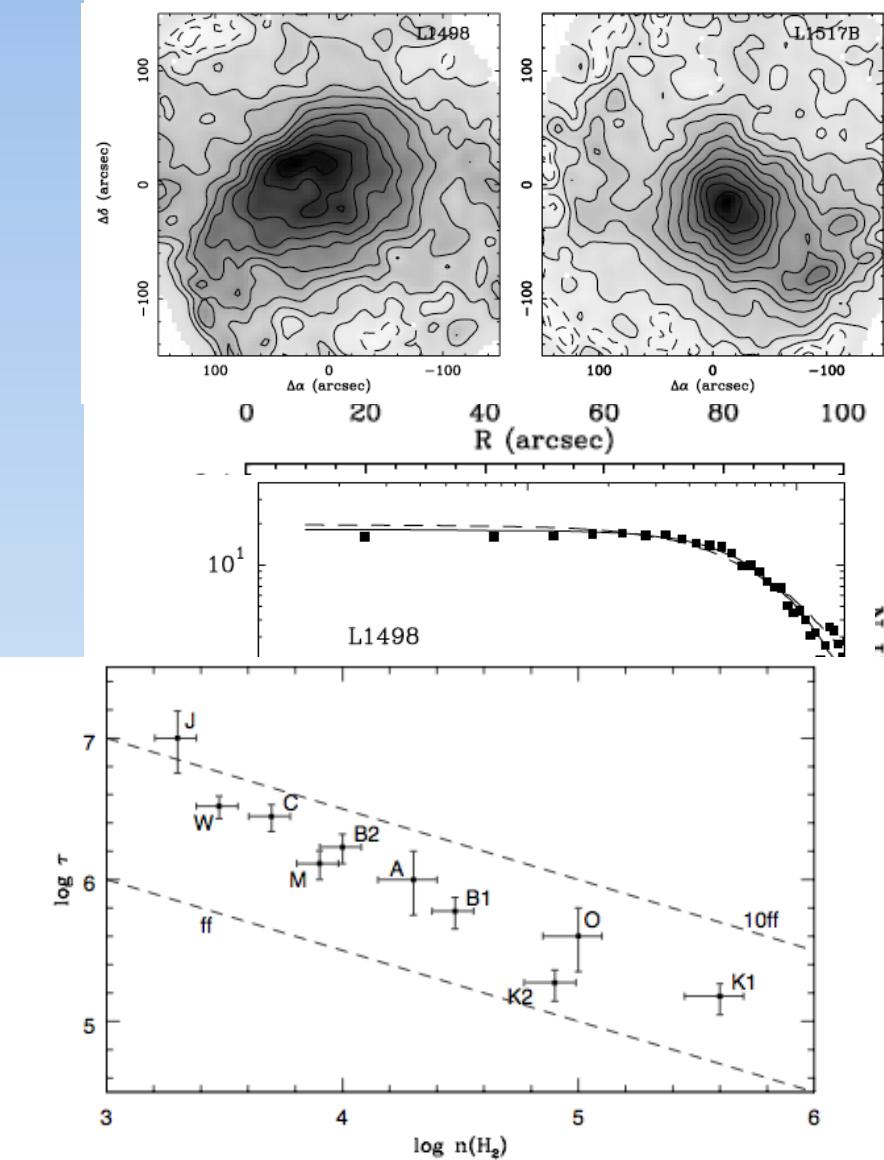
(Ward-Thompson et al 1994, Evans et al 2001, Caselli et al 2002, Lada et al 2003, Tafalla et al 2004, Kirk et al 2005, Kandori et al 2005)

- Subsonic internal turbulent velocity (Myers 1983; Goodman et al. 1998; Kirk et al. 2007; Andre et al 2007; Lada et al. 2008)
- Duration of prestellar phase  
~ few  $\times$  gravitational free-fall time

$$t_{ff} \equiv \left( \frac{3\pi}{32G\rho} \right)^{1/2} = 1.4 \times 10^5 \text{ yr} \left( \frac{n_H}{10^5 \text{ cm}^{-3}} \right)^{-1/2}$$

~ embedded protostellar lifetime

(Hatchell et al 2007, Ward-Thompson et al 2007, Enoch et al 2008, Evans et al 2009)



# Classical theory: isothermal spheres

- Maximum spherical mass that can be supported by thermal pressure at a given temperature and external pressure is the critical Bonnor-Ebert mass (Bonnor 1956, Ebert 1955):

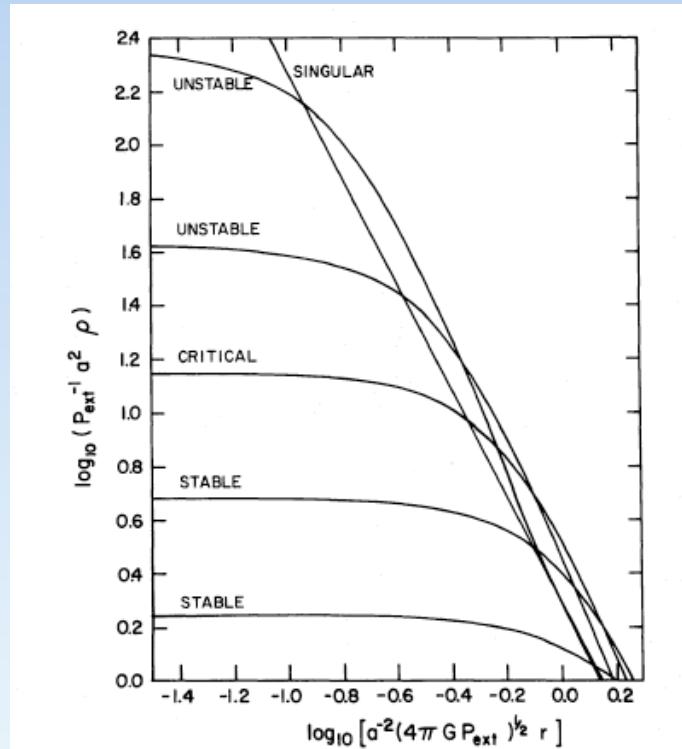
$$M_{BE} = 1.2 \frac{v_{th}^4}{(G^3 P_{edge})^{1/2}} = 1.2 \frac{v_{th}^3}{(G^3 \rho_{edge})^{1/2}} = 1.5 M_\odot \frac{(T / 10K)^{3/2}}{(n_{edge} / 10^4 cm^{-3})^{1/2}}$$

- More centrally-concentrated spheres are unstable, less concentrated spheres are stable

For critical BE sphere

- $\rho_c = 14\rho_{edge}$
- $\langle \rho \rangle = 2.5\rho_{edge}$
- $R = 0.4 GM/v_{th}^2$

Shu (1977)



Critical BE mass =

- $1/4.7 \times$  Jeans mass at edge P and T
- $1/3 \times$  Jeans mass at average P and T

# Exercise

- Integrate ODE to obtain solution to

$$\frac{1}{\xi^2} d_\xi [\xi^2 d_\xi \ln(\rho/\rho_0)] = -\frac{\rho}{\rho_0}$$

where  $\xi=r(4\pi G \rho_0)^{1/2}/v_{th}$  for  $\rho_0$  the central density of isothermal sphere with pressure  $P(r)=v_{th}^2 \rho(r)$ .

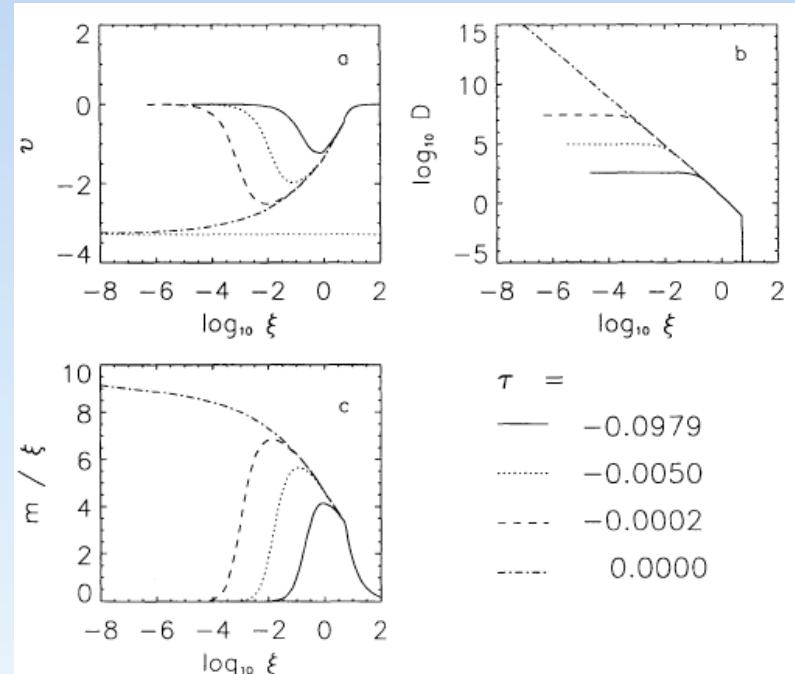
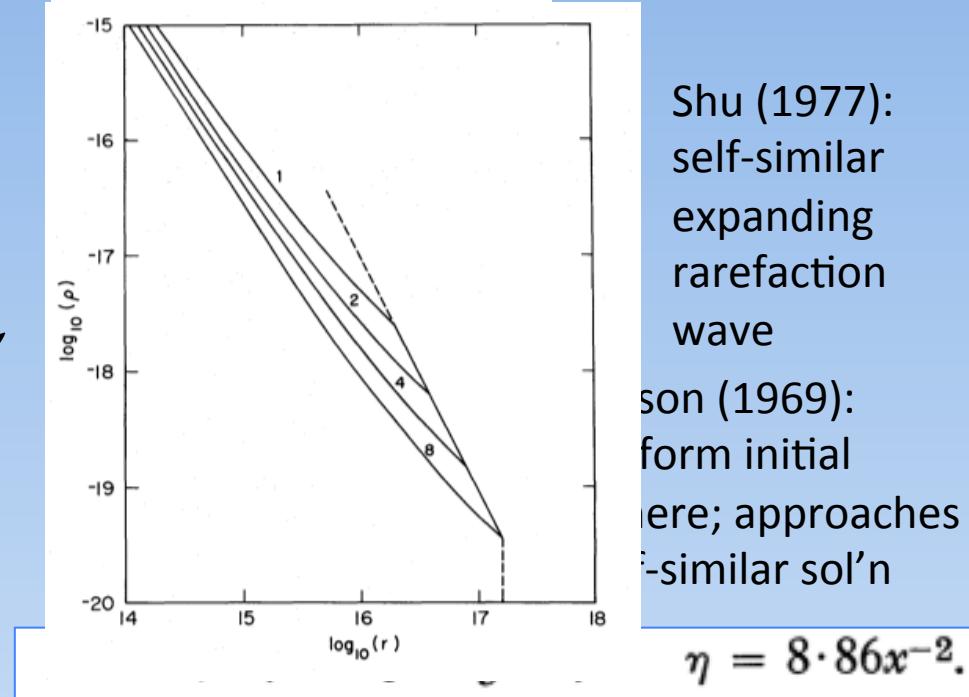
- Each  $\xi$  corresponds to a ratio  $\rho(\xi)/\rho_0=P_{\text{edge}}/P_0$
- Mass within  $\xi$  is 
$$M(\xi) = \frac{4\pi v_{th}^4}{(4\pi G)^{3/2} P_{\text{edge}}^{1/2}} \left( \frac{\rho(\xi)}{\rho_0} \right)^{1/2} \int^\xi d\xi' \xi'^2 \rho(\xi')/\rho_0$$
- Show that  $\xi=6.5$ ,  $\rho(\xi)/\rho_0=14$  yields the maximum mass for a given external pressure  $P_{\text{edge}}$ . Show that this  $M(\xi)=M_{\text{BE,crit}}$ .

# Core collapse

- Collapse of initial unstable static core is “outside-in” (Larson 1969, Penston 1969) followed by “inside-out” (Shu 1977, Hunter 1977)
- Inside initially has low velocity; wave of collapse starts in outer core and redistributes mass to attain singular profile:

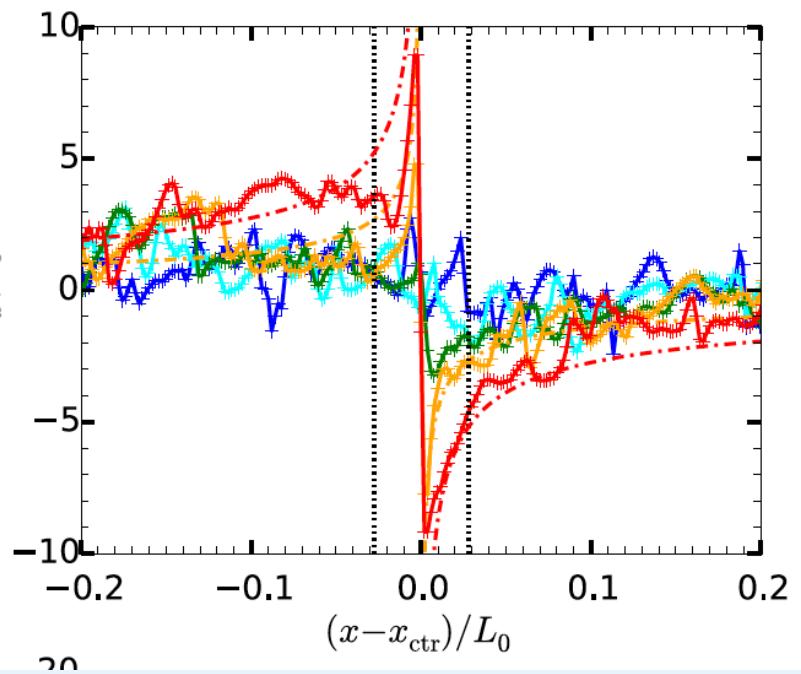
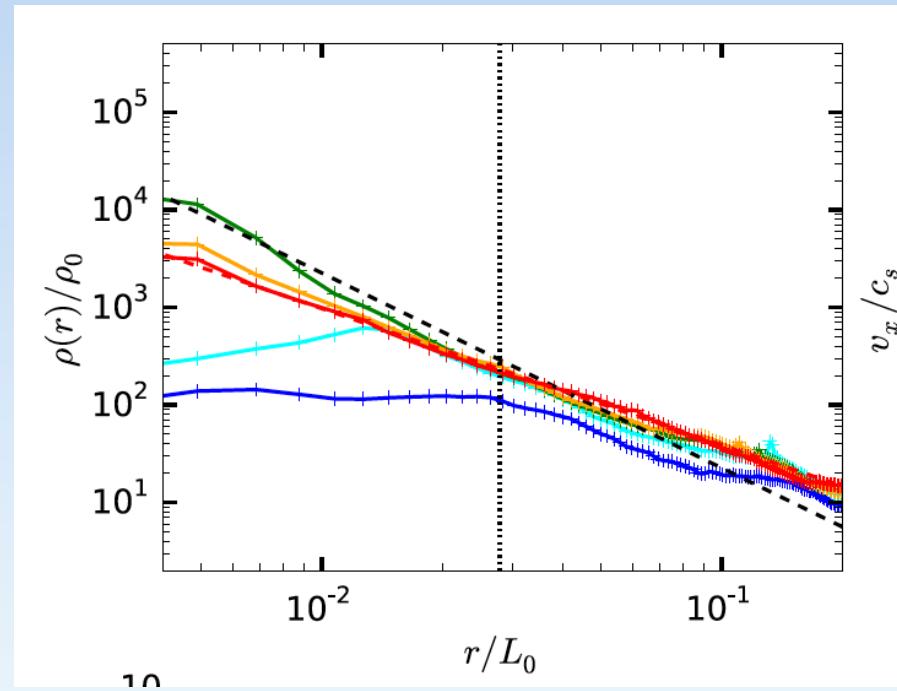
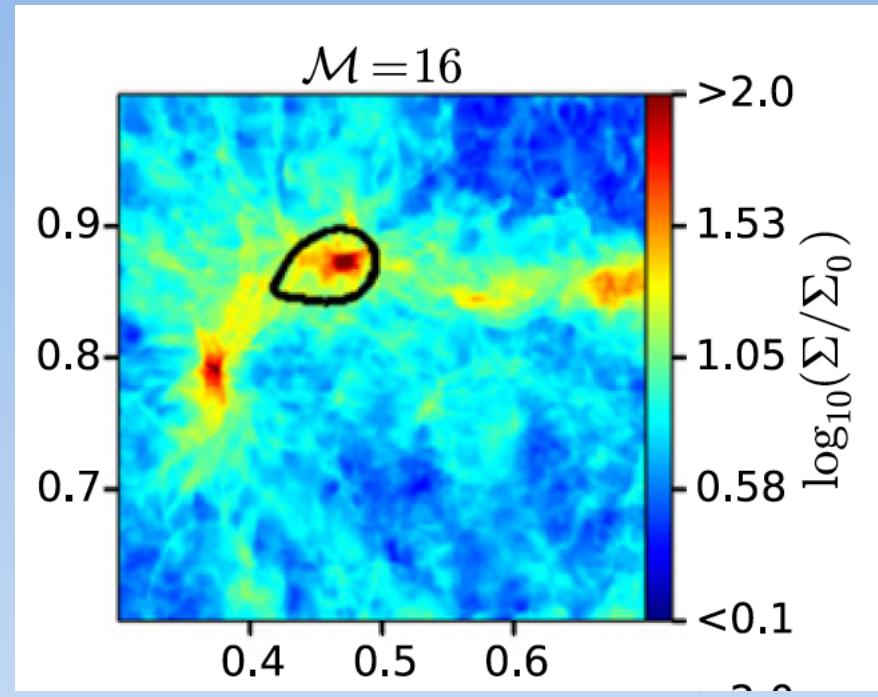
$$\rho_{LP} = 8.9 \frac{c_s^4}{4\pi G r^2}$$

- After central density  $\rightarrow \infty$ , rarefaction starts to propagate outward from the center as gas accretes onto the protostar:  
 $t_{\text{infall}}(r) \propto \rho^{-1/2} \propto r$
- In infalling region,  
 $v \propto r^{-1/2}, \rho \propto r^{3/2}$



# Core collapse in simulations

Gong & Ostriker (2015)



# Gravitational collapse: sink particle

- Singular density profile implies collapse become *unresolved*
- Numerical approach: introduce a “sink particle”
- Various different criteria and implementations

Bate et al 1995, Krumholz et al 2004, Federrath et al 2010, Wang et al 2010, Teyssier et al 2011, Gong & Ostriker 2013

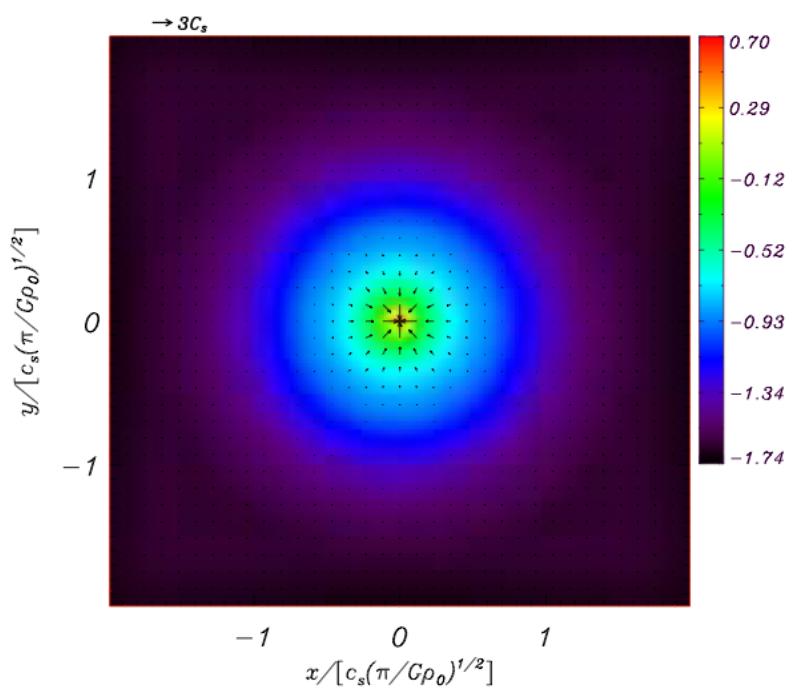
EG: density threshold

$$\text{Truelove (1997): } \rho_{Tr} = \frac{\pi}{16} \frac{c_s^2}{G\Delta x^2} \quad \text{GO13: } \rho_{LP} = \frac{8.86}{\pi} \frac{c_s^2}{G\Delta x^2}$$

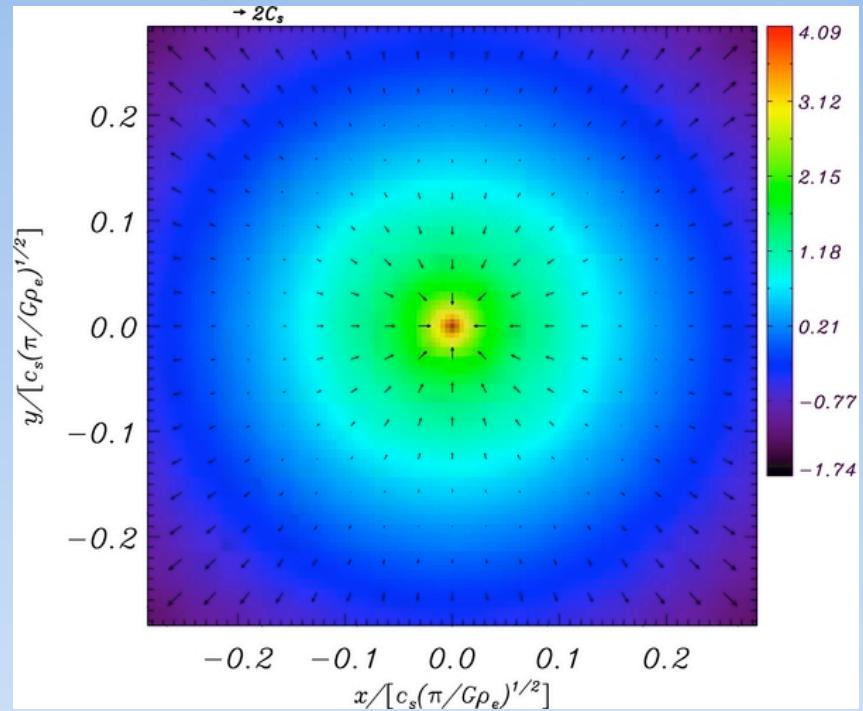
+ potential minimum, + converging flow

- Sink  $\mathbf{x}(t)$ ,  $\mathbf{v}(t)$  integrated as particle under gravity; mass grows by accretion
- Resolution must be high enough that inflow is *supersonic*
- Useful code test: Shu (1977) expansion wave sol’n

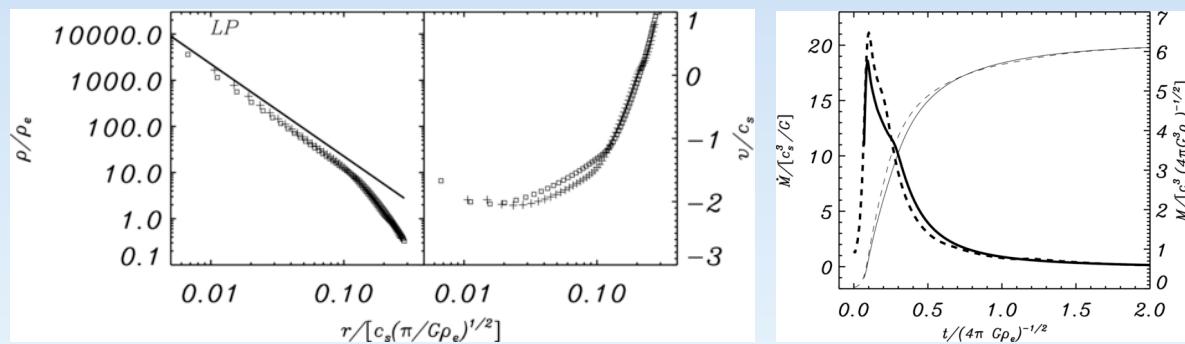
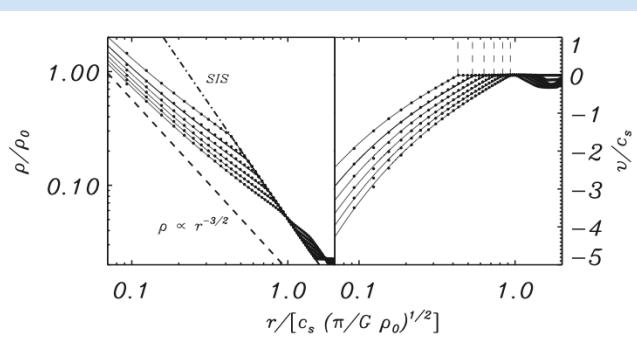
# Sink particles in *Athena*



Collapse of singular isothermal sphere

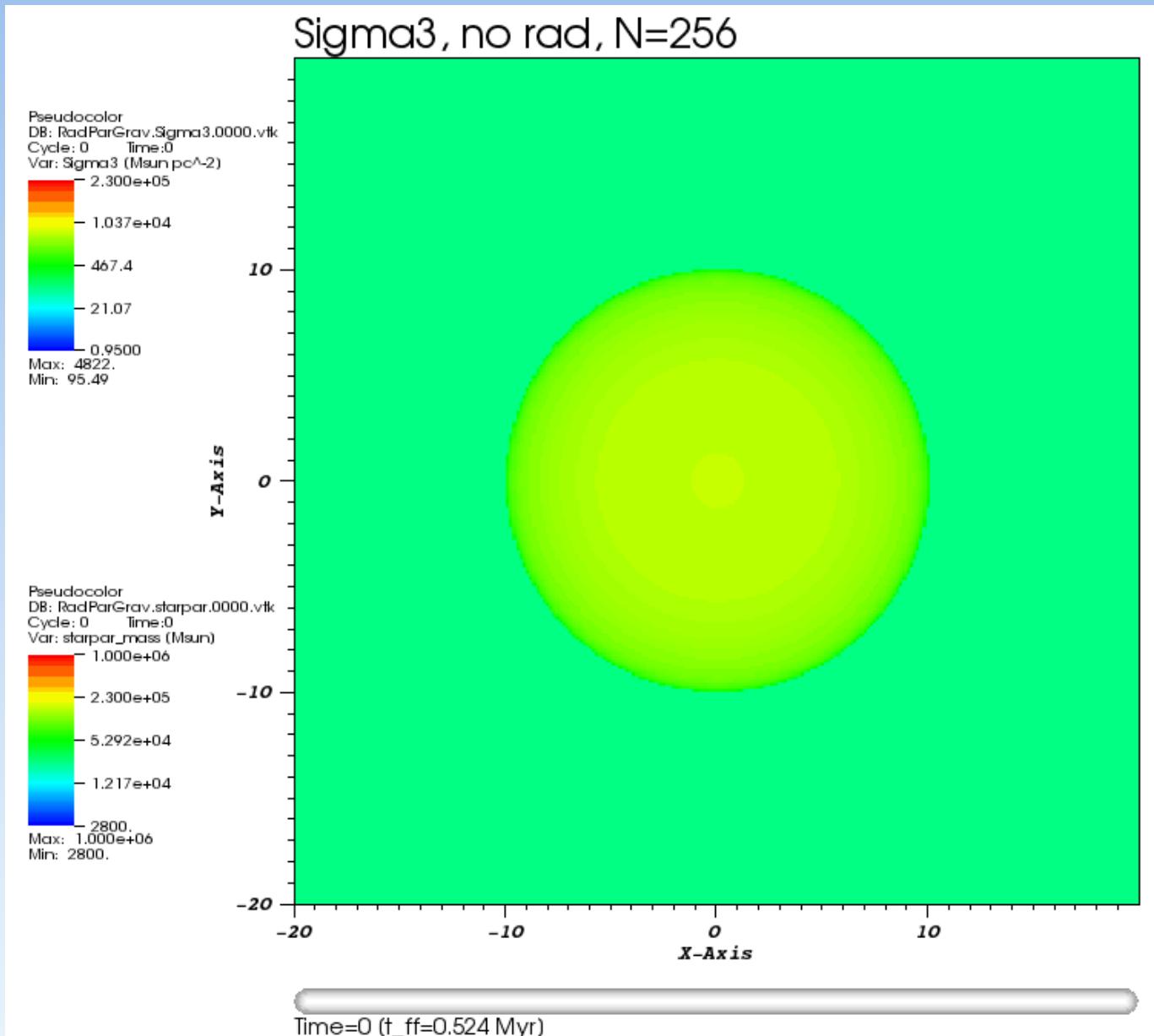


Collapse of unstable BE sphere

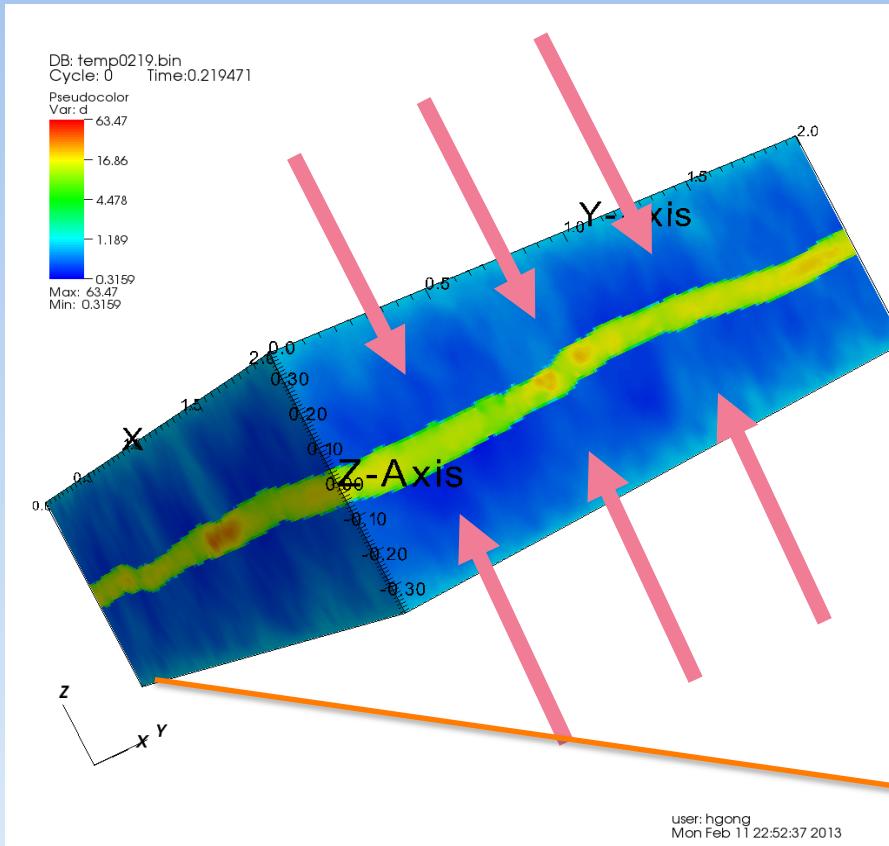


# Global cloud with sinks

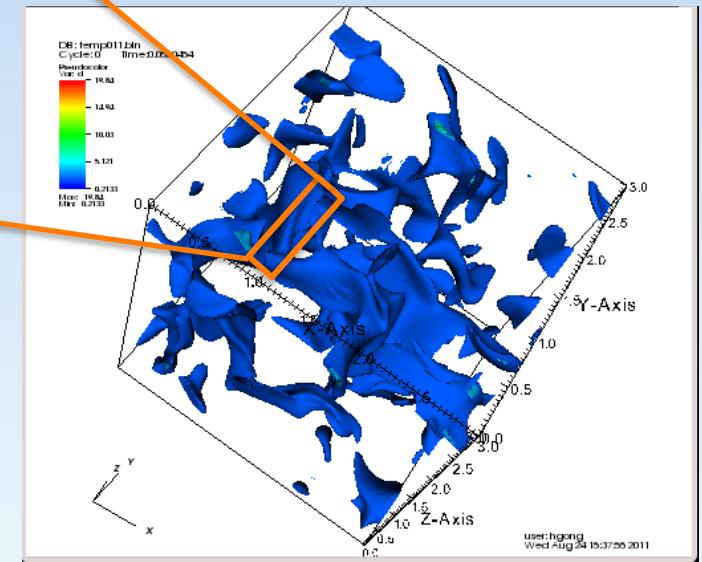
Skinner & Ostriker (2015)



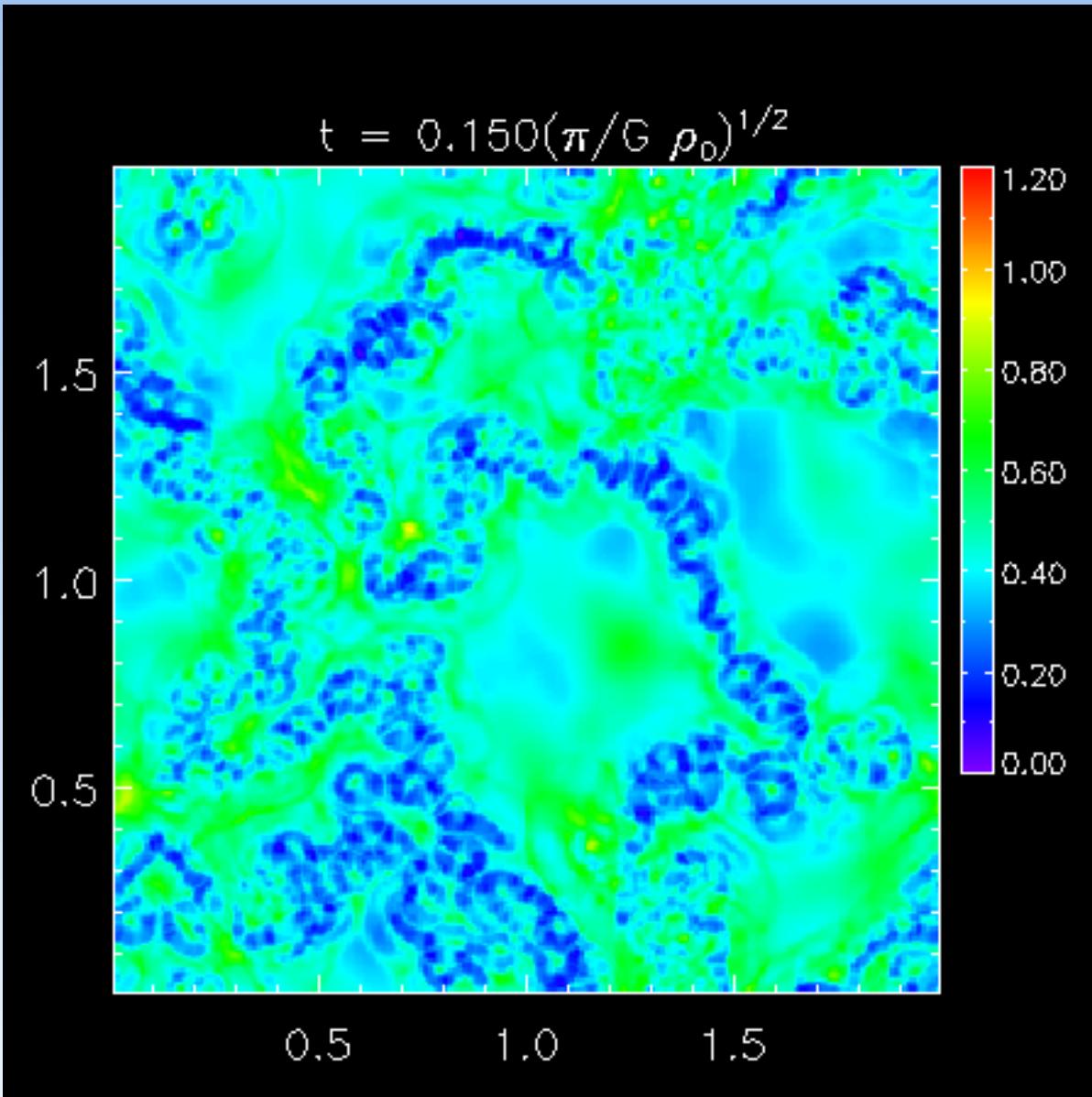
# Planar converging flow within a turbulent cloud



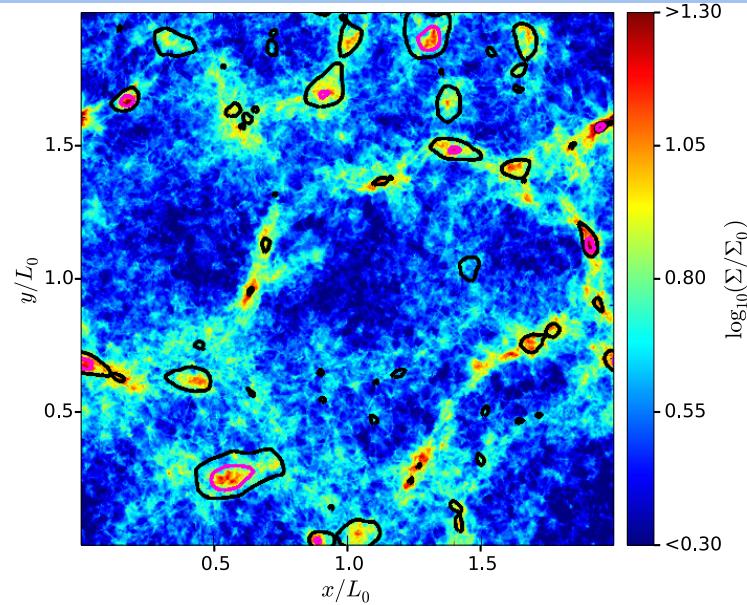
- Focus on local shocked region in a large cloud
- Range of inflow Mach numbers ( $v_{in}/c_s$ )
- Additional turbulence included



# Star formation in filaments

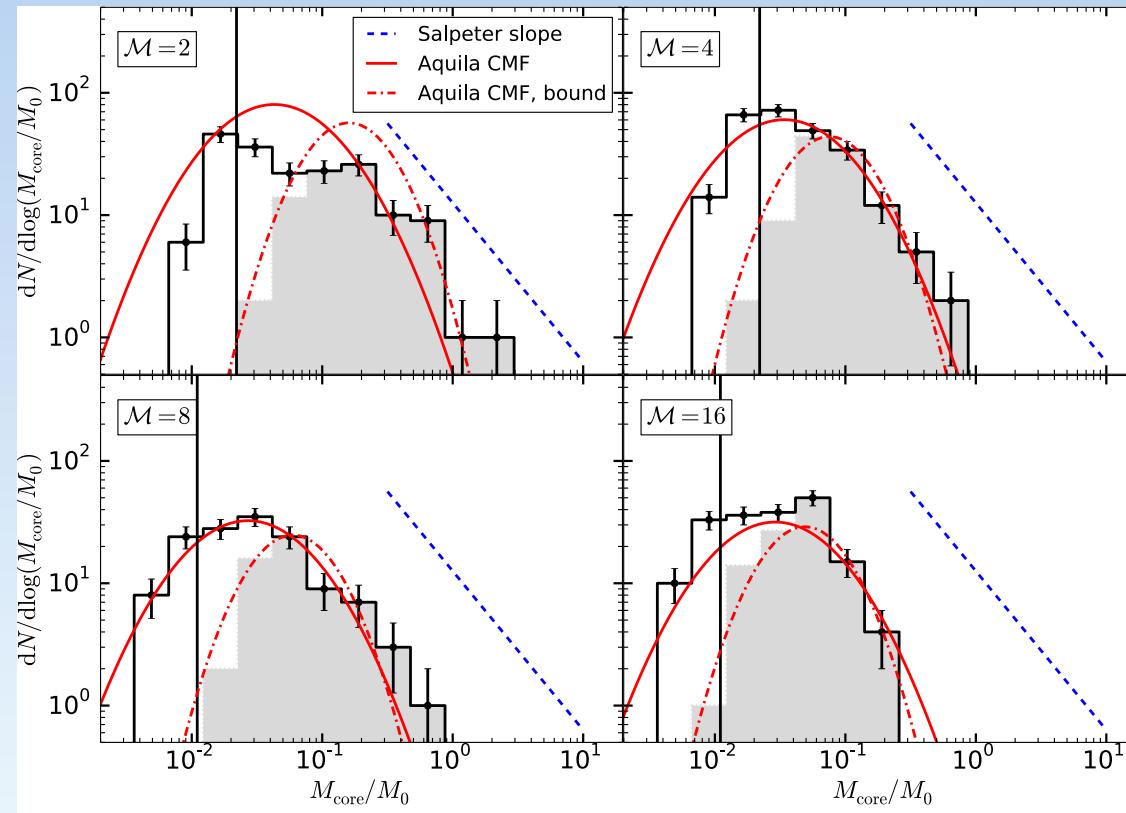


# Comparison to observed CMF

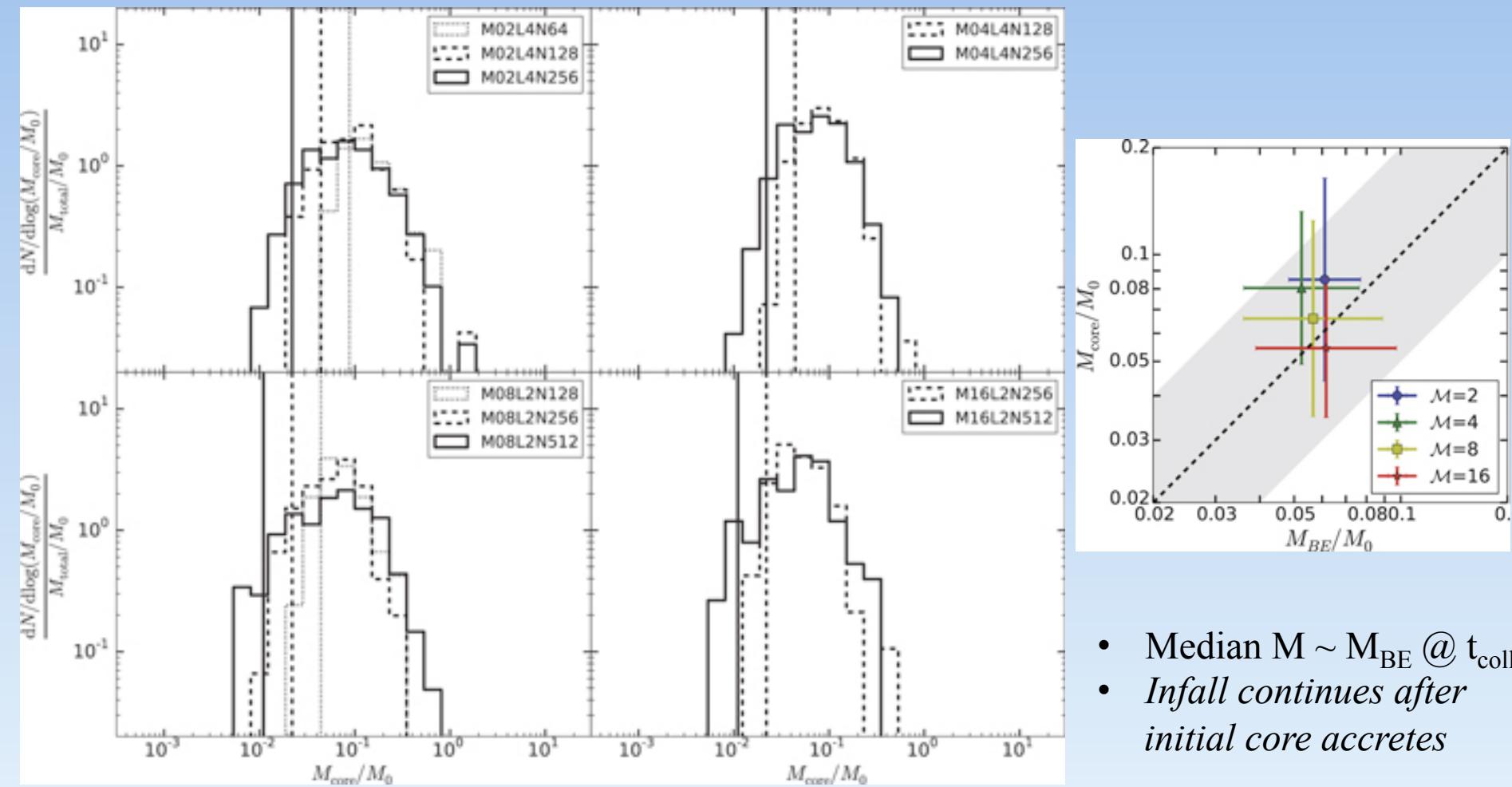


- Full CMF is similar to Aquila cores (Konyves 2010, from *Herschel*)
- CMF of bound cores also similar to Aquila bound cores
- High mass cores are lacking compared to IMF

Gong & Ostriker (2015)



# Convergence study: CMF



Gong & Ostriker (2015)

# Magnetic critical mass

- Mestel & Spitzer (1956): For object to contract gravitationally, must have:  $E_G \sim GM^2/R > E_B \sim (B^2/8\pi)(4\pi R^3/3)$

i.e.  $\frac{M}{\Phi} > \frac{1}{\pi\sqrt{6G}}$

*Note: conserved from flux freezing (Kunz lecture)*

- More exact solution for sphere:

(Mouschovias & Spitzer 1976)

$$\frac{M}{\Phi} > \frac{0.13}{\sqrt{G}}$$

- Cold cloud or sheet:

(Nakano & Nakamura 1978)

$$\frac{M}{\Phi} = \frac{\Sigma}{B} > \frac{0.17}{\sqrt{G}} \approx \frac{1}{2\pi\sqrt{G}}$$

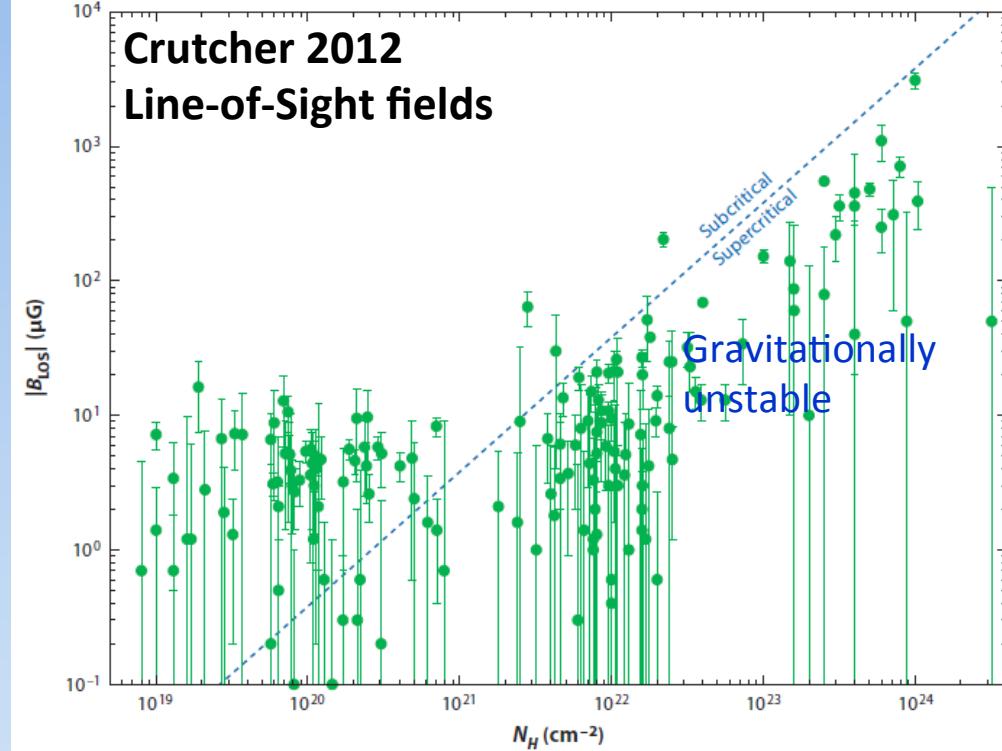
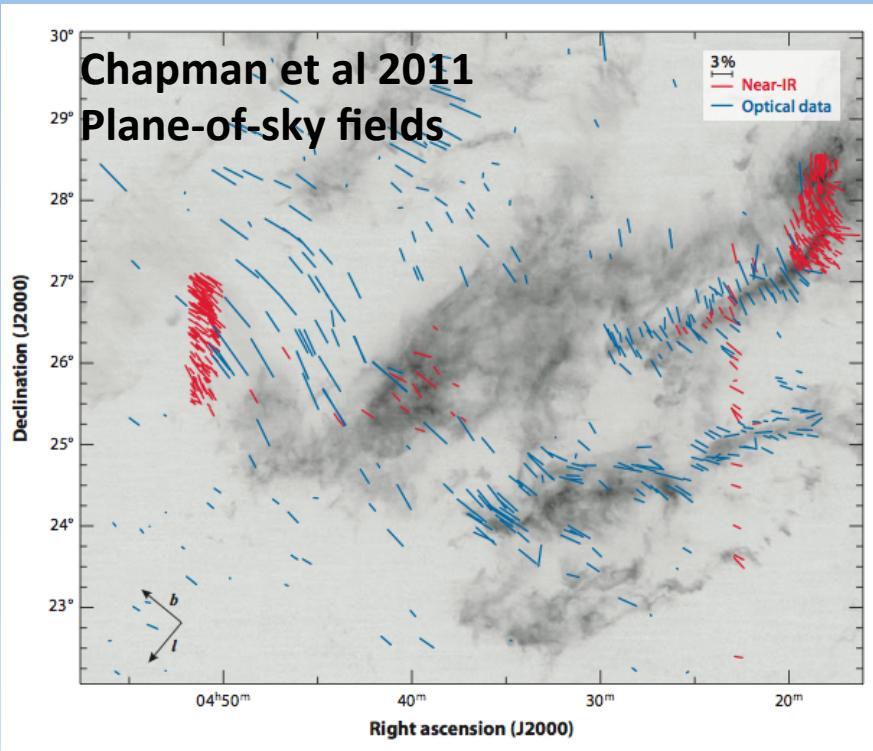
- Corresponds to minimum “gathering scale” along the magnetic field:

$$L_{crit} = \frac{B}{2\pi\sqrt{G}\rho} = 0.9\text{pc} \left( \frac{B}{10\mu\text{G}} \right) \left( \frac{n}{10^3\text{cm}^{-3}} \right)^{-1}$$

- For spherical core,

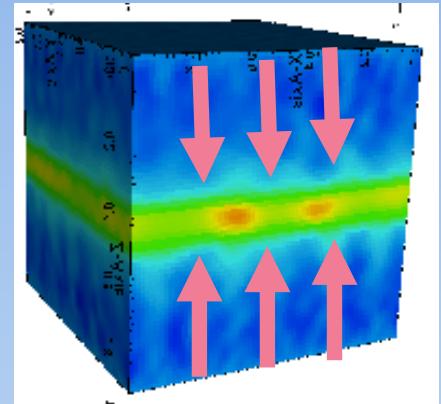
$$M_{crit,sph} = \frac{9B^3}{128\pi^2 G^{3/2} \rho^2} = 38M_\odot \left( \frac{B}{10\mu\text{G}} \right)^3 \left( \frac{n}{10^3\text{cm}^{-3}} \right)^{-2}$$

# Role of magnetic Fields

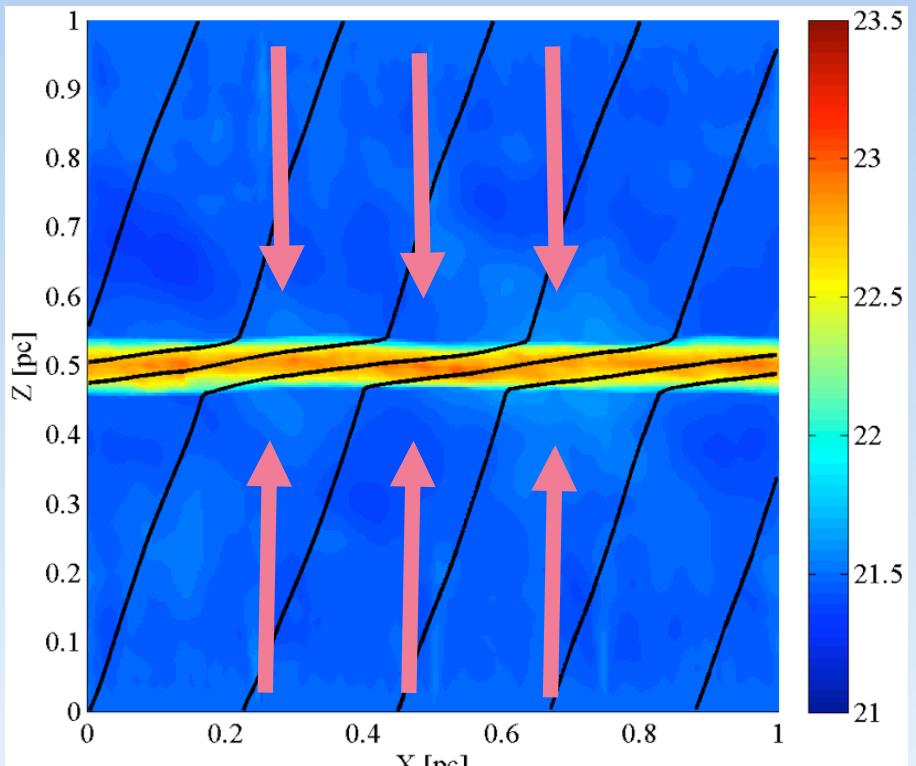


- Observed dense cores have  $M/\Phi \sim 2\text{-}3 \times$ critical value
- But:  $M_{\text{crit,sphere}} = 0.007 B^3/(G^{3/2} \rho^2)$  for “pre-core” gas is typically tens of  $M_\odot$  - much larger than observed cores
- Ambipolar diffusion in low-mass cores could reduce  $M/\Phi$  as neutrals drift inward relative to ions and the magnetic field (Mestel & Spitzer 1956)
- But:  $t_{\text{AD}} \sim 10 t_{\text{dyn}}$  for initially critical core (Mouschovias 1987) is longer than observed core lifetimes

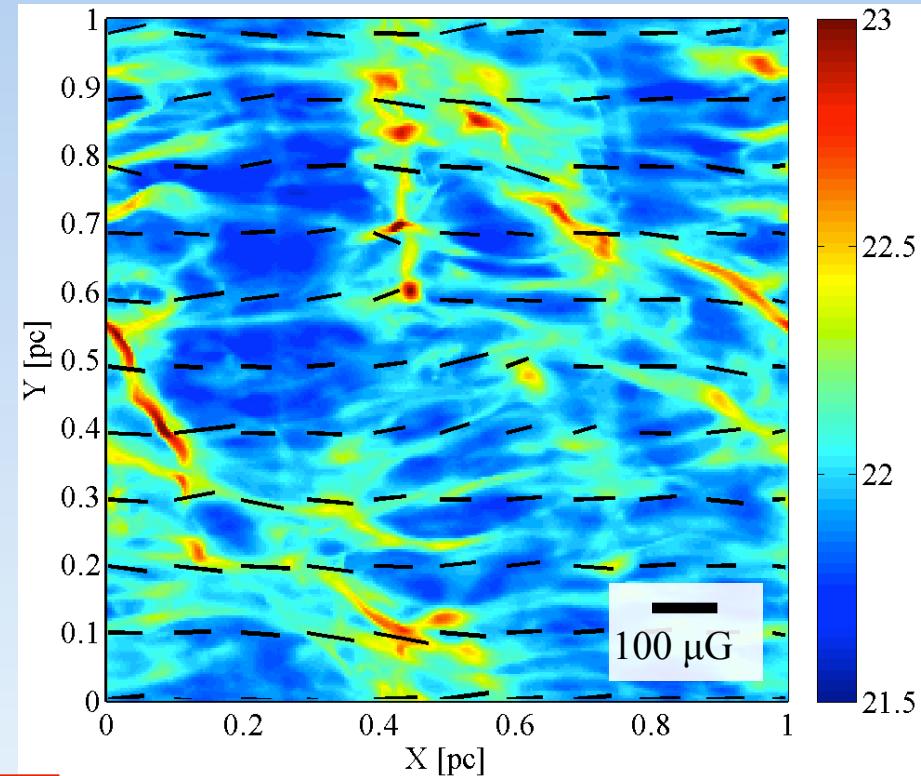
# Post-shock layer for magnetized model



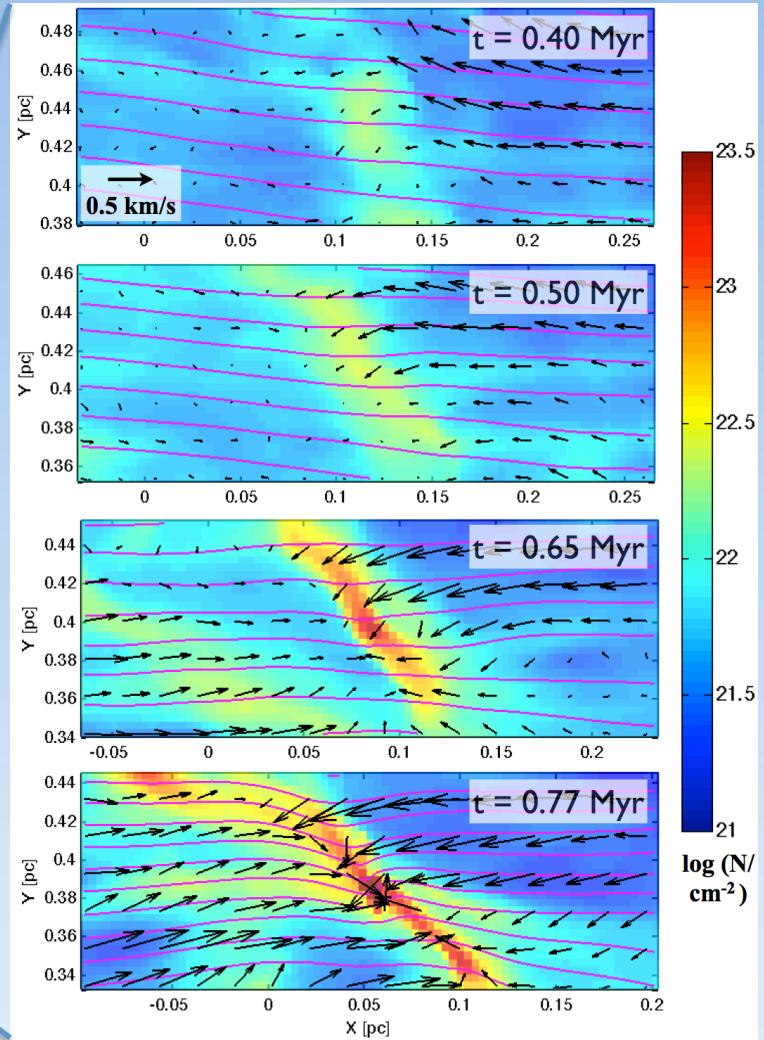
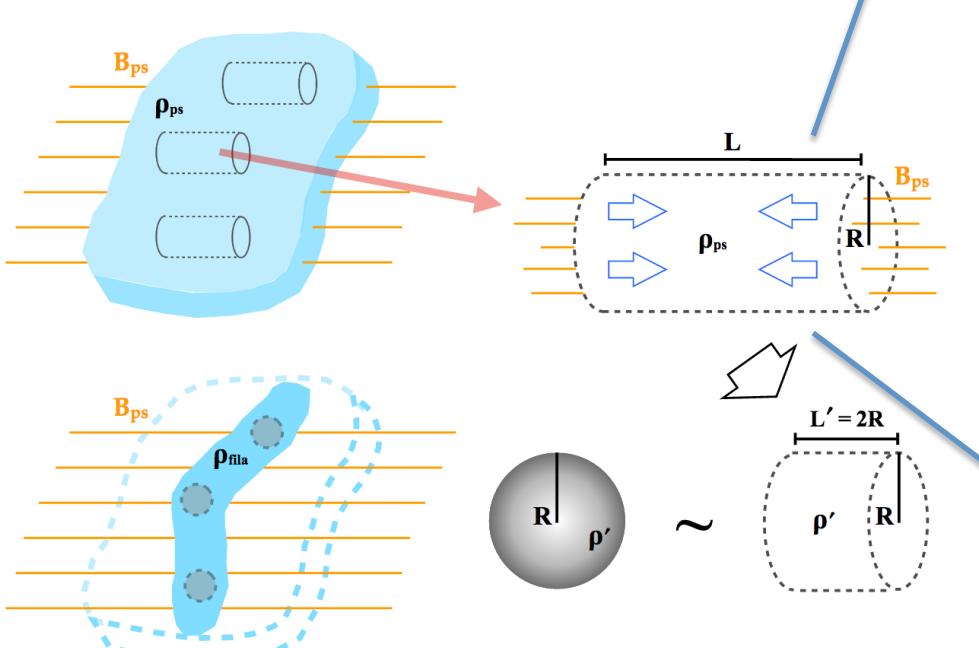
(Chen & Ostriker 2014)



$$B_{ps}^2/8\pi \sim \rho_0 v_0^2$$



# B-aligned flow for filament/core formation



# Exercise

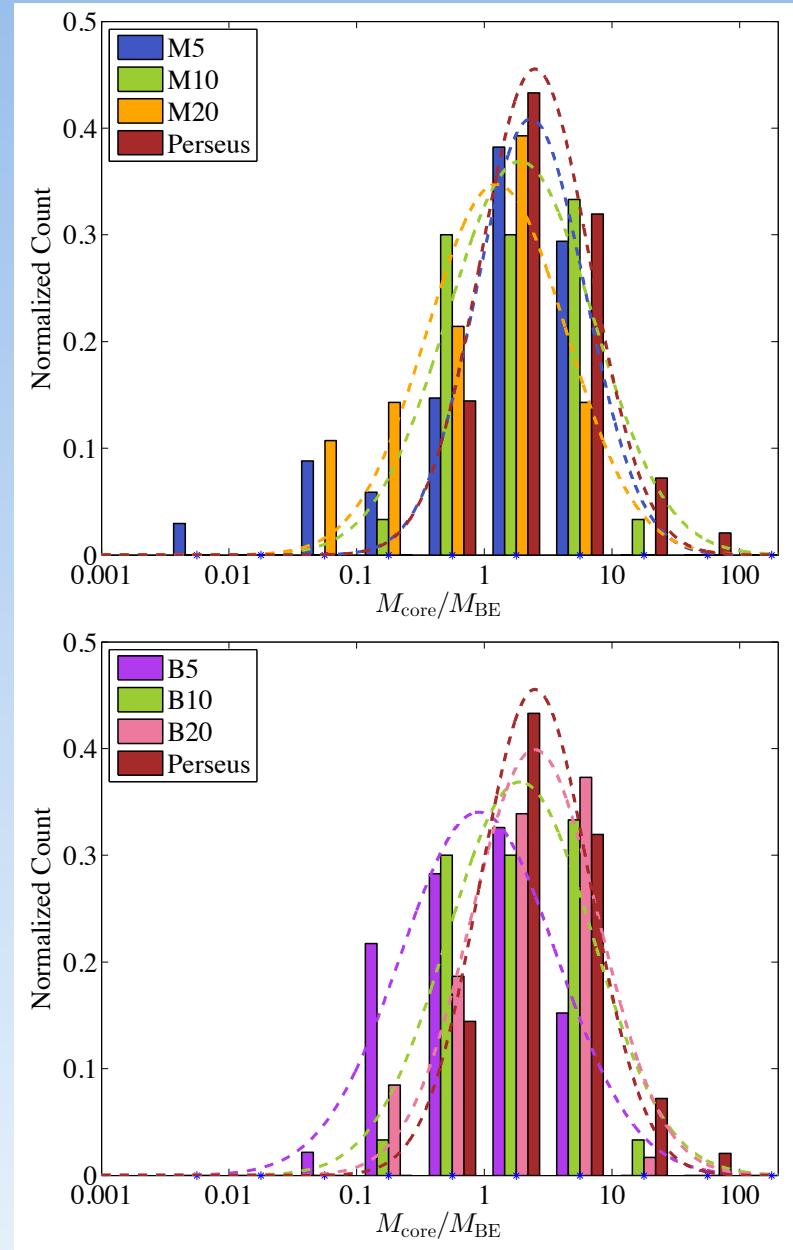
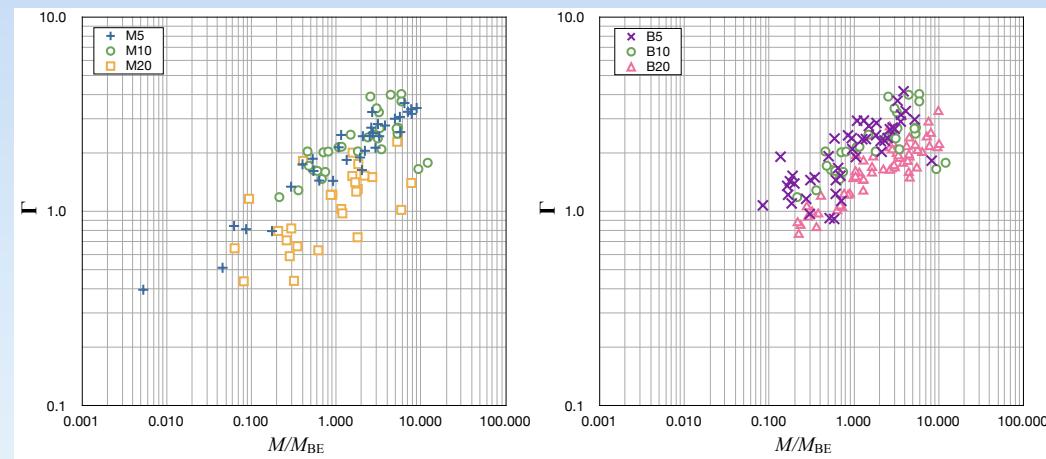
- Consider post-shock layer with  $B_{ps}^2/8\pi \approx \rho_0 v_0^2$
- Magnetic critical length along field has  $\rho_{ps}L_{crit} = B_{ps}/(2\pi G^{1/2})$
- Gas contracts along flux tube maintaining  $\rho L = \rho_{ps}L_{crit}$
- When  $L = R_{BE} = 0.8 v_{th}/(G\rho)^{1/2}$  a core that is both magnetically and thermally unstable can contract
- Show that this condition yields:

$$M = (4\pi/3) R_{BE}^3 \rho \approx 2v_{th}^4 / (G^{3/2} \rho_0^{1/2} v_0),$$

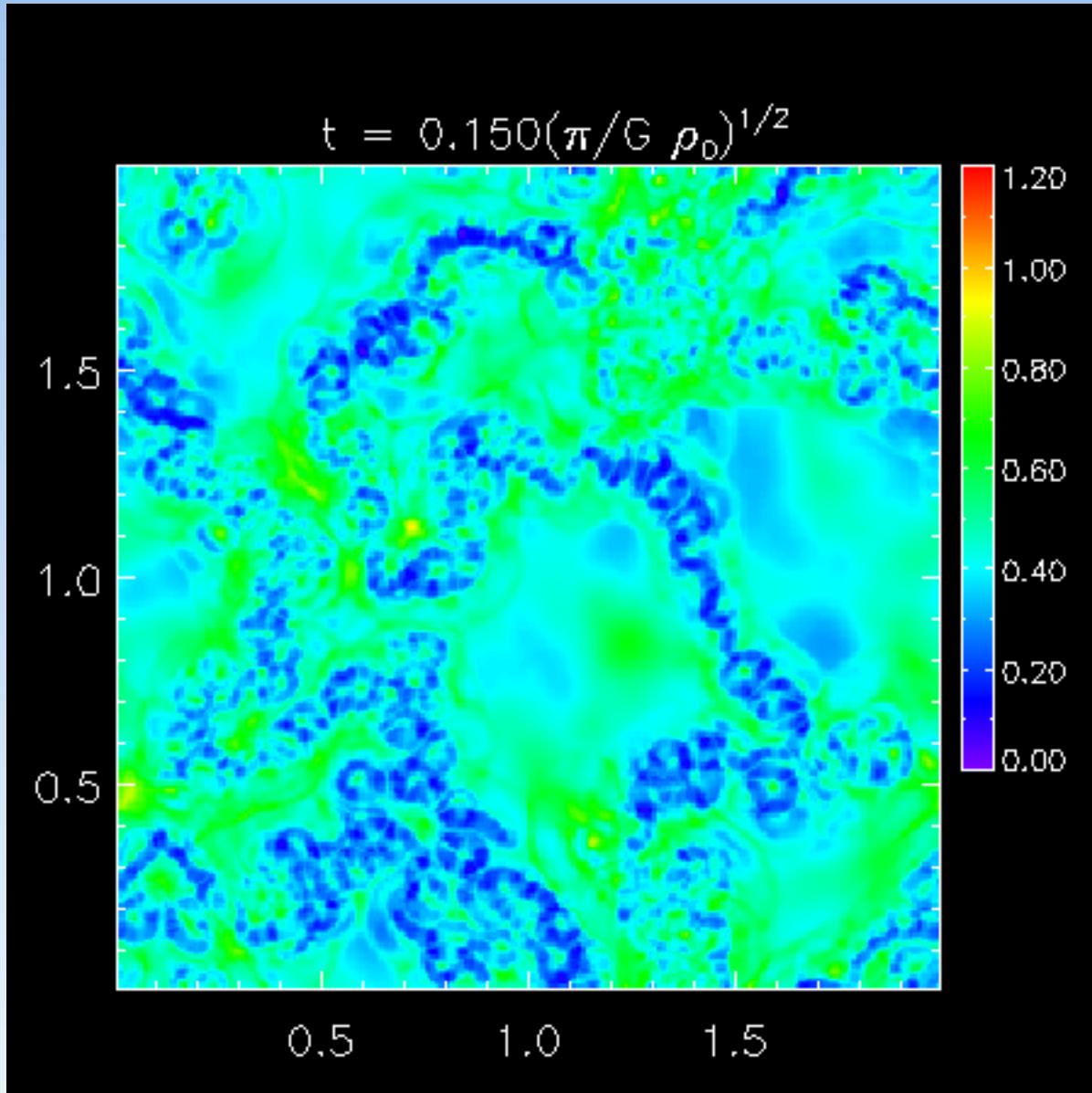
i.e. characteristic core mass is comparable to critical  $M_{BE}$  using  $P_{edge} = \rho_0 v_0^2$

# $M/M_{\text{BE}}$ & $M/\Phi$

- Distribution of mass relative to BE mass is similar to observed cores
- Cores with  $M/M_{\text{BE}} > 1$  in simulations are also magnetically supercritical,  $\Gamma > 1$

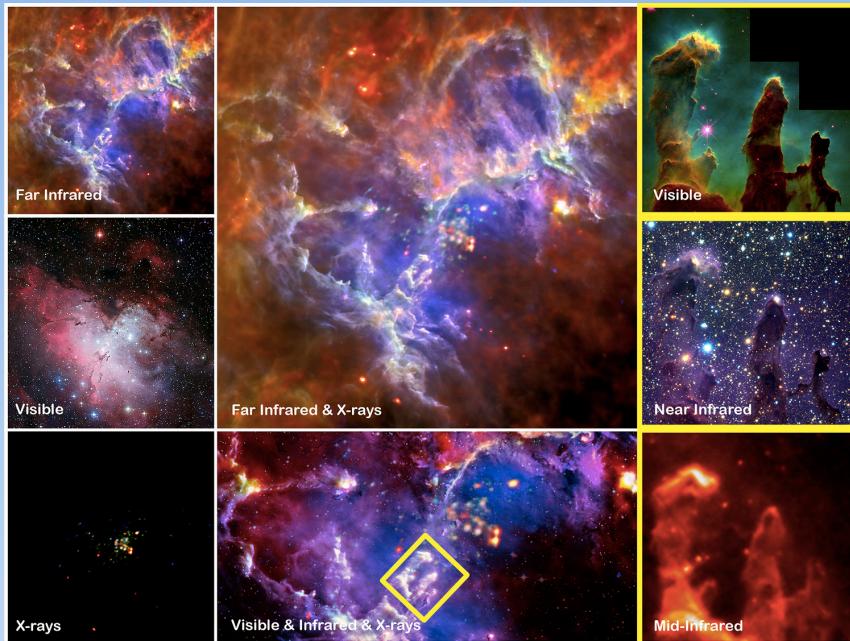


# *Star formation runaway!*

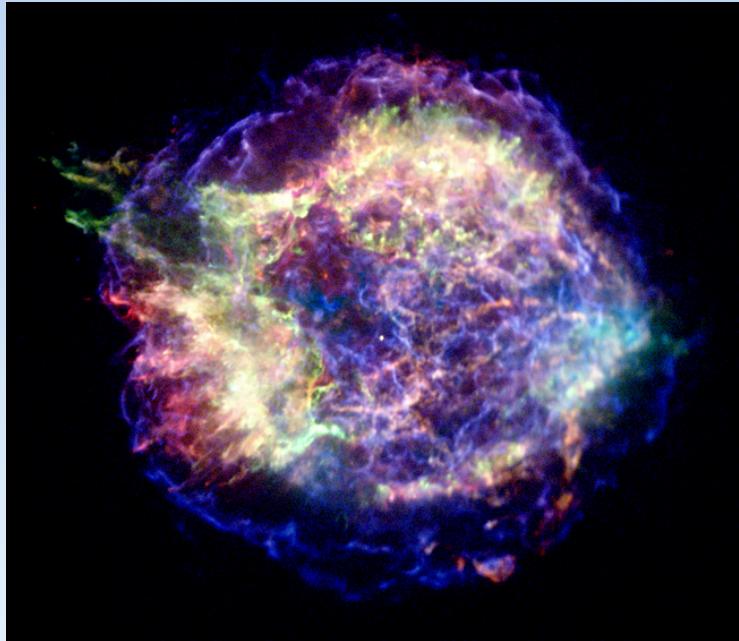


# The need for feedback

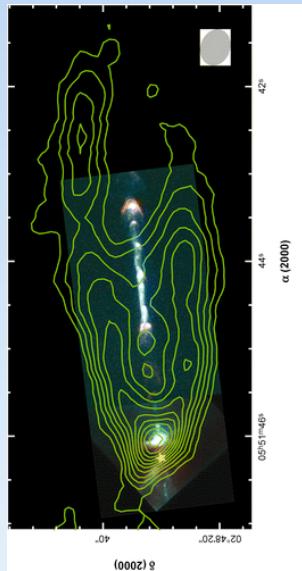
- Without **feedback**, all the mass in a cloud would end up in stars
- Can be halted/turned around by:
  - Protostellar outflows
  - HII regions (photoionization, winds)
  - Radiation pressure
  - Supernova blasts



Eagle nebula/M16 cluster



Cas A supernova remnant



HH 111 jet and outflow



Herschel: Carina nebula

# Why feedback?

*By allowing a small part of the gas to collapse...*

- new stars are born
- high mass stars energize their surroundings

*...collapse of the majority of gas is prevented*

*Enables star formation to be self-regulated by feedback:*

- *In individual star-forming clouds*
- *On scale of local galactic disk  $\sim H^3$*
- *On scale of whole galaxy/halo*

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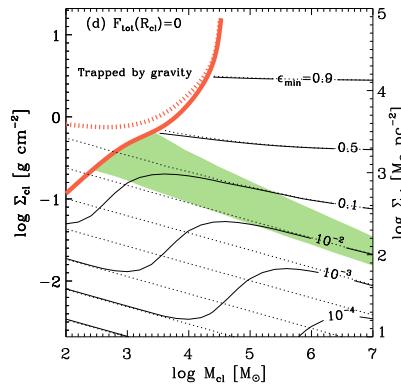
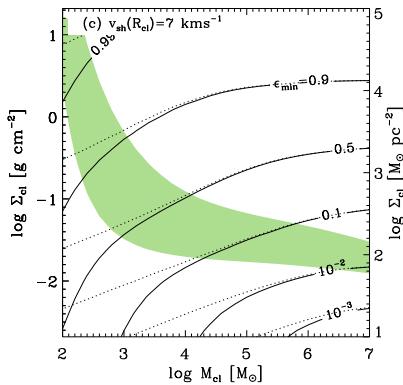
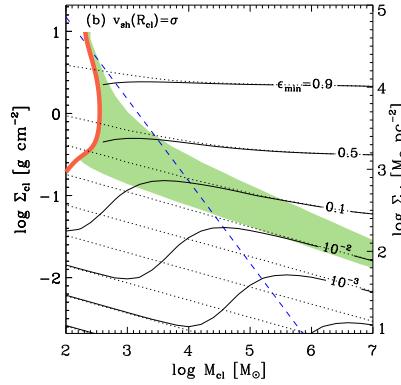
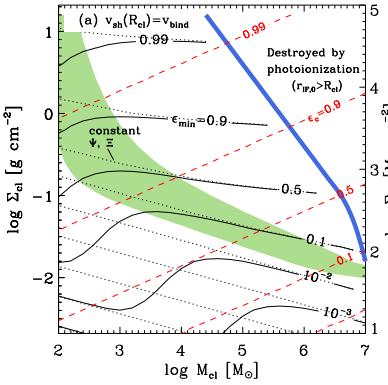
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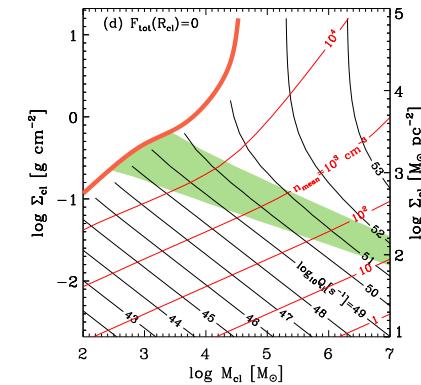
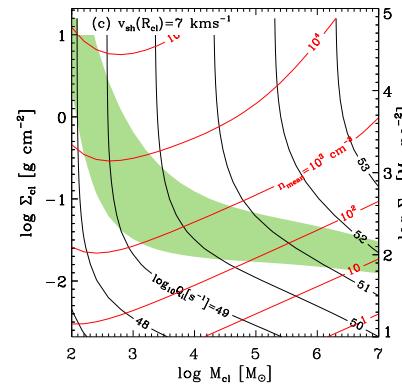
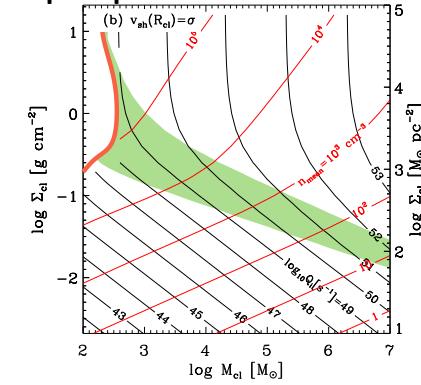
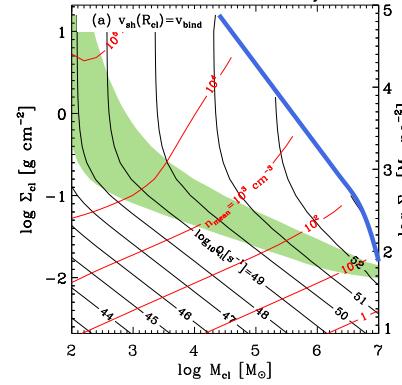
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# Spherical cloud: ionizing + non-ionizing radiation

Minimum SFE



Cloud, cluster properties



# Effects of non-ionizing radiation

- Photon momentum = photon energy/c
- Maximum force from direct radiation (UV) of star or cluster with luminosity  $L$  is  $L/c$
- UV radiation is absorbed by dust and re-emitted as infrared (IR)
- Reprocessed photons give multiple “kicks” to gas if the cloud IR optical depth  $\tau=\kappa\rho R$  is large
- We follow gas + radiation interaction using *radiation hydrodynamics* (RHD) computational models
  - Follow evolution of turbulent cloud with gravity
  - Collapsing gas is replaced by “star particles” (representing clusters) with luminosity  $L_*=\Psi M_*$

# RHD with RSL

- Basic equations (Skinner & Ostriker 2013, 2015; Raskutti et al 2016)

ID: radiative equilibrium

UV: absorption only

$$\partial_t \rho + \nabla \cdot (\rho \mathbf{v}) = 0, \quad (1)$$

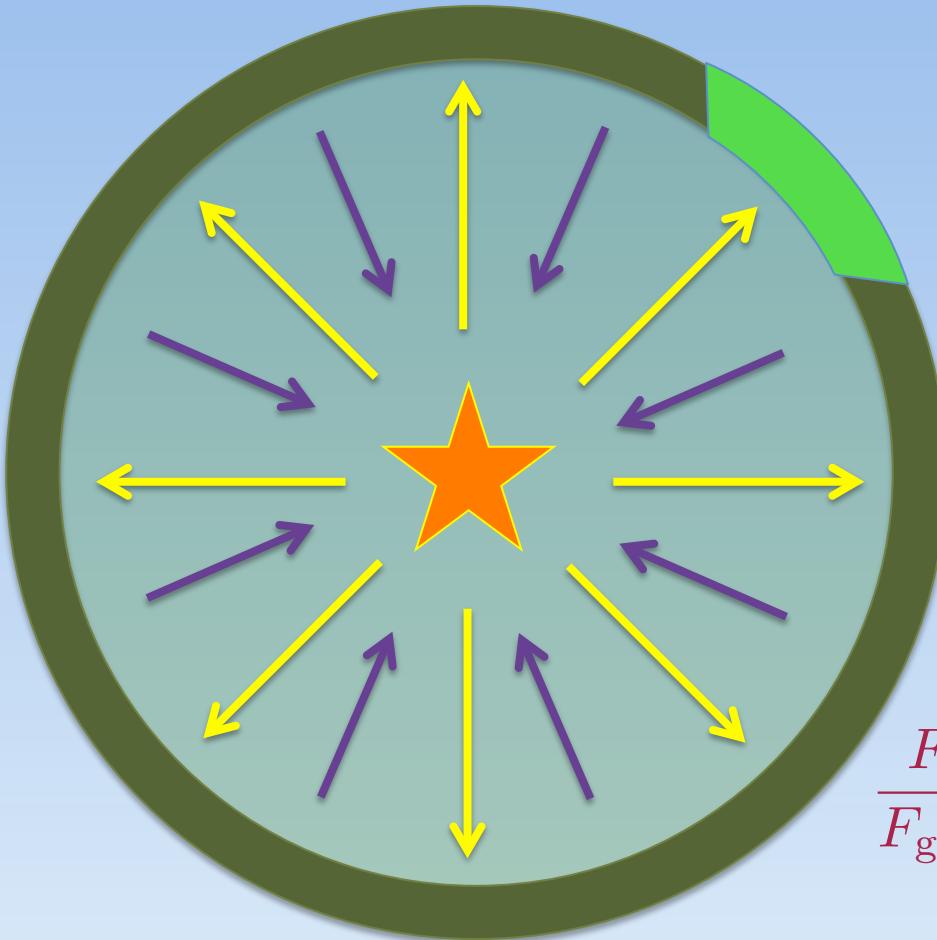
$$\partial_t (\rho \mathbf{v}) + \nabla \cdot (\rho \mathbf{v} \mathbf{v} + P \mathbb{I}) = -\rho \nabla \Phi + \rho \kappa \frac{\mathbf{F}}{c}, \quad (2)$$

$$\frac{1}{\hat{c}} \partial_t \mathcal{E} + \nabla \cdot \left( \frac{\mathbf{F}}{c} \right) = -\rho \kappa \mathcal{E} + \mathbb{S}, \quad (3)$$

$$\frac{1}{\hat{c}} \partial_t \left( \frac{\mathbf{F}}{c} \right) + \nabla \cdot \mathbb{P} = -\rho \kappa \frac{\mathbf{F}}{c}, \quad (4)$$

- RSL signal speed  $\hat{c} \gg v_{\max} \times \tau$  (diffusion) or 1 (absorption only)
- Finite volume scheme with HLL-type solvers, piecewise linear
- Operator-split radiation (substepped) from gas
- Adopt M1 closure (Levermore & Pomraning 1981) for radiation pressure tensor in terms of  $\mathcal{E}$  and  $\mathbf{F}$
- Sink particles are also radiation sources with luminosity  $L_* = \Psi M_*$

# Effect of UV radiation feedback



$$\tau_{\text{shell}} = \kappa M_{\text{shell}} / (4\pi R^2)$$

$$\mathcal{L}_* = \Psi M_* \quad \Psi \sim 1000 \text{ L}_\odot / M_\odot$$

$$\begin{aligned} F_{\text{rad}} &= \mathcal{L}_* (1 - \exp(-\tau_{\text{shell}})) / c \\ &= \Psi M_* (1 - \exp(-\tau_{\text{shell}})) / c \end{aligned}$$

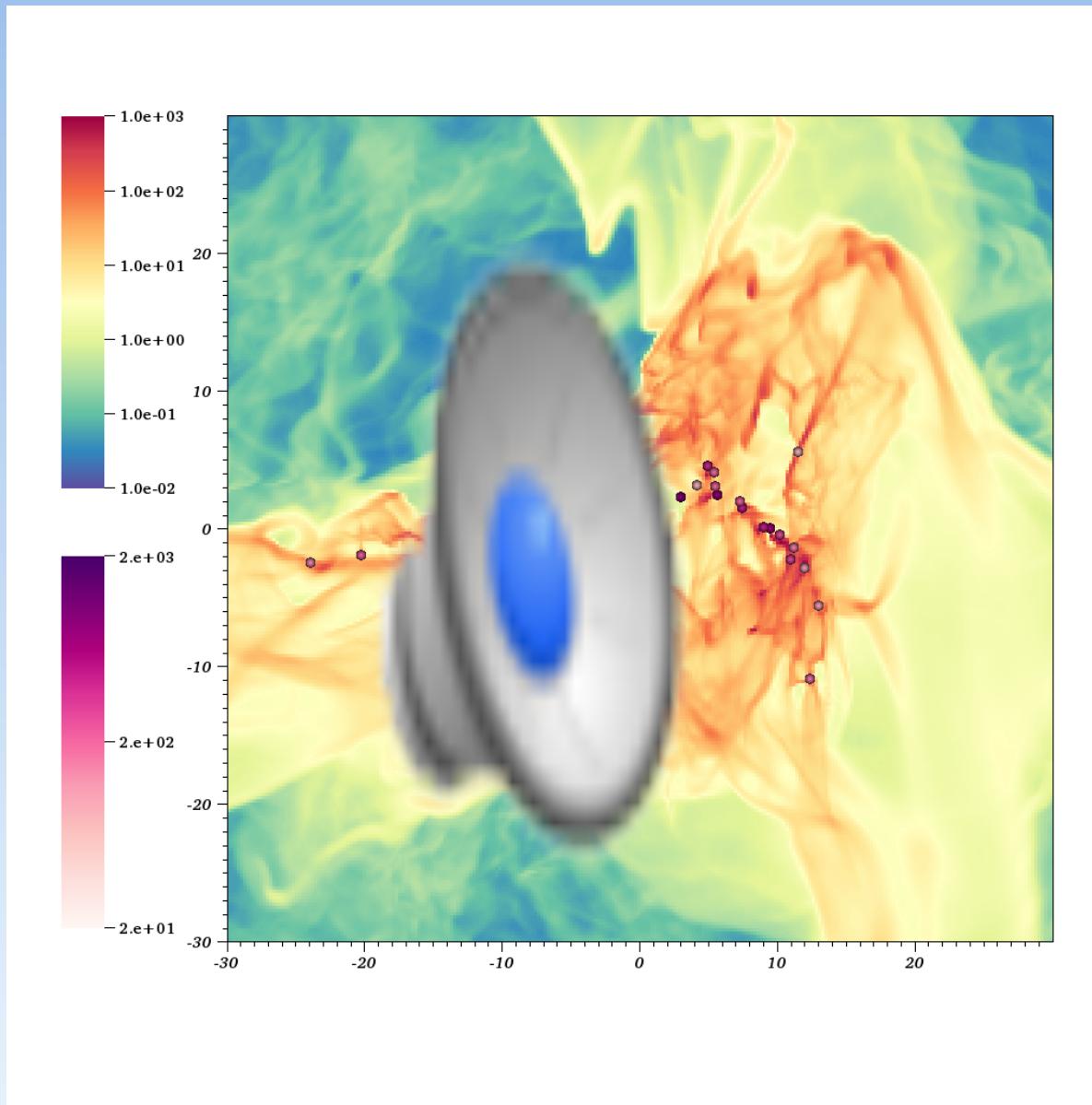
$$\begin{aligned} F_{\text{grav},*} &= G M_* M_{\text{shell}} / r^2 \\ &= G M_* \Sigma_{\text{shell}} / 4\pi \end{aligned}$$

$$\begin{aligned} \frac{F_{\text{rad}}}{F_{\text{grav},*}} &= \frac{\Psi / (4\pi c G)}{\Sigma_{\text{shell}}} [1 - \exp(-\tau_{\text{shell}})] \\ &= \frac{380 M_\odot \text{pc}^{-2}}{\Sigma_{\text{shell}}} [1 - \exp(-\tau_{\text{shell}})] \end{aligned}$$

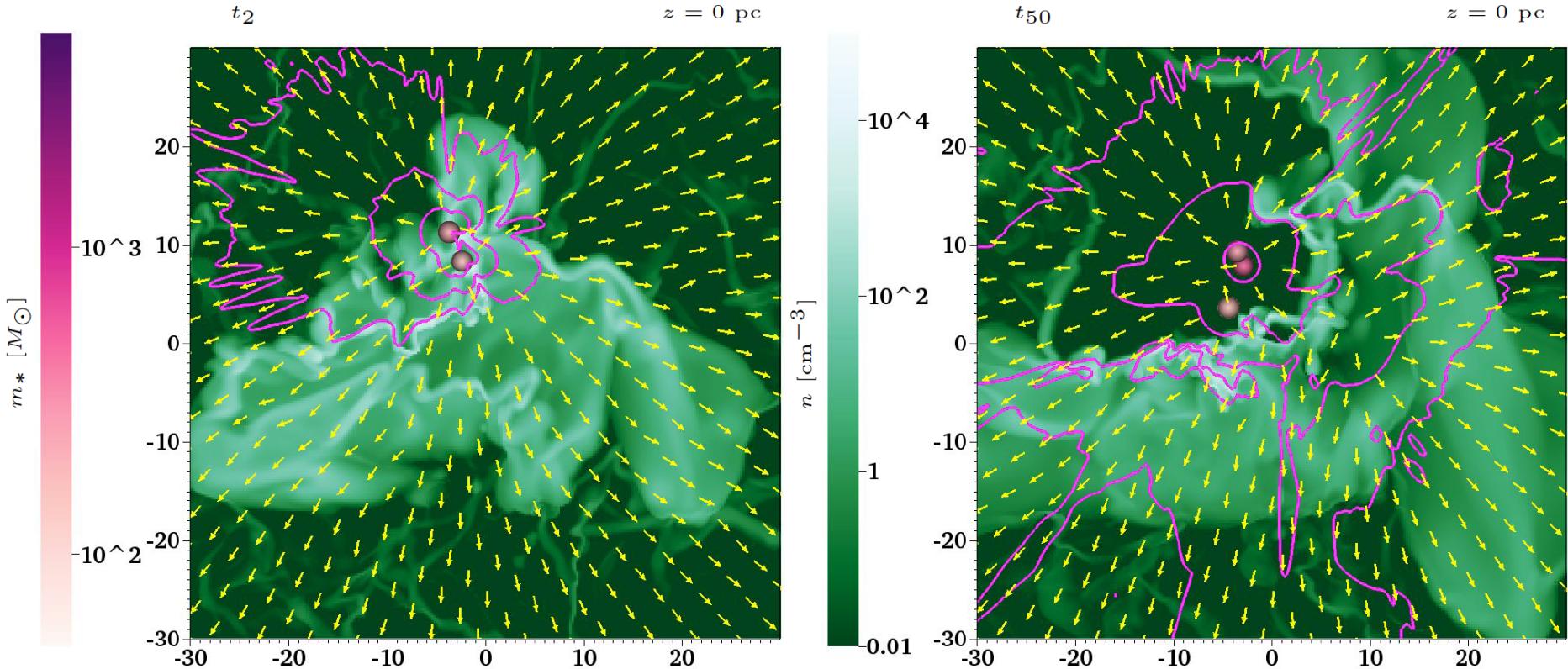
- Maximum  $f_{\text{Edd},*} = \Psi \kappa_{\text{UV}} / (4\pi c G) = 80$  for  $\tau_{\text{shell}} \lesssim 1$ ,  $\Sigma_{\text{shell}} \lesssim 5 \text{ M}_\odot / \text{pc}^2$
- $f_{\text{Edd},*} < 1$  for  $\Sigma_{\text{shell}} > 380 \text{ M}_\odot / \text{pc}^2$

# Cloud evolution with direct (UV) radiation

Raskutti, Ostriker, & Skinner (2016)



$5 \times 10^4 M_{\odot}$   
 $r=15\text{pc}$  initial  
cloud with  
sink particles  
to represent  
cluster, and  
RHD for non-  
ionizing UV  
radiation



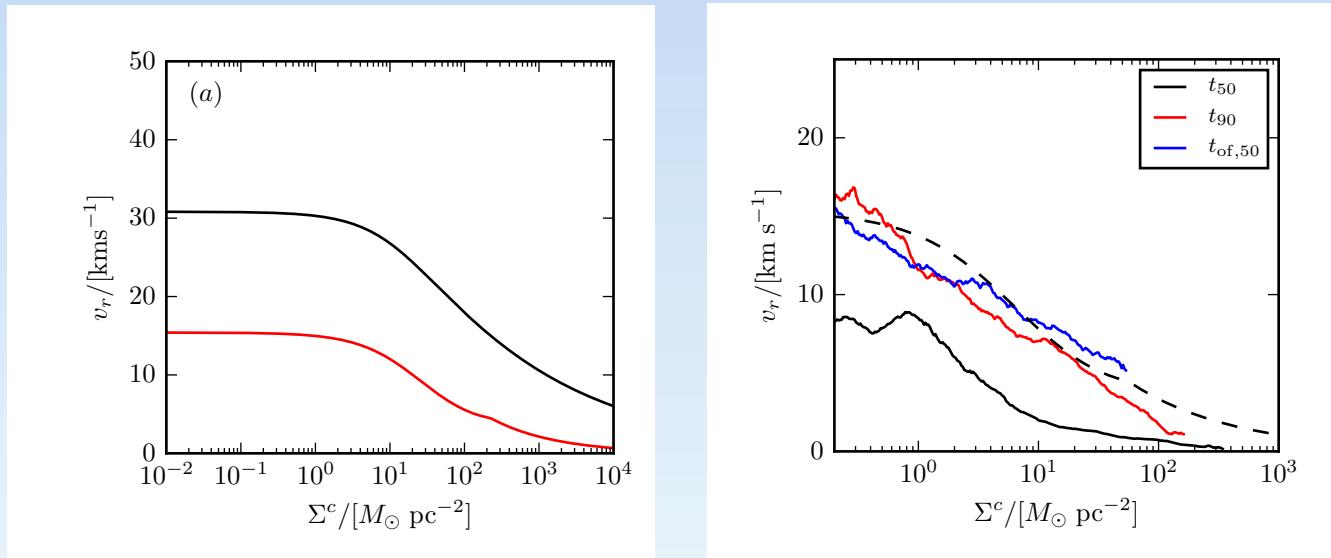
# UV radiation driven outflows

- At  $r \gg r_0$ , shell with initial surface density  $\Sigma_0 < \Sigma_E$  reaches:

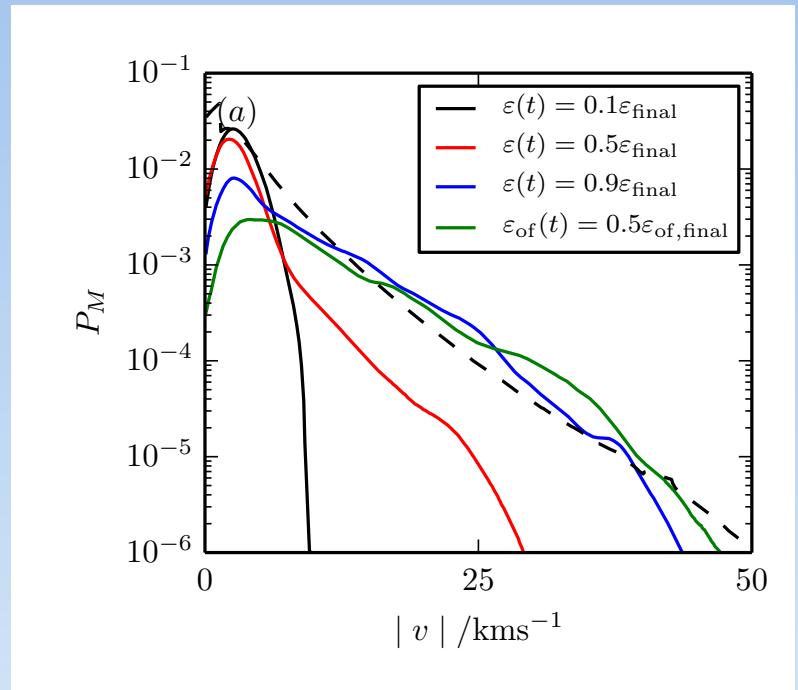
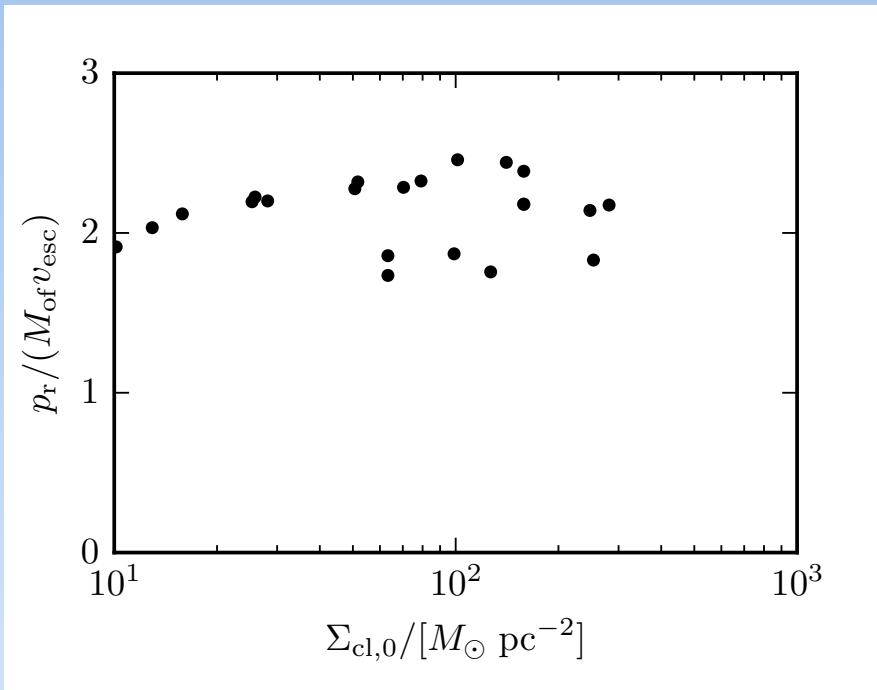
$$v^2 \rightarrow \frac{2GM_*}{r_0} \frac{\Psi/(4\pi cG)}{\Sigma_0} [\sqrt{\pi\tau_0} \operatorname{erf}(\sqrt{\tau_0}) + \exp(-\tau_0) - 1]$$

- Optically thin (UV):  $v^2 \rightarrow \frac{2GM_*}{r_0} \frac{\Psi\kappa}{4\pi cG} \approx 80v_{\text{esc}}^2(r_0)$

- Optically thick (UV):  $v^2 \rightarrow \frac{2GM_*}{r_0} \frac{\Psi\kappa}{4\pi cG} \left(\frac{\pi}{\tau_0}\right)^{1/2} = v_{\text{thin}}^2 \left(\frac{\pi}{\tau_0}\right)^{1/2}$

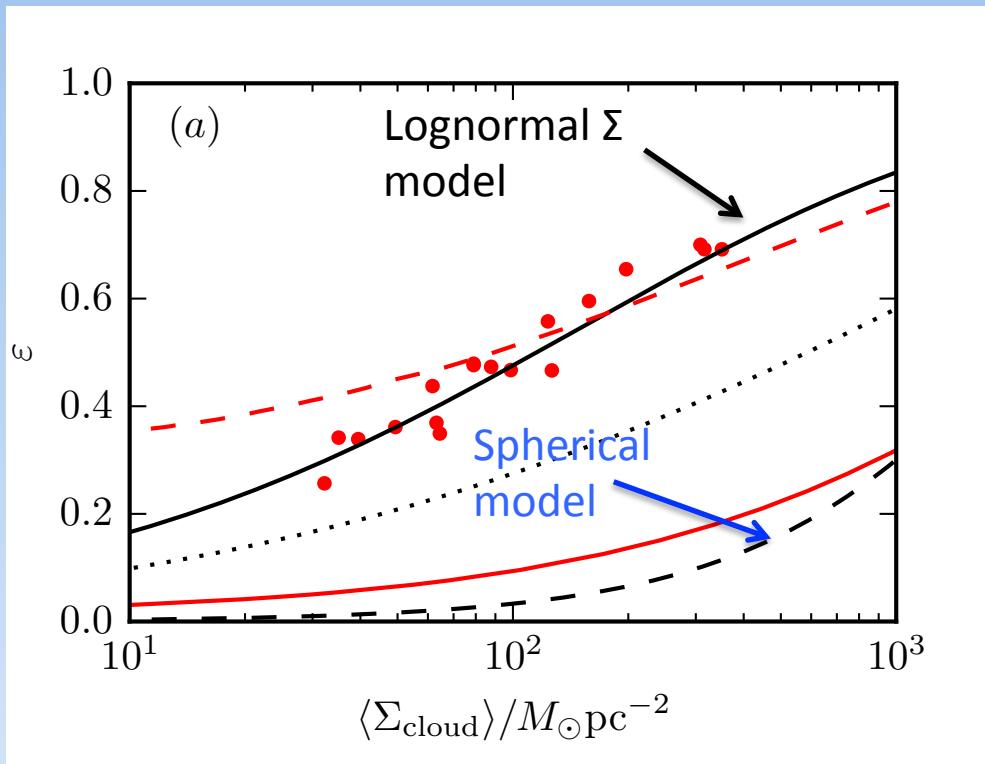


# $M(v)$ distribution



- Mean velocity of outflowing gas is  $\sim 2 v_{\text{esc}}(r_{\text{cloud}})$
- But: extends to  $\sim 15 v_{\text{esc}}(r_{\text{cloud}})$  due to range of  $r_0$
- Consistent with convolution of  $v(r_0, \Sigma)$  with  $f_m(\Sigma)$  for  $r_0 < r_{\text{cloud}}$

# Lifetime star formation efficiency of GMC

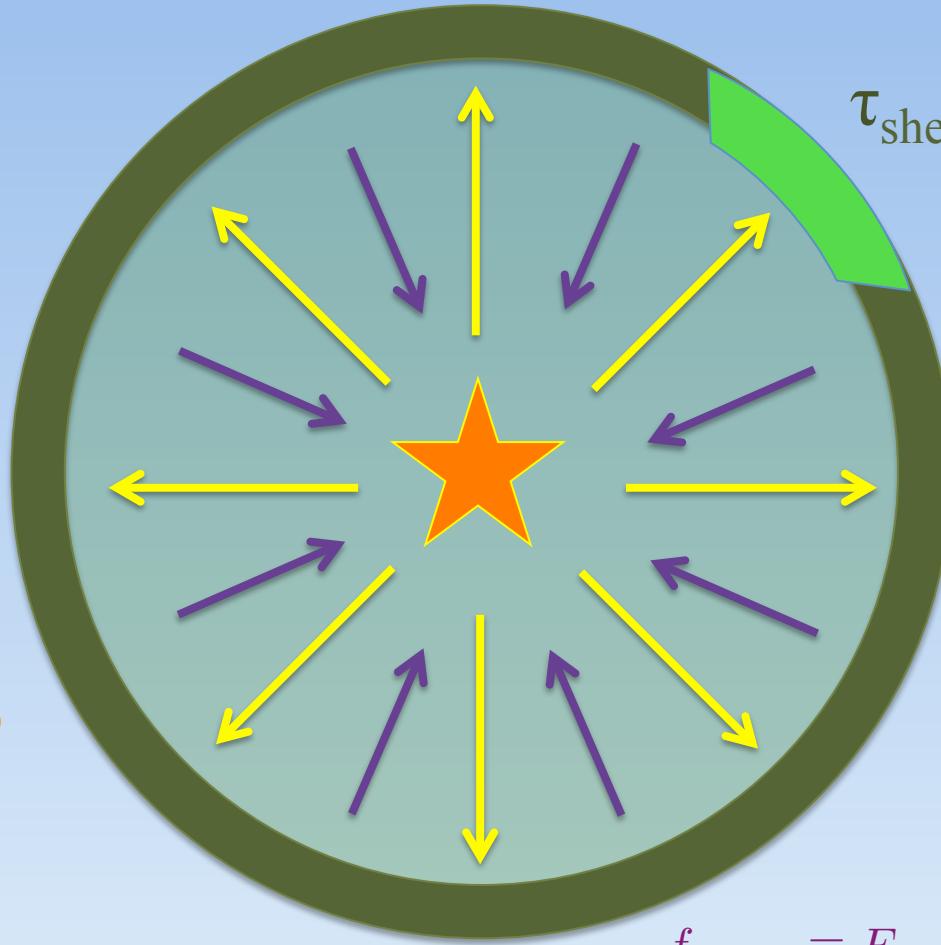


Raskutti, Ostriker, & Skinner (2016)

$$\Sigma_E = \frac{2\varepsilon}{\varepsilon + 1} \frac{\Psi}{4\pi c G} = 380 M_{\odot} \text{pc}^{-2} \frac{2\varepsilon}{\varepsilon + 1} \frac{\Psi}{2000 \text{erg s}^{-1} \text{g}^{-1}}$$

- Radiation force/area  $\sim L/(c4\pi r^2) \propto M_*/r^2$  must exceed gravity force/area  $\sim G(M_* + M_{\text{gas}}/2)\Sigma/r^2$  to expel structure:  
require  $\Sigma < \Sigma_E$
- *Non-spherical, turbulent:*
  - Lognormal  $\Sigma$  distribution
  - Gas structures of increasingly high  $\Sigma$  are driven out as  $\varepsilon$  and  $L_*$  of cluster increases.
- Final SFE much higher than for simple spherical model (uniform  $\Sigma$ ) because turbulence increases  $\langle \Sigma \rangle_M$

# Effect of IR radiation feedback



$$\mathcal{L}_* = \Psi M_*$$

$$\Psi \sim 1000 L_\odot / M_\odot$$

$$F_{\text{rad}} = \mathcal{L}_* \tau_{\text{shell}} / c = \Psi M_* \kappa_{\text{IR}} \Sigma_{\text{shell}} / c$$

$$F_{\text{grav},*} = GM_* M_{\text{shell}} / R^2 = GM_* \Sigma_{\text{shell}} 4\pi$$

$$\begin{aligned}\tau_{\text{shell}} &= \kappa M_{\text{shell}} / (4\pi R^2) \\ &= \kappa \Sigma_{\text{shell}}\end{aligned}$$

$$f_{Edd,*} \equiv F_{\text{rad}} / F_{\text{grav}} = \frac{\Psi \kappa_{\text{IR}}}{4\pi G c}$$

$\rightarrow 0.7$  for  $\kappa = 10$  (*bound*)

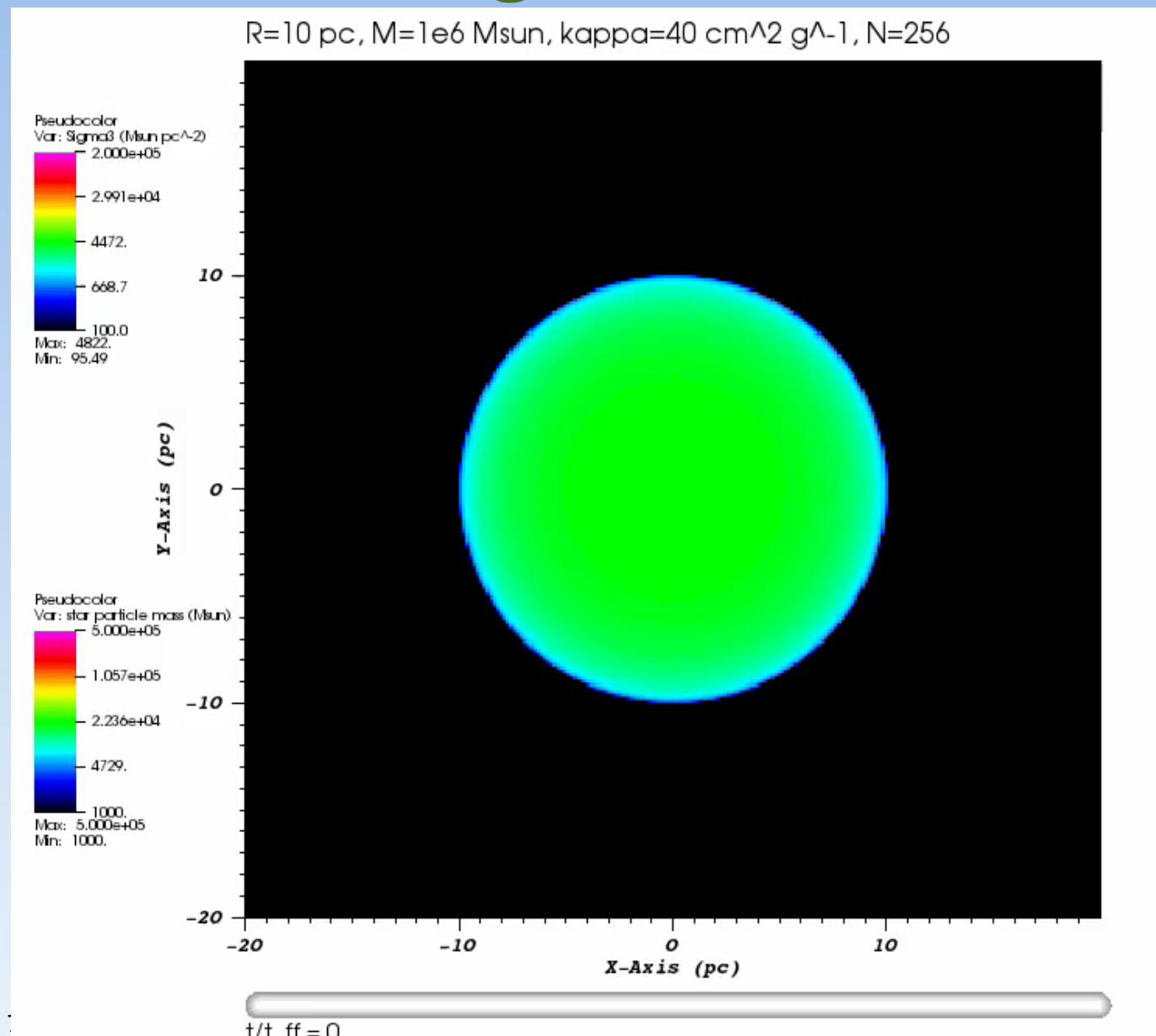
$\rightarrow 1$  for  $\kappa = 15$  (*Critical*)

$\rightarrow 1.4$  for  $\kappa = 20$  (*unbound*)

$\rightarrow 2.4$  for  $\kappa = 40$  (*unbound*)

# Star-forming cloud with IR RHD

Skinner & Ostriker (2015)



$10^6 M_{\odot}$  initial  
cloud with  
sink particles  
and RHD

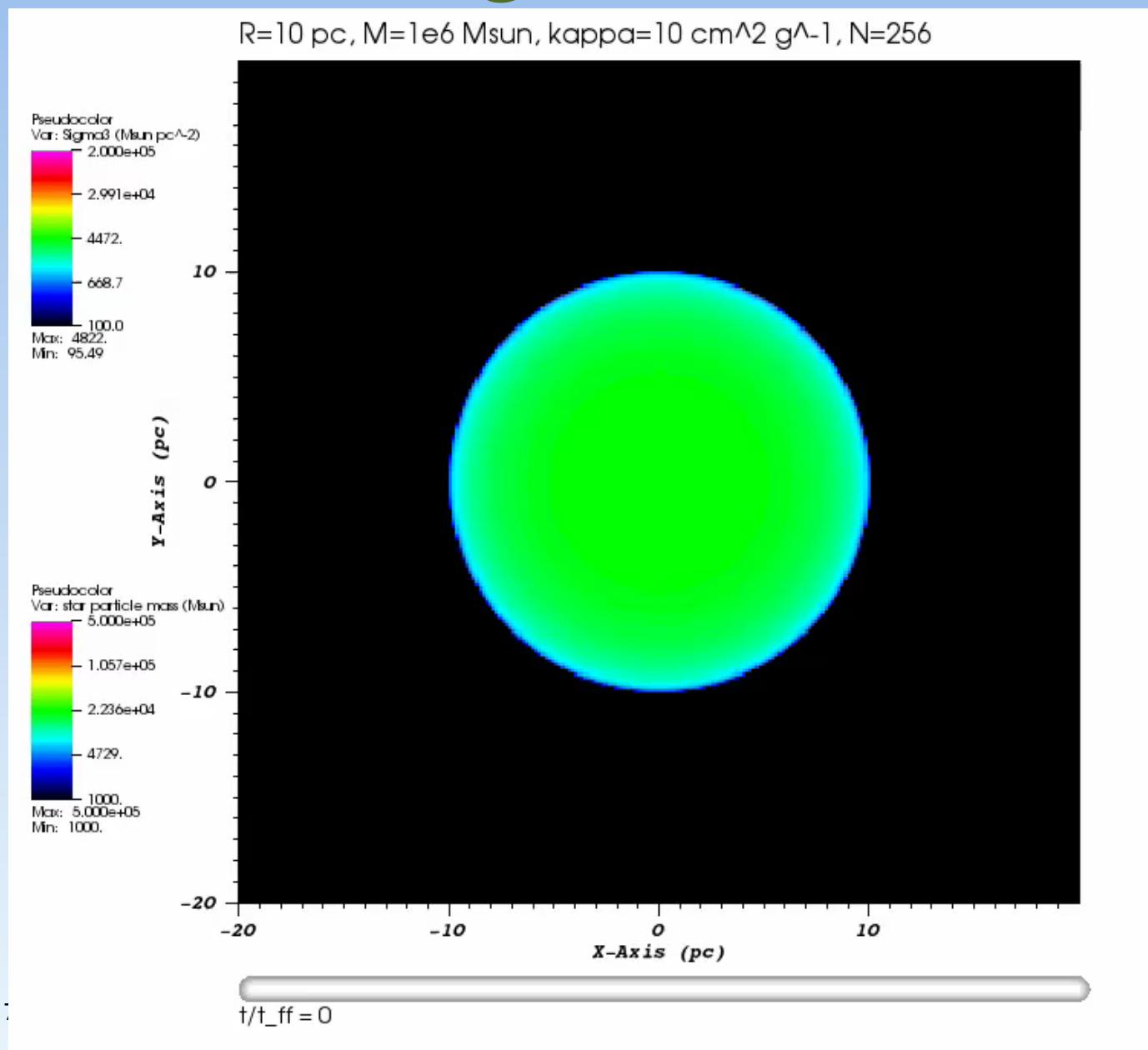
$\kappa=40 \text{ cm}^2/\text{g}$

$L_* = \Psi M_*$  for  
subclusters;  
 $\Psi=1700 \text{ erg/s/g}$

$t_{\text{ff}}=0.52 \text{ Myr}$

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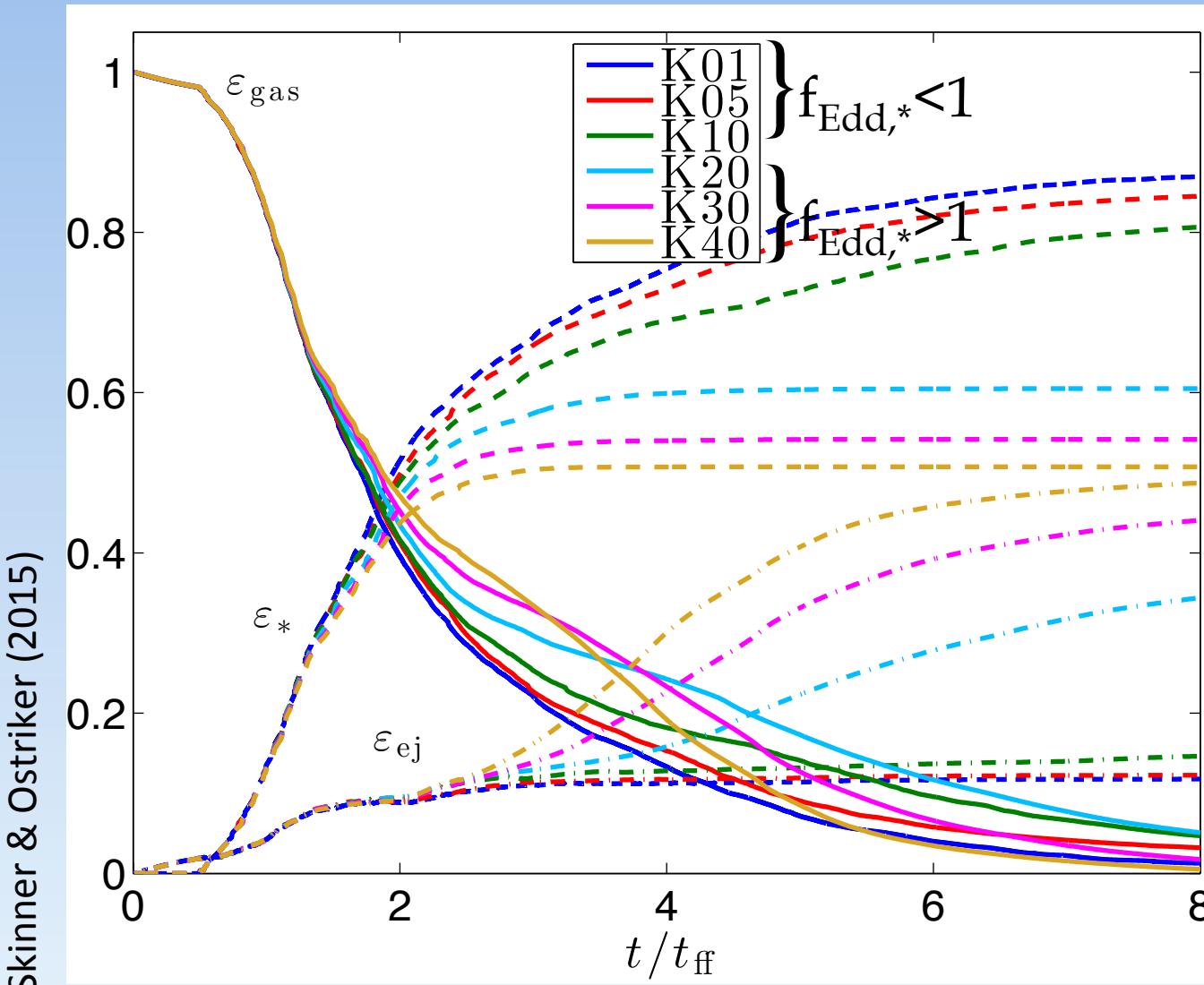
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# SF efficiency for varying IR opacity



$$f_{\text{Edd},*} = F_{\text{rad},*}/F_{\text{grav},*} \\ = \Psi \kappa / (4\pi G c)$$

$$\kappa_{\text{IR}} = 1, 5, 10, 20, 30, 40 \text{ g/cm}^2$$

*Fractional mass loss and net SF efficiency depends strongly on IR opacity*

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# Feedback by SNe

- Supernovae drive blast waves into surrounding interstellar medium
- Blast shocks and sweeps up ambient medium
  - Initially adiabatic
  - Shell cools and expansion slows when shock drops to  $\sim 200$  km/s
- Classical evolution stages :
  - Free expansion, Sedov-Taylor, Pressure-Driven Snowplow, Momentum-Conserving Snowplow  
*Spherical simulations: Cioffi et al 1988, Blondin et al 1998, Thornton et al 1998*
- Key feedback parameter is the net (spherical) momentum injection  $p_*$  to surroundings

# Supernova remnant momentum

- Uniform medium: “congruent” evolution depending on  $t/t_{sf}$
- Momentum increases  $\sim 50\%$  after shell formation
- Maximum hot gas mass  $\sim 1000M_\odot$
- **Real ISM: inhomogenous medium**

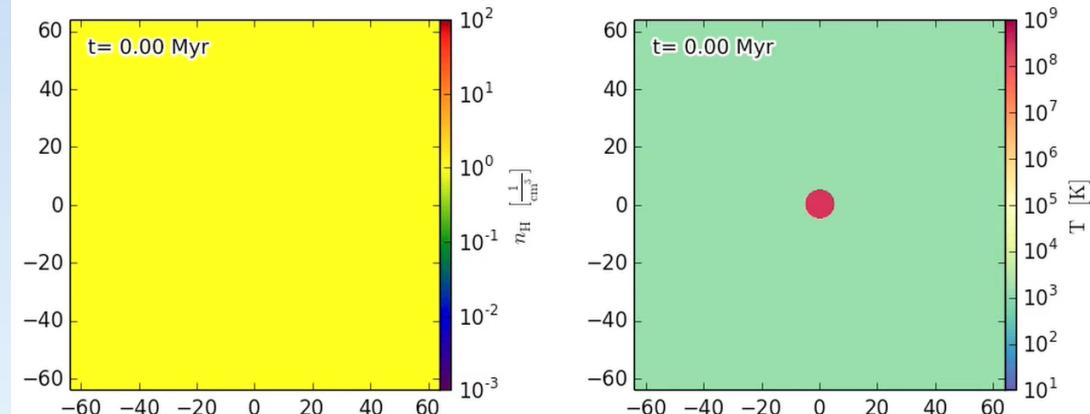
$$t_{sf} = 40 \text{ kyr } n_0^{-0.6}$$

$$r_{sf} = 22 \text{ pc } n_0^{-0.4}$$

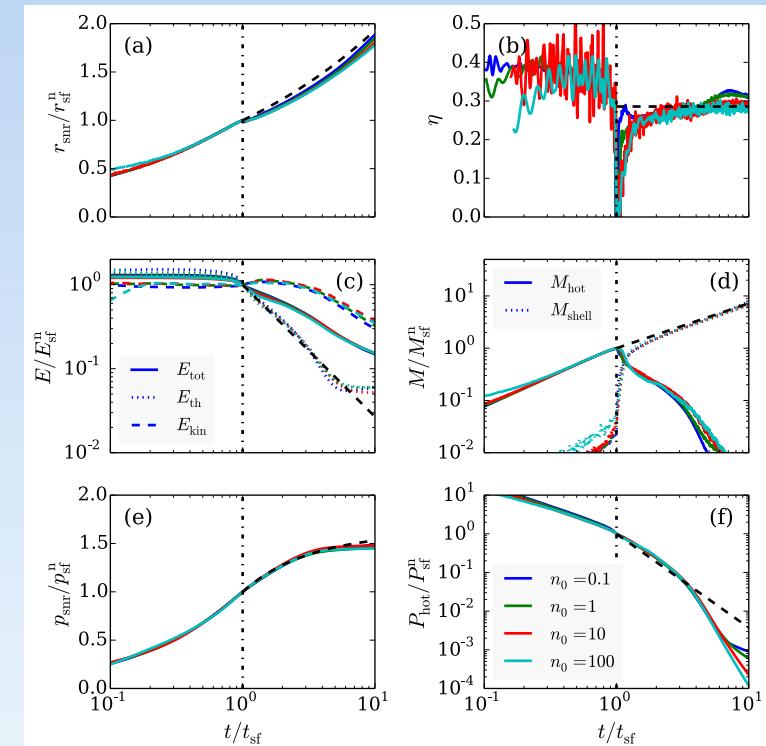
$$v_{sf} = 210 \text{ km/s } n_0^{0.1}$$

$$M_{sf} = 1550 M_\odot n_0^{-0.3}$$

$$p_{sf} = 2 \times 10^5 M_\odot \text{ km/s } n_0^{-0.15}$$



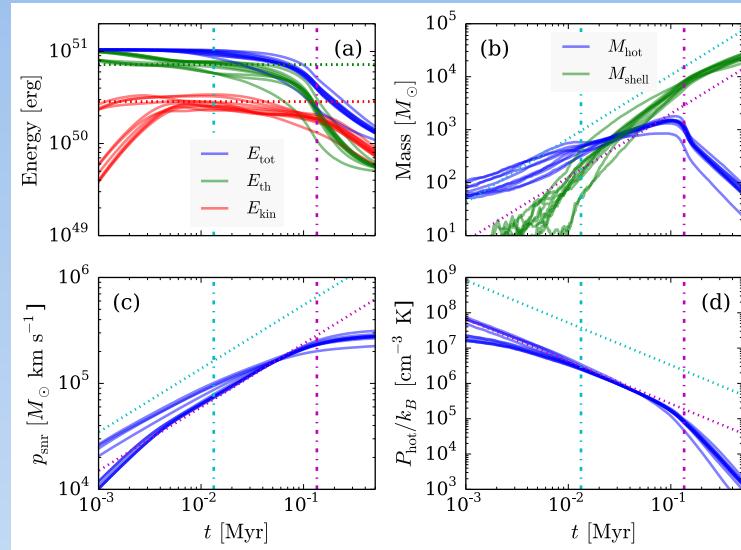
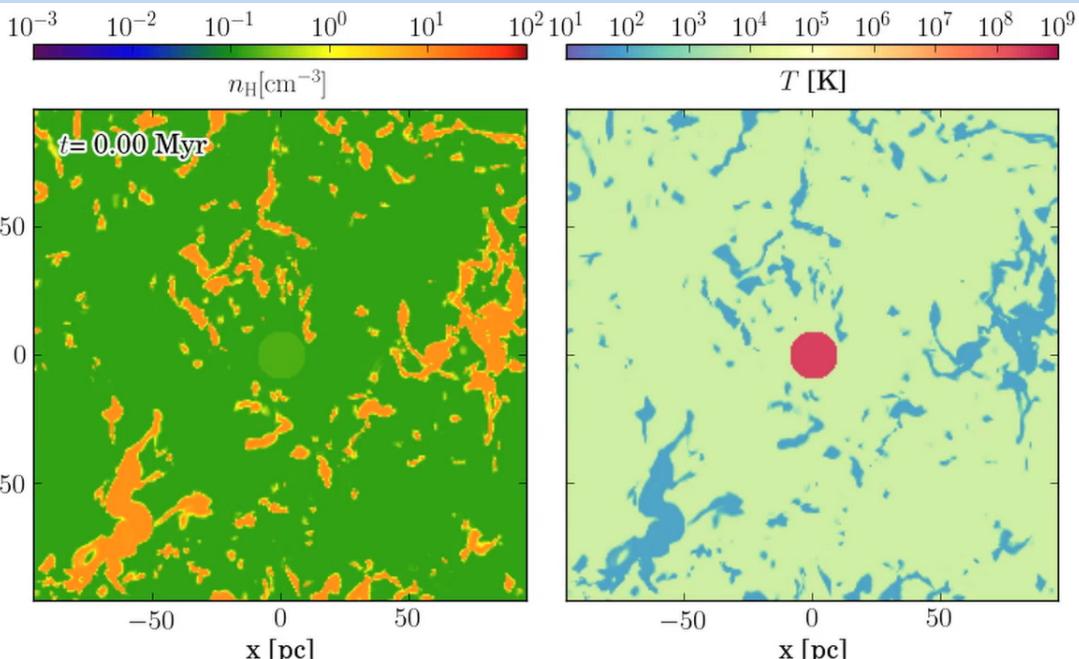
Kim & Ostriker (2015a)



# Cloudy ambient medium: SNR

- Cloudy-ISM models with mean density  $\langle n_0 \rangle$  from 0.1 to 100 cm<sup>-3</sup>
- Intercloud density sets maximum radius before onset of strong cooling
- Final SNR momentum is  $\sim 10 \times$  initial momenta of SN ejecta

*Kim & Ostriker (2015), Iffrig & Hennebelle (2015), Martizzi et al (2015), Walch & Naab (2015)*

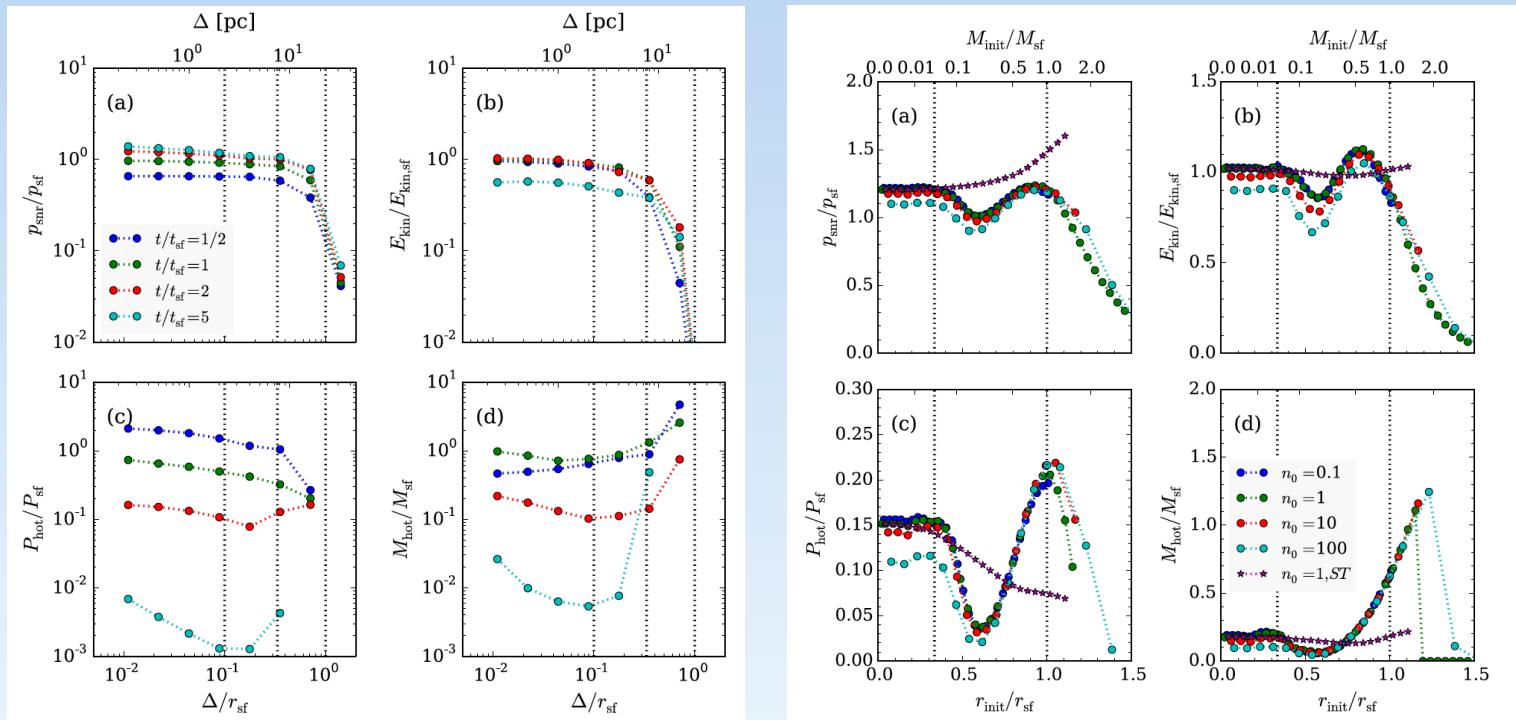


$$p_{\text{final}} = 2.8 \times 10^5 M_\odot \text{ km/s} \langle n_0 \rangle^{-0.17}$$

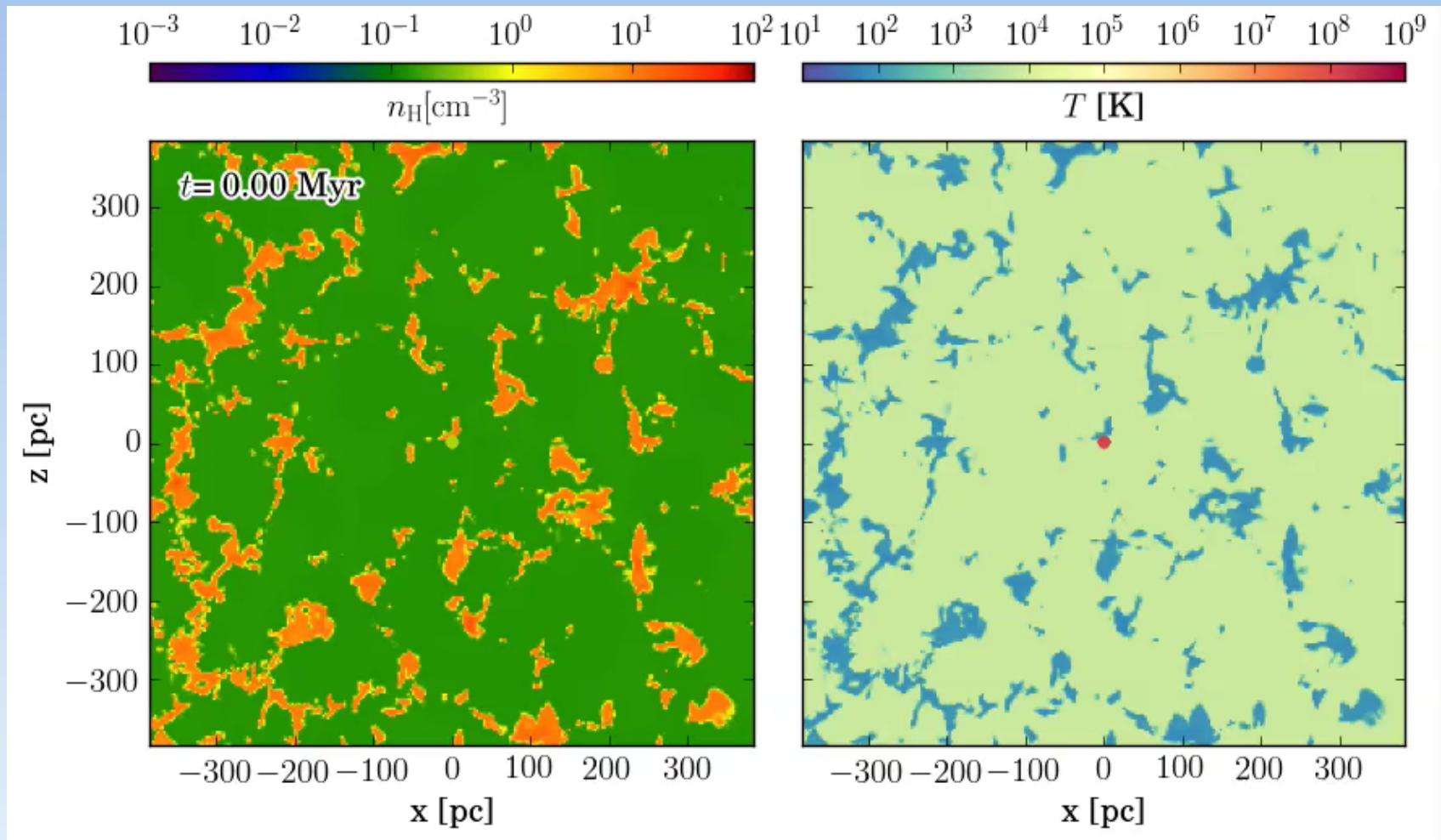
*Comparable momentum to single-phase prediction using average ambient density*

# Numerical resolution requirements

- To resolve the ST stage and obtain the correct mass of hot gas and total momentum injected, must have:  
 $r_{\text{init}}/r_{\text{sf}} < 1/3$  and  $\Delta/r_{\text{sf}} < 1/10$
- “Overcooling” problem of SN feedback in many galaxy formation simulations is due to insufficient numerical resolution

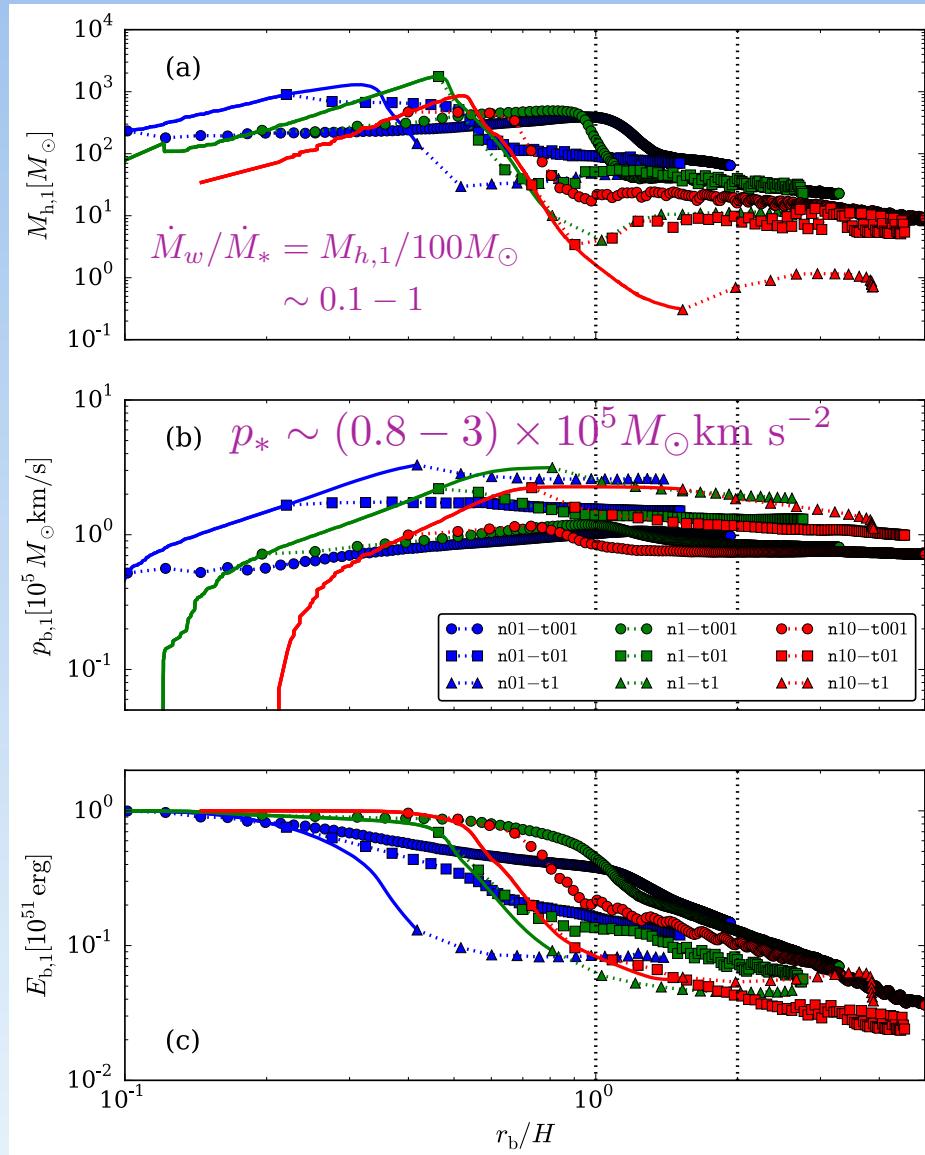


# Superbubbles in two-phase ISM



# SB & galactic wind loading

- For high enough  $\Sigma_{\text{SFR}}$ , superbubble breaks out before shell formation:  
 $(\text{SB mass})/(\text{star cluster mass}) \sim 10$
- Lower  $\Sigma_{\text{SFR}}$  :  
 $(\text{hot gas mass})/(\text{cluster mass}) \sim 0.1 - 1$ 
  - Wind mass loading is higher at lower density and for shorter  $\Delta t_{\text{SN}}$



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# Self-regulation concept

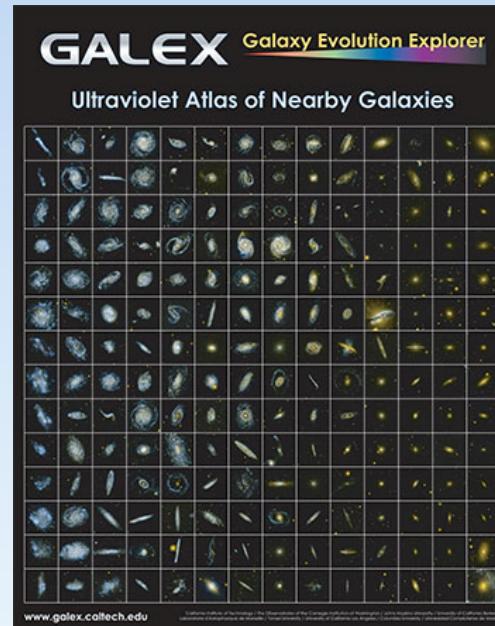
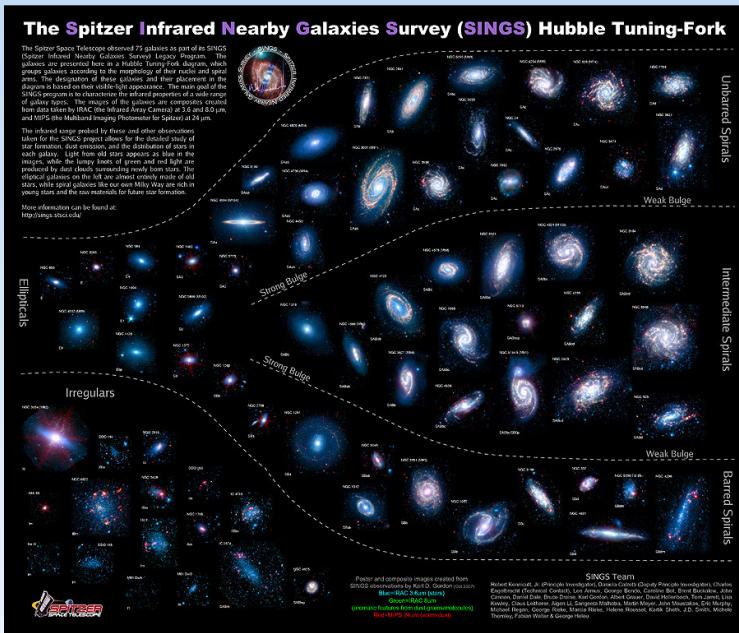
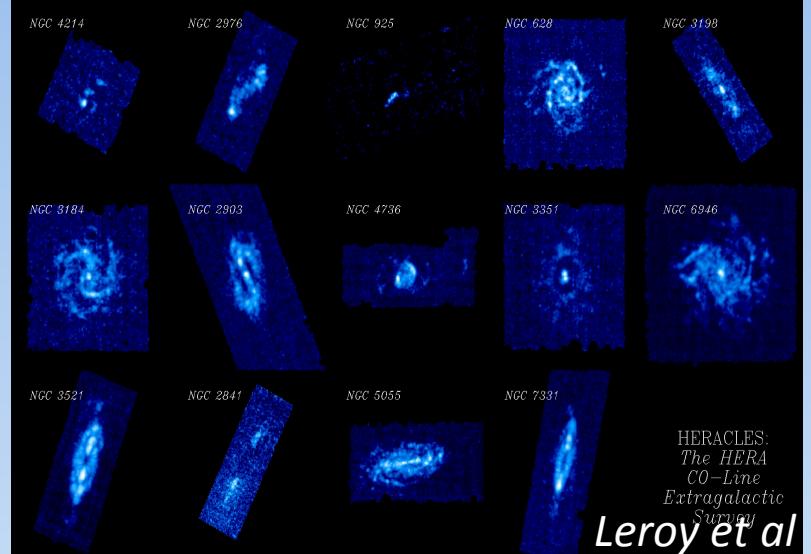
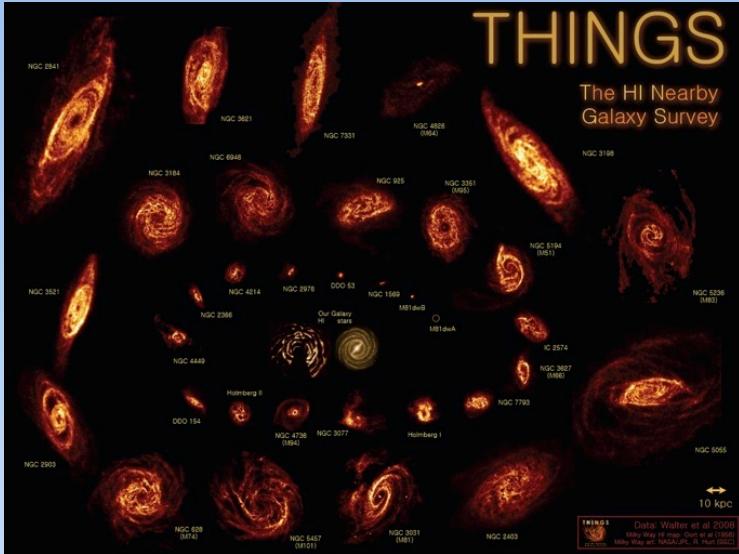
*By allowing a small part of the gas to collapse...*

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*Star formation rates and efficiencies can be predicted from energy and momentum requirements to maintain ISM equilibrium on scales  $\sim H^3$  in galactic disk*

# Large-scale gas and SFR



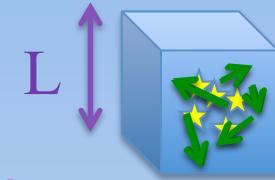
*kpc-scale surveys*

# ISM energetics and feedback

- Timescales for cooling and turbulent dissipation in the diffuse ISM are **short**
- To maintain equilibrium, radiated energy must be replenished
- Energy input is from high-mass stars
- Midplane pressure  $\propto$  energy density must support weight of diffuse ISM
  - weight depends on gravity of gas, stars, dark matter
- *ISM equilibrium demands a certain level of feedback*

# Quantifying self-regulation

Gas mass  $M$ , size  $L^3$ , turbulence  $v$ , SFR  $\dot{M}_*$



- Assume SF feedback momentum/mass is  $p_*/m_*$
- Momentum input rate is

$$\dot{p}_{driv} = \frac{p_*}{m_*} \dot{M}_*$$

- Momentum dissipation rate is

$$\dot{p}_{diss} \sim \frac{v M}{t_{dyn}} \sim \frac{v^2 M}{L}$$

- Balancing,

$$\dot{M}_* \sim \frac{v^2 M}{L p_*/m_*}$$

- For system in dynamical equilibrium

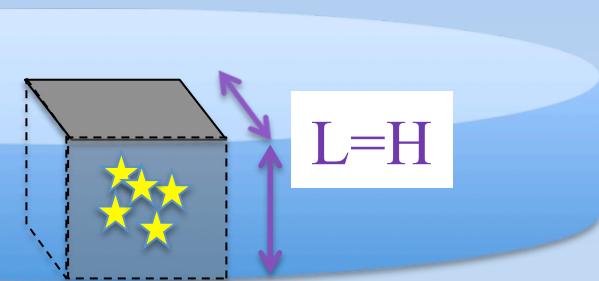


$$\dot{M}_* \sim \frac{G M_{tot} M}{L^2 p_*/m_*}$$

$v^2 \sim GM_{tot}/L$   
 $(\text{Kin. E} \sim \text{Gray. E})$   
*Self-regulated star formation*

# Gas-dominated starburst disk

$$\dot{M}_* \sim \frac{GM_{tot}M}{L^2 p_*/m_*} \longrightarrow \frac{\dot{M}_*}{L^2} \sim \frac{GM^2}{L^4(p_*/m_*)}$$

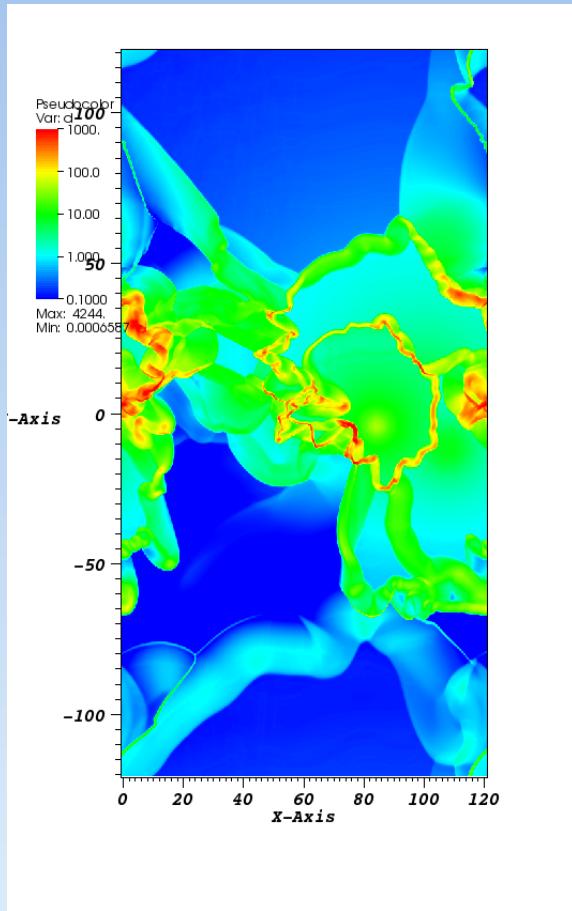


$$\begin{aligned}\dot{M}_*/H^2 &\rightarrow \Sigma_{SFR} \\ M/H^2 &\rightarrow \Sigma\end{aligned}$$

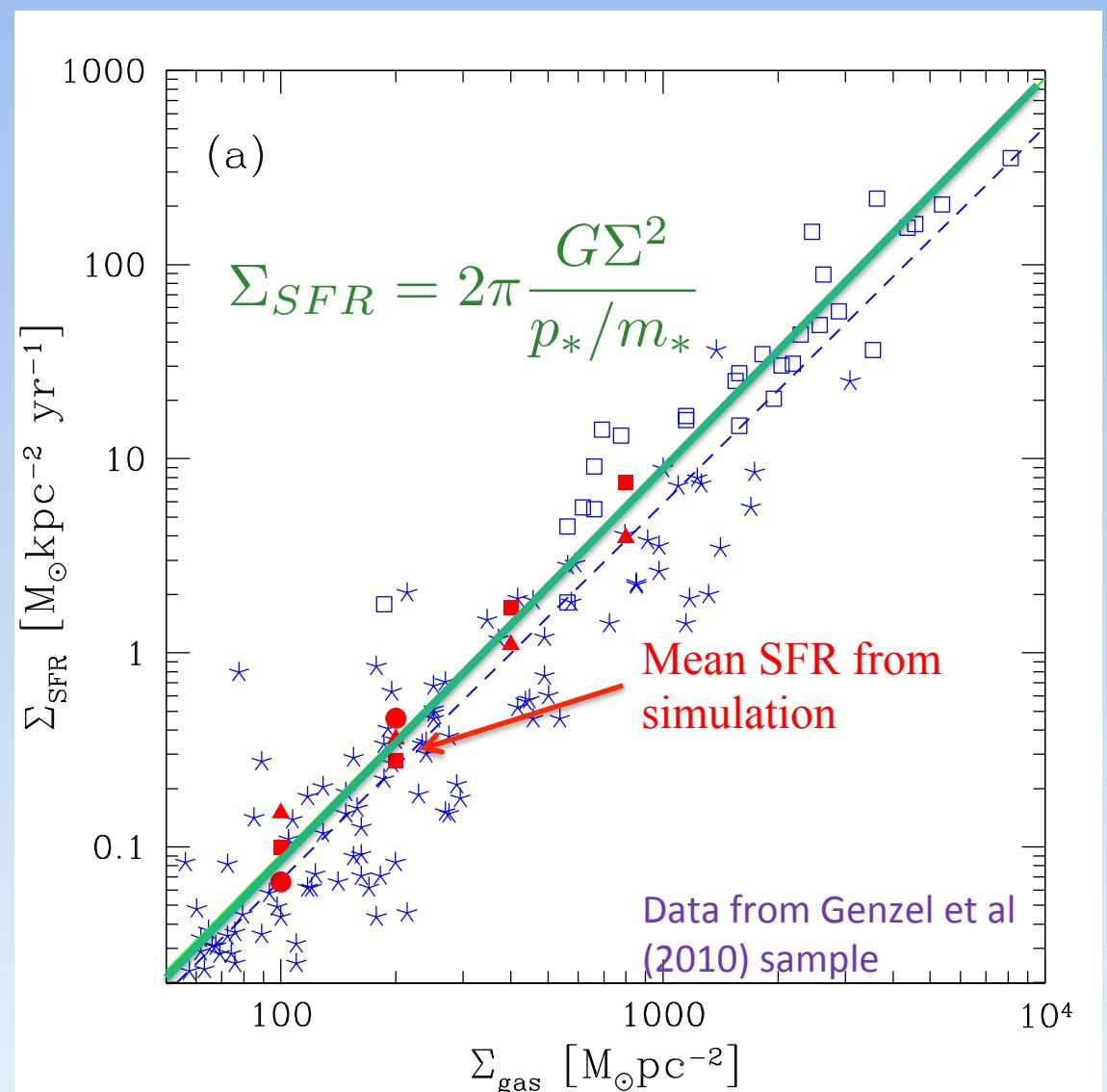
$$\Sigma_{SFR} \sim \frac{G\Sigma^2}{p_*/m_*}$$

- Star formation rate per unit area in disk is
  - *independent* of details of turbulence  $\pi G \Sigma^2 / 2 =$  weight of gas  
= Pressure
  - *independent* of small-scale collapse rate
- Disk thickness and internal dynamical time must adjust until momentum feedback rate matches vertical gravitational force on ISM

# Starburst regime



Ostriker & Shetty (2011)



Adopt:  $p_* = 300,000$  km/s for SNR with “momentum feedback,” isothermal EOS

# Self-regulation in outer disks

Allowing for *thermal* and *magnetic* as well as *turbulent* feedback to atomic gas,  $P_{\text{th}} = \eta_{\text{th}} \Sigma_{\text{SFR}}$ ,  $\delta P_{\text{mag}} = \eta_{\text{mag}} \Sigma_{\text{SFR}}$  and  $P_{\text{turb}} = \eta_{\text{turb}} \Sigma_{\text{SFR}}$ , leading to

$$\Sigma_{\text{SFR}} = (P_{\text{th}} + \delta P_{\text{mag}} + P_{\text{turb}}) / (\eta_{\text{th}} + \eta_{\text{mag}} + \eta_{\text{turb}}) = P_{\text{DE}} / \eta_{\text{tot}}$$

for

$$P_{\text{DE}} = \frac{\Sigma}{2} g_z \approx \frac{\pi G \Sigma^2}{2} + \Sigma (2G\rho_*)^{1/2} \sigma_z$$

depending only on the total gravity and total gas surface density of the disk from vertical dynamical equilibrium

- General result is

$$\Sigma_{\text{SFR}} = 2 \times 10^{-3} M_{\odot} \text{ kpc}^{-2} \text{ yr}^{-1} \left( \frac{P/k}{10^4 \text{ cm}^{-3} \text{ K}} \right)$$

and for disk regions where stellar gravity dominates:

$$\Sigma_{\text{SFR}} = 2 \times 10^{-3} M_{\odot} \text{ kpc}^{-2} \text{ yr}^{-1} \left( \frac{\Sigma}{10 M_{\odot} \text{ pc}^{-2}} \right) \left( \frac{\rho_*}{0.1 M_{\odot} \text{ pc}^{-3}} \right)^{1/2}$$

# Exercise

- Integrating vertical component of momentum equation

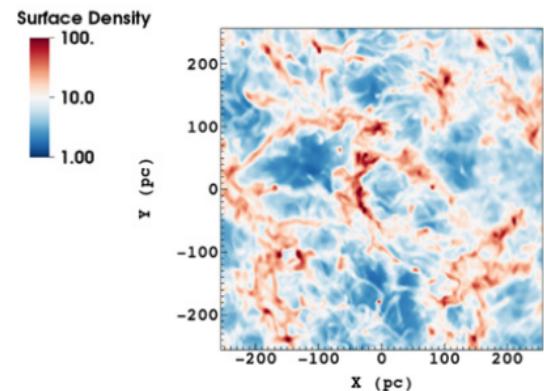
$$\frac{\partial(\rho\mathbf{v})}{\partial t} + \nabla \cdot \left[ \rho\mathbf{v}\mathbf{v} - \frac{\mathbf{B}\mathbf{B}}{4\pi} + \mathbf{I}(P + \frac{B^2}{8\pi}) \right] = -\rho\nabla\Phi$$

from  $z$  to  $z_{max}$  in steady state, show:

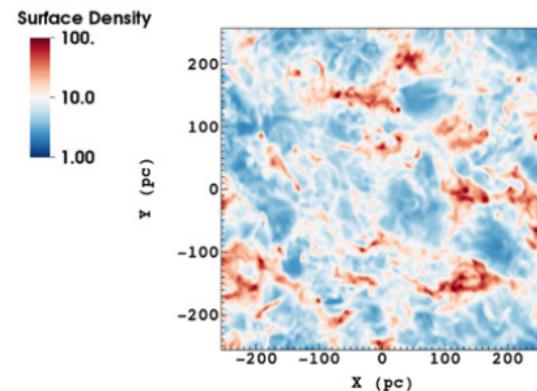
$$\langle \rho v_z^2 + P \rangle_z + \left\langle \frac{|\mathbf{B}|^2}{8\pi} - \frac{B_z^2}{4\pi} \right\rangle \Big|_z^{z_{max}} = - \int_z^{z_{max}} \rho \frac{\partial \Phi}{\partial z} dz$$

$$\text{For } z=0 \text{ and } \Phi_{\text{gas}}, \text{ show } - \int_0^{z_{max}} \rho \frac{\partial \Phi}{\partial z} dz = \frac{\pi G \Sigma^2}{2}$$

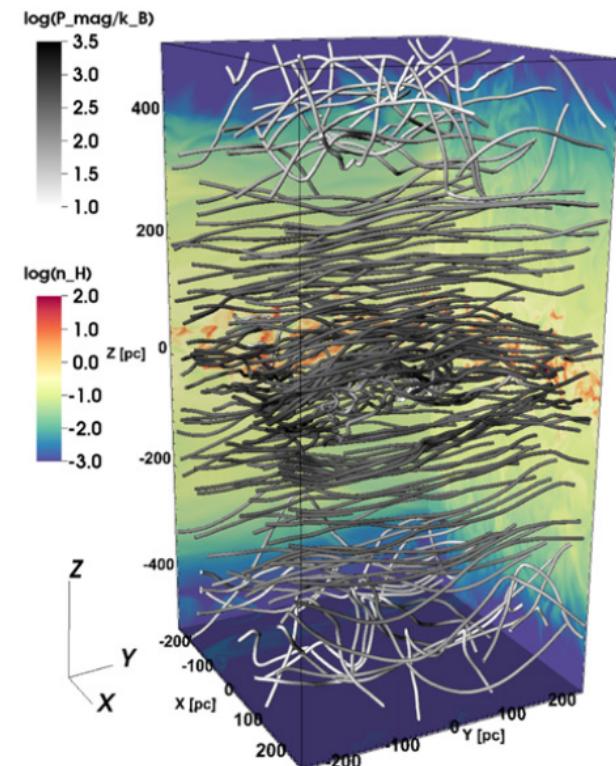
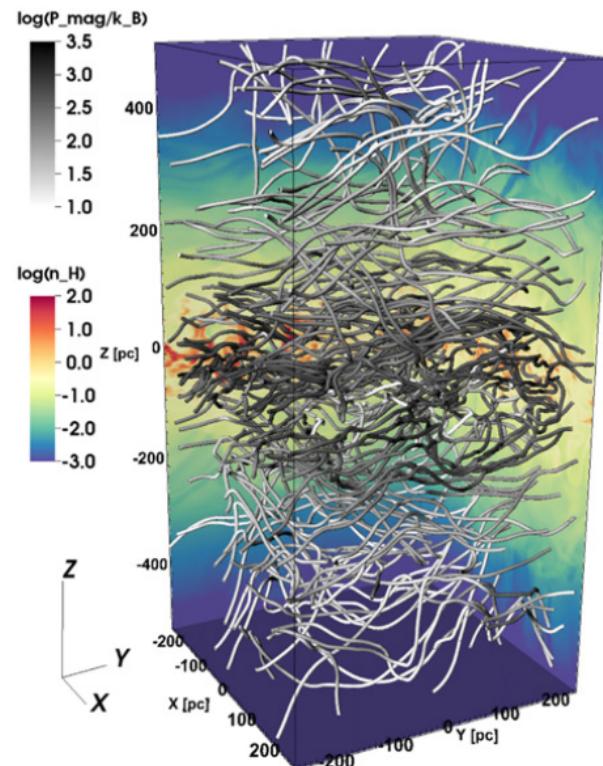
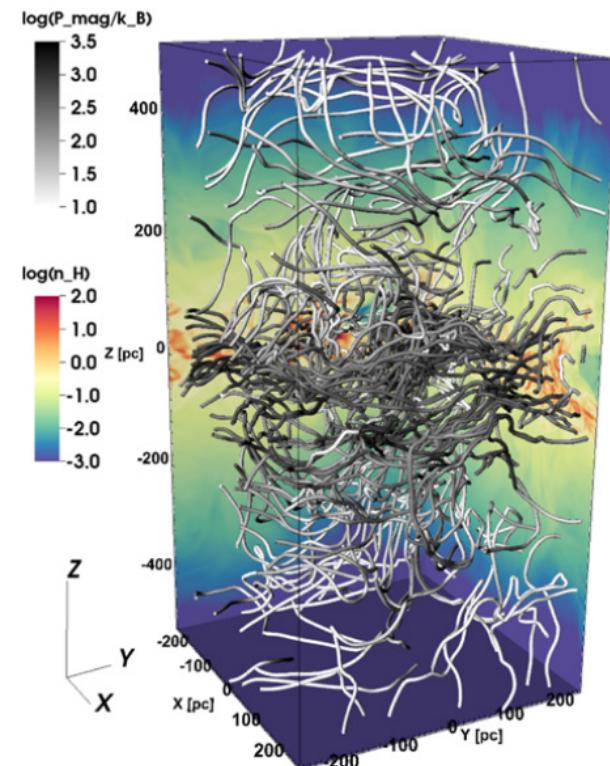
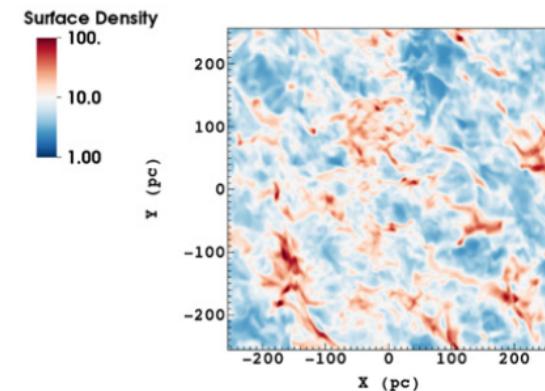
(a) MA 100



(b) MB10



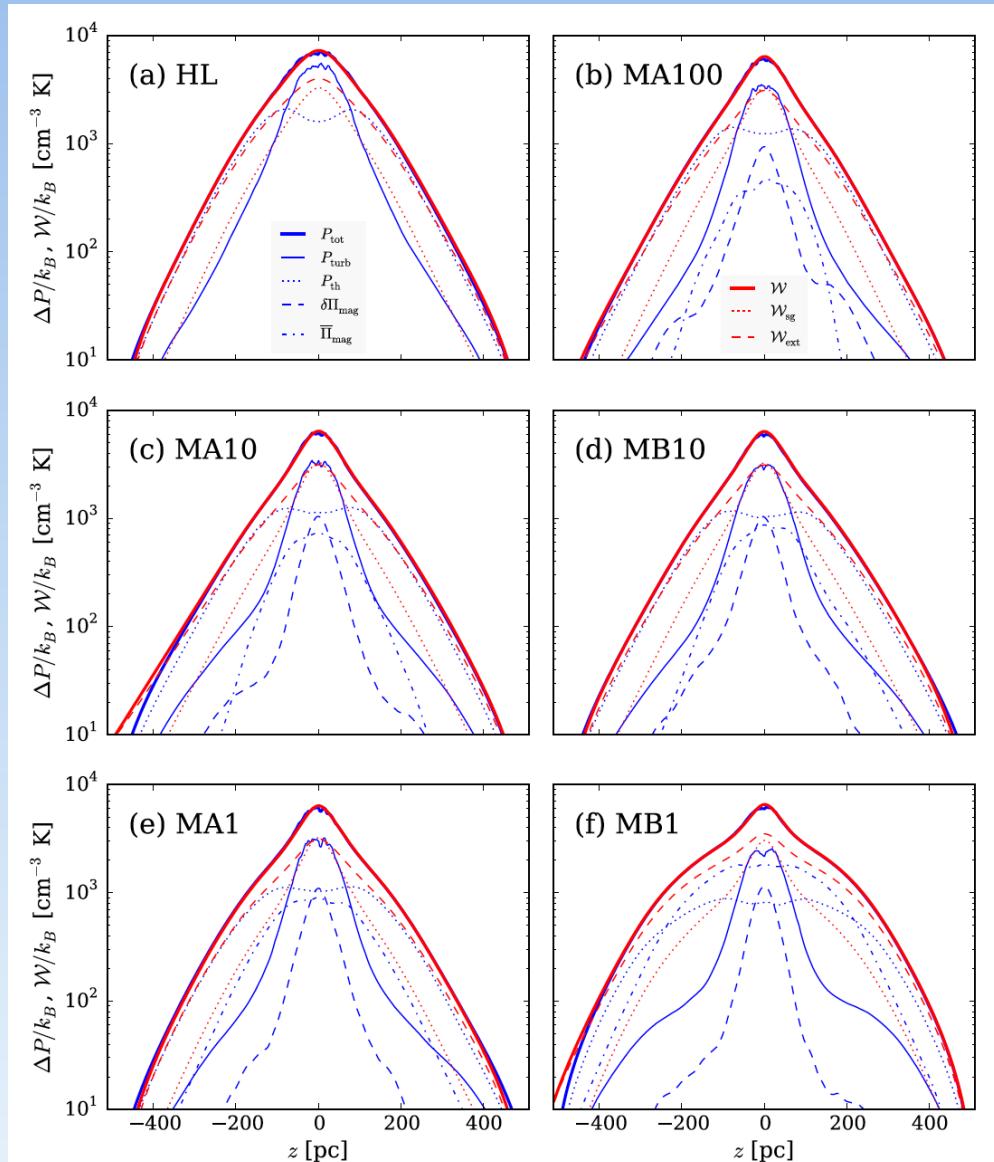
(c) MBT

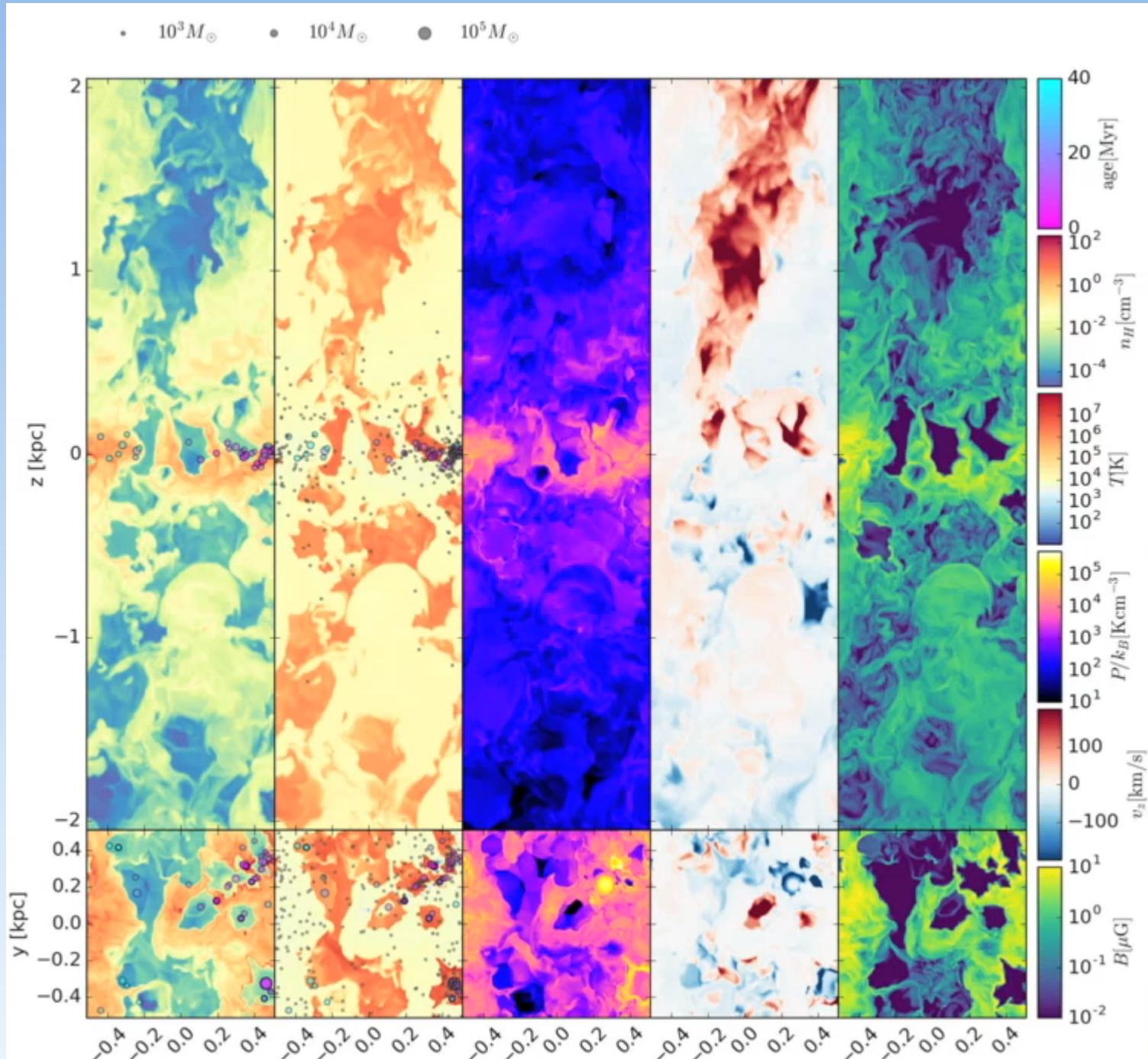


7/26/16

Kim & Ostriker (2015)

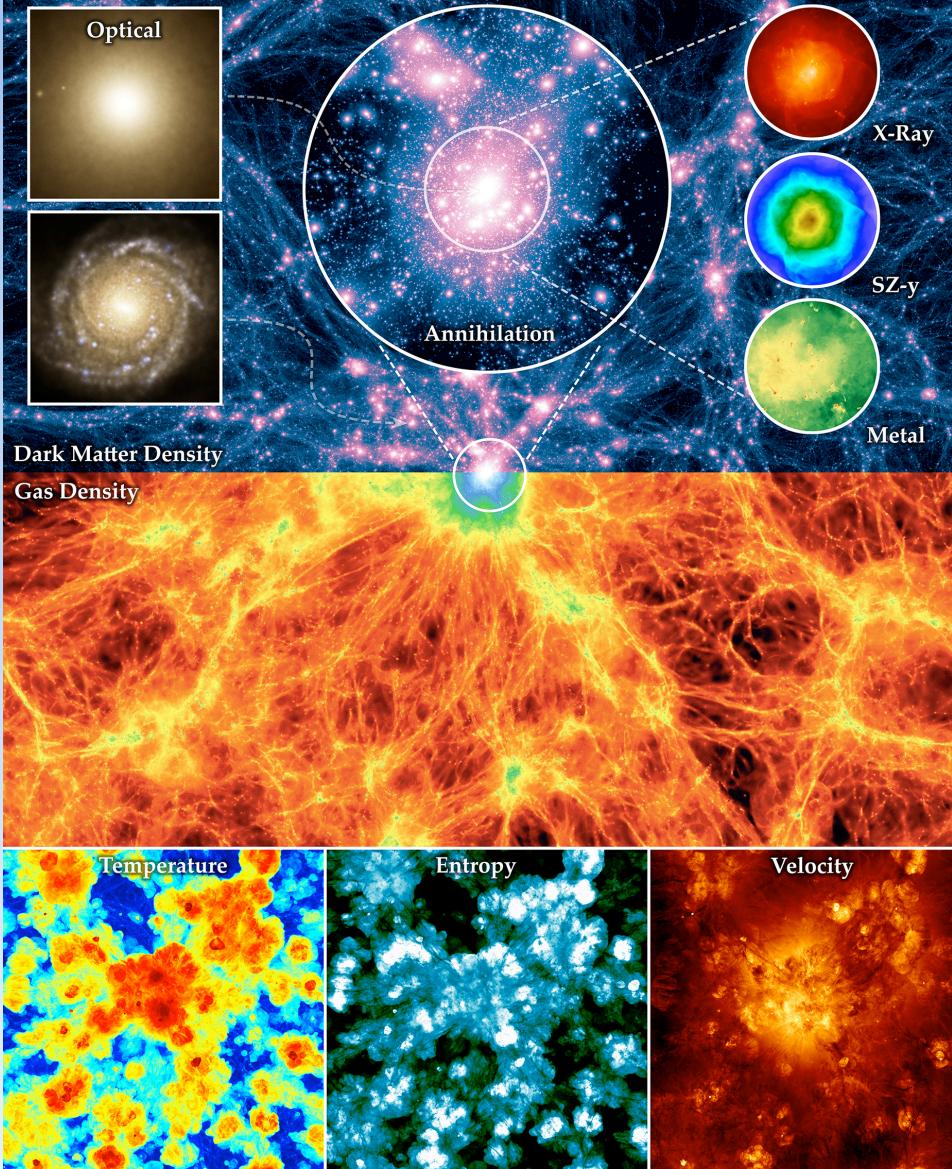
# Vertical equilibrium





# The Illustris Simulation

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*“Only connect.”*

-- E.M. Forster

# *... and a final word*



Think♦Read♦Act

Read♦Act♦Think

Act♦Think♦Read

*“All this will not be finished in the first 100 days. Nor will it be finished in the first 1,000 days... But let us begin.*

*In your hands, my fellow citizens, more than in mine, will rest the final success or failure of our course.”*

-- J.F. Kennedy (1961)