

Intro to collider physics

Lian-Tao Wang
University of Chicago

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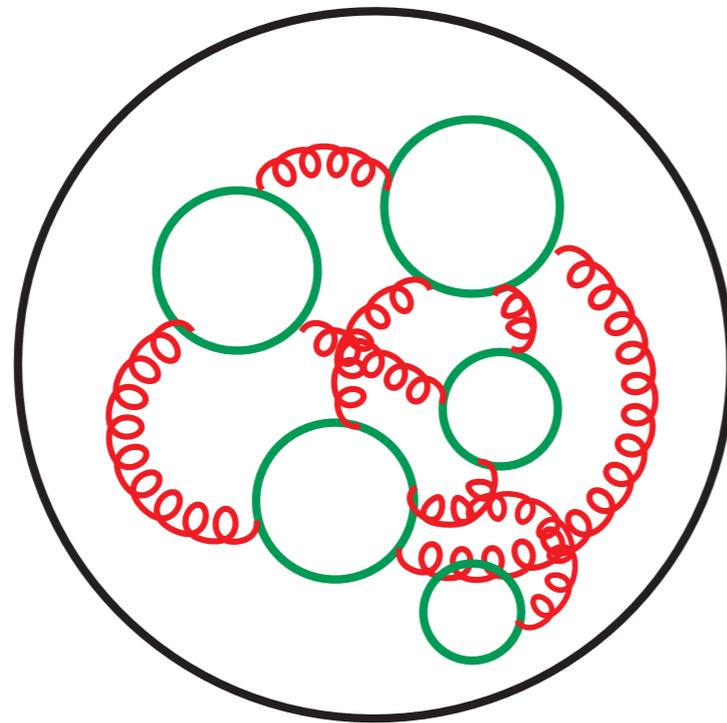
Before we start

- This is a huge subject.
 - Focus more on intuitive understanding, generic feature, less on specifics.
 - Only a (small) subset.
- Focus on methodology, rather than specific models.

Hopefully, this serves as the starting point of
your further study.

Many good references, such as
Tao Han, TASI lecture, [hep-ph/0508097](https://arxiv.org/abs/hep-ph/0508097)

proton



 gluon

 quark

Partons:

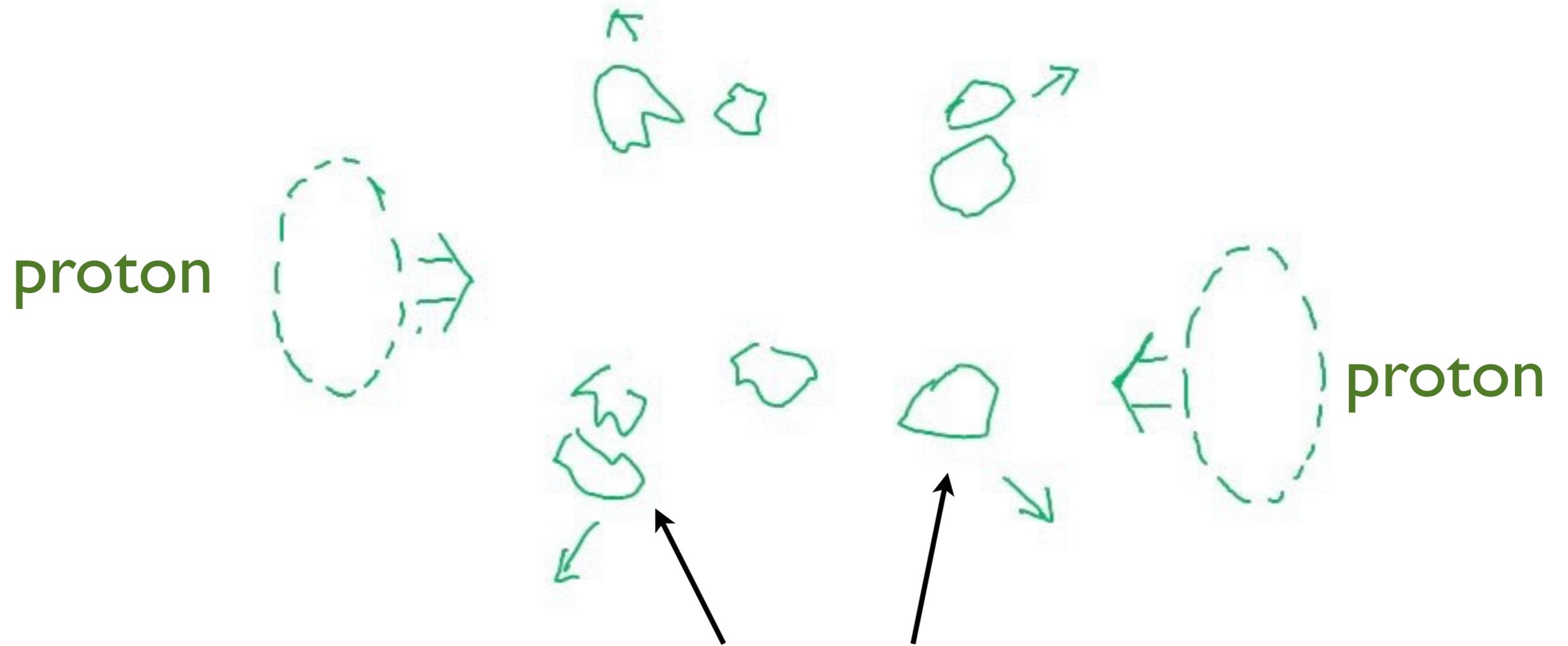
gluon

valence: u, d

“sea”: $q\bar{q}$, s \bar{s} , c, $c\bar{c}$, b, $b\bar{b}$

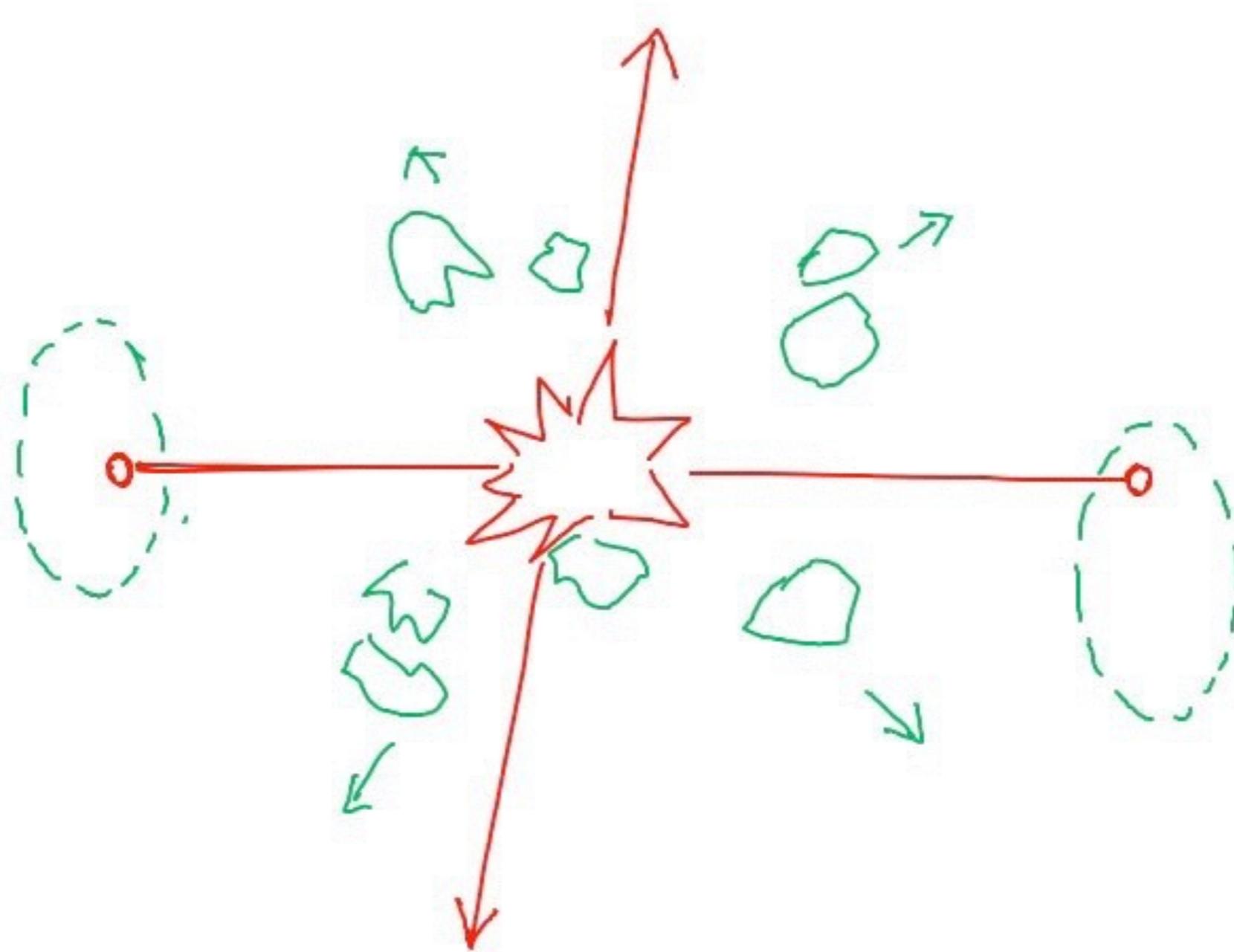
binding energy \sim GeV

Most of the time

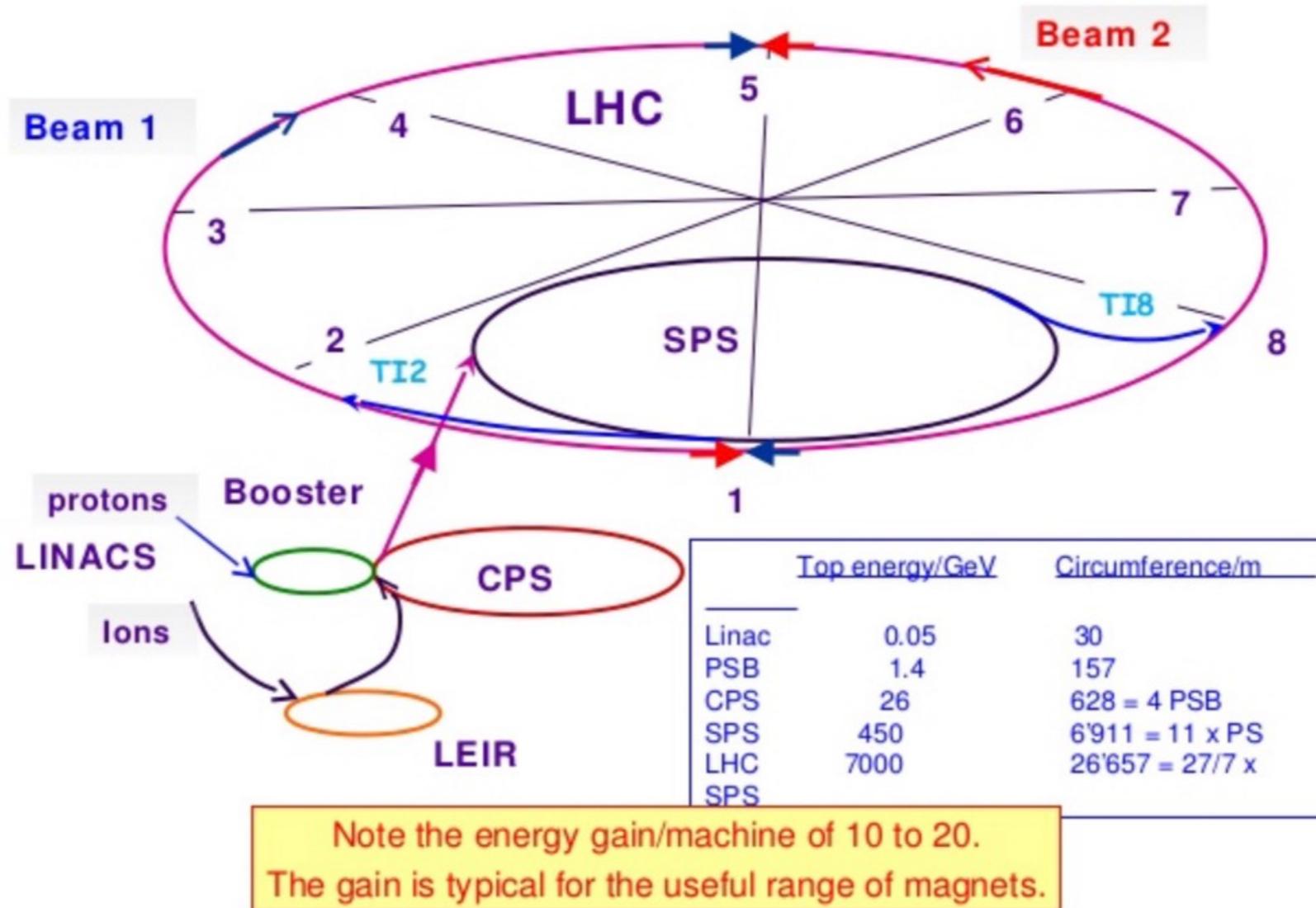


low energy fragments: $E \sim \text{GeV}$

High energy collision rare



The Large Hadron Collider (LHC)



Luminosity

$$L \propto k N^2 f / a$$

f : revolution freq $f \sim 11.25 \text{ kHz}$

N : # of protons in a bunch. $N \sim 10^{11}$

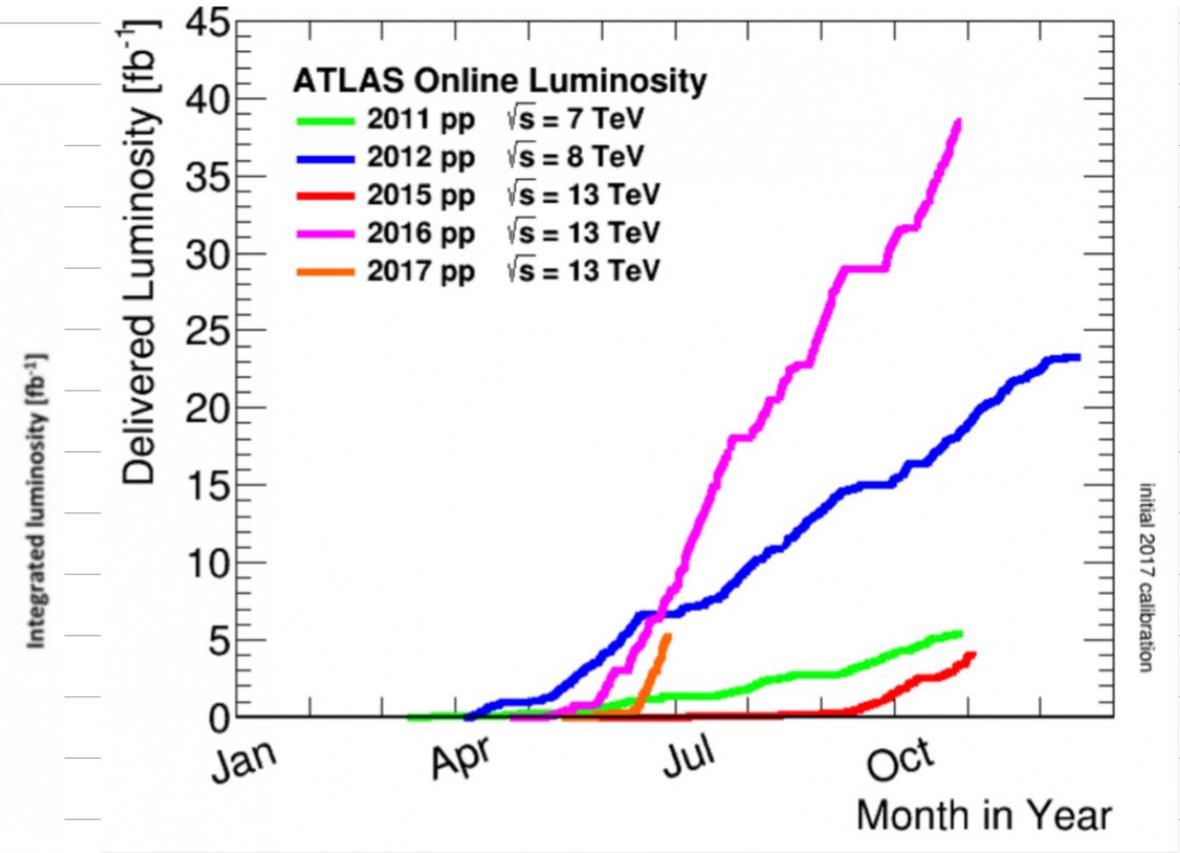
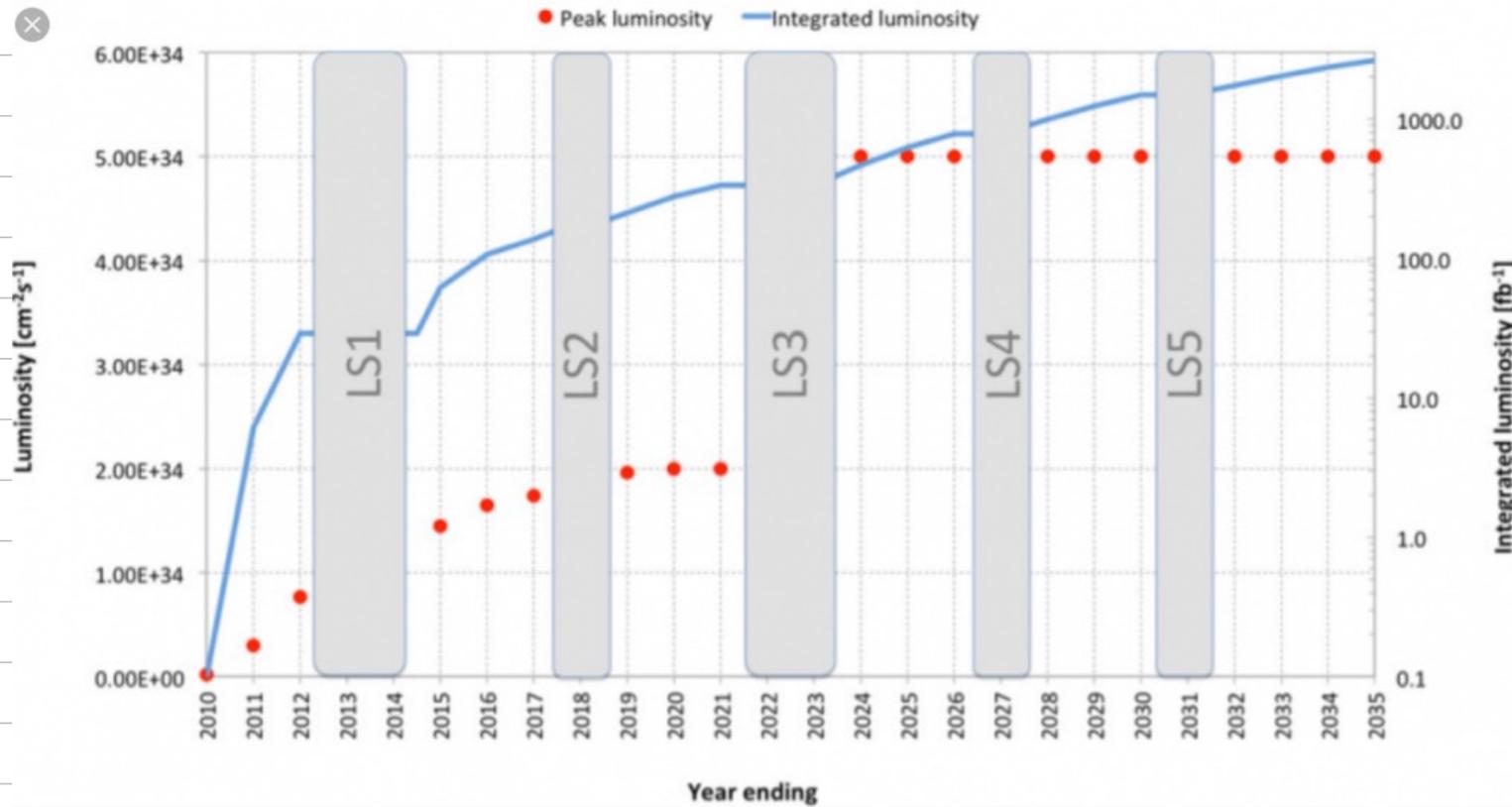
k : # of bunches $k = 2808$

a : beam size (area) $A \sim \pi (16 \mu\text{m})^2$



$$\# \text{ events} = L \cdot \sigma \quad \sigma : \text{cross section.}$$

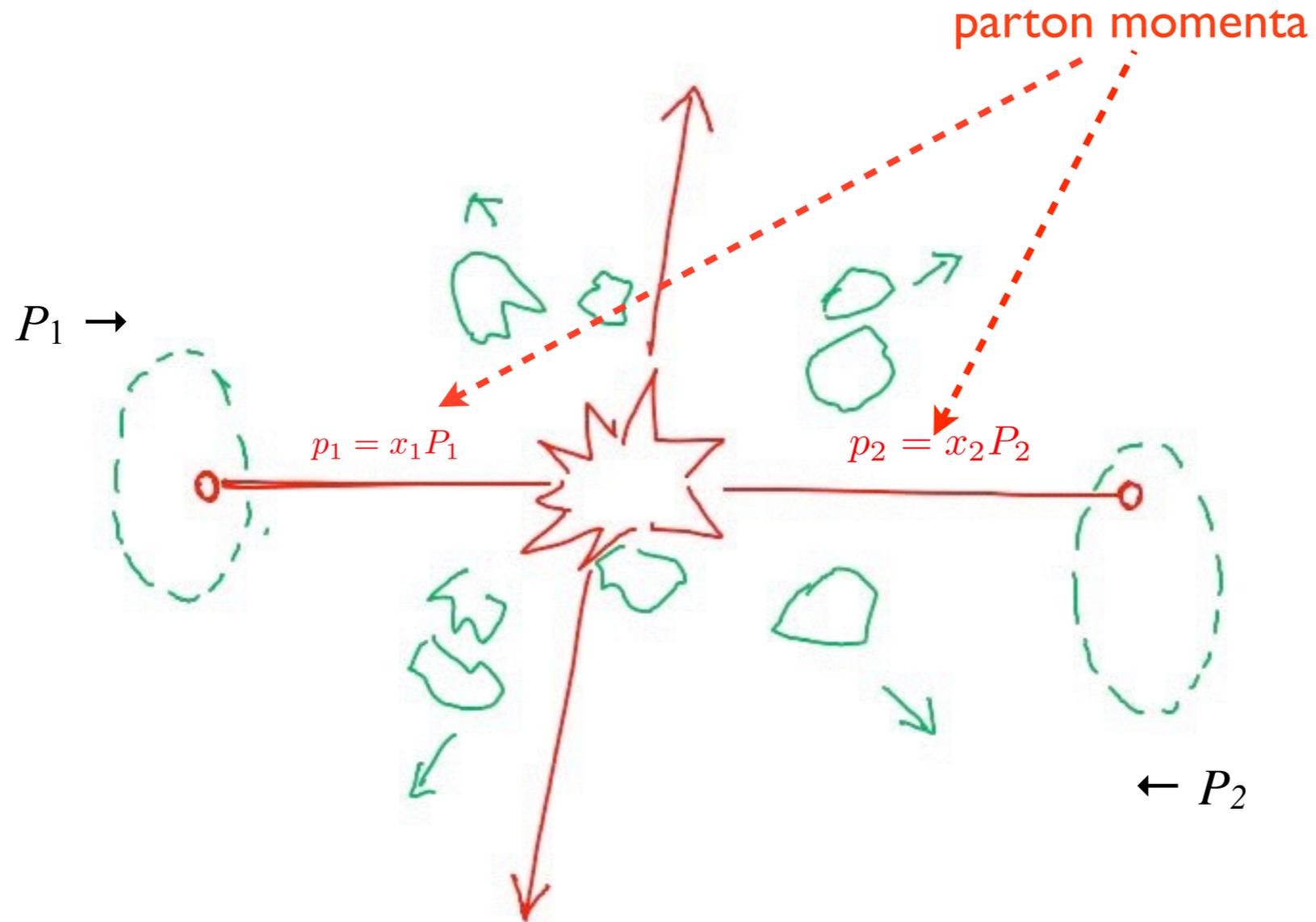
LHC Luminosity



$$1 \text{ mb} \equiv 10^{-27} \text{ cm}^2 = 2.56 (\text{GeV})^{-2}$$

$$10^{34} \text{ cm}^{-2} \text{ s}^{-1} \sim 100 \text{ fb}^{-1} / \text{yr}$$

Kinematics



$$P_1 = (E_1, 0, 0, E_1), \quad P_2 = (E_2, 0, 0, -E_2) \quad \sqrt{S} = E_{\text{cm}}^{\text{collider}} = E_1 + E_2$$

$$\sqrt{\hat{s}} = \sqrt{(p_1 + p_2)^2} = E_{\text{cm}}^{\text{parton}} = \sqrt{x_1 x_2 S}$$

Rapidity

Define rapidity

$$y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$$

$$p^\mu = (E_T \cosh y, p_T \sin \phi, p_T \cos \phi, E_T \sinh y), \quad E_T = \sqrt{p_T^2 + m^2}$$

Under boost along z-direction

$$y' = \frac{1}{2} \ln \frac{E' + p'_z}{E' - p'_z} = \frac{1}{2} \ln \frac{(1 - \beta_0)(E + p_z)}{(1 + \beta_0)(E - p_z)} = y - y_0$$

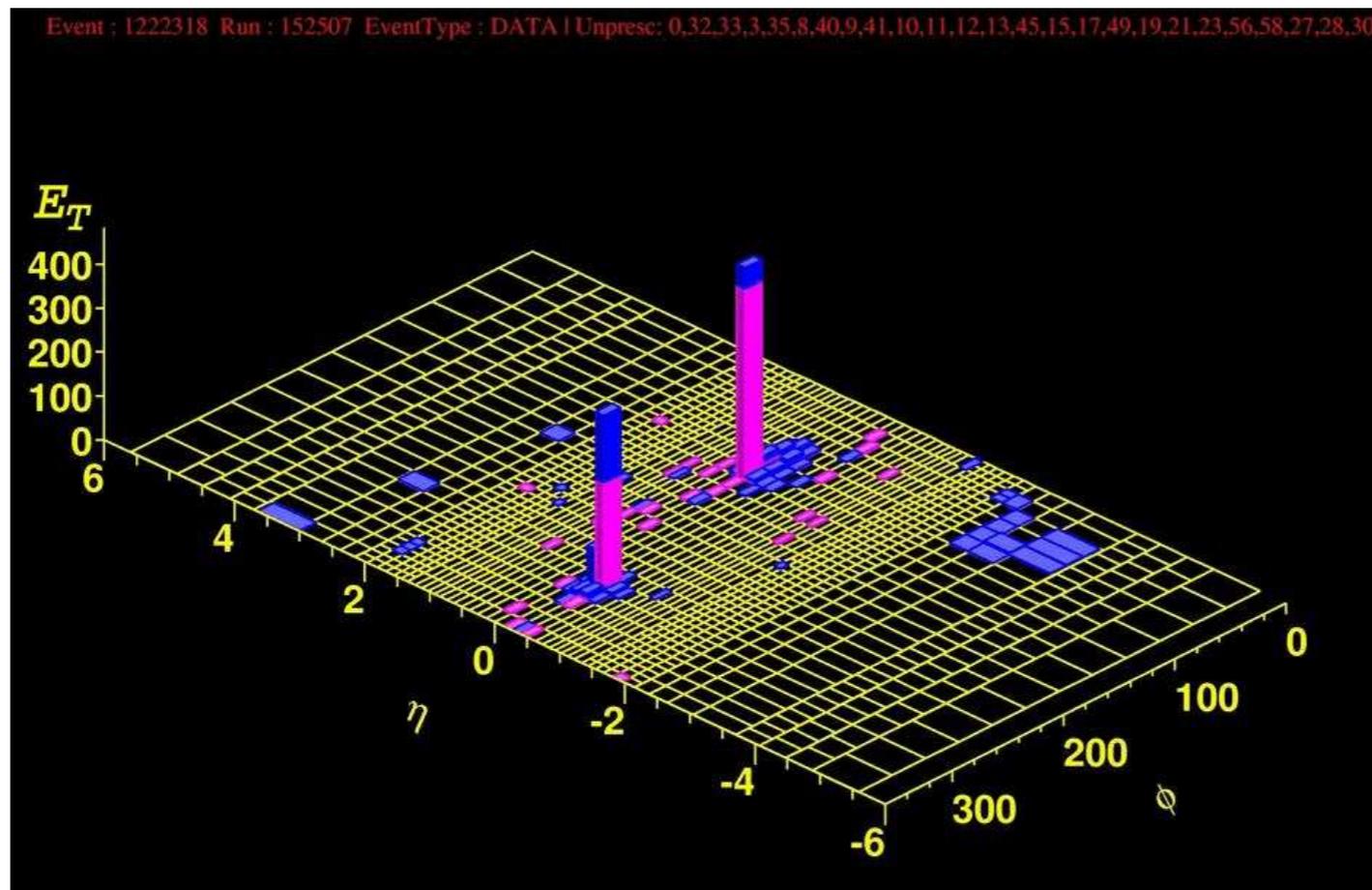
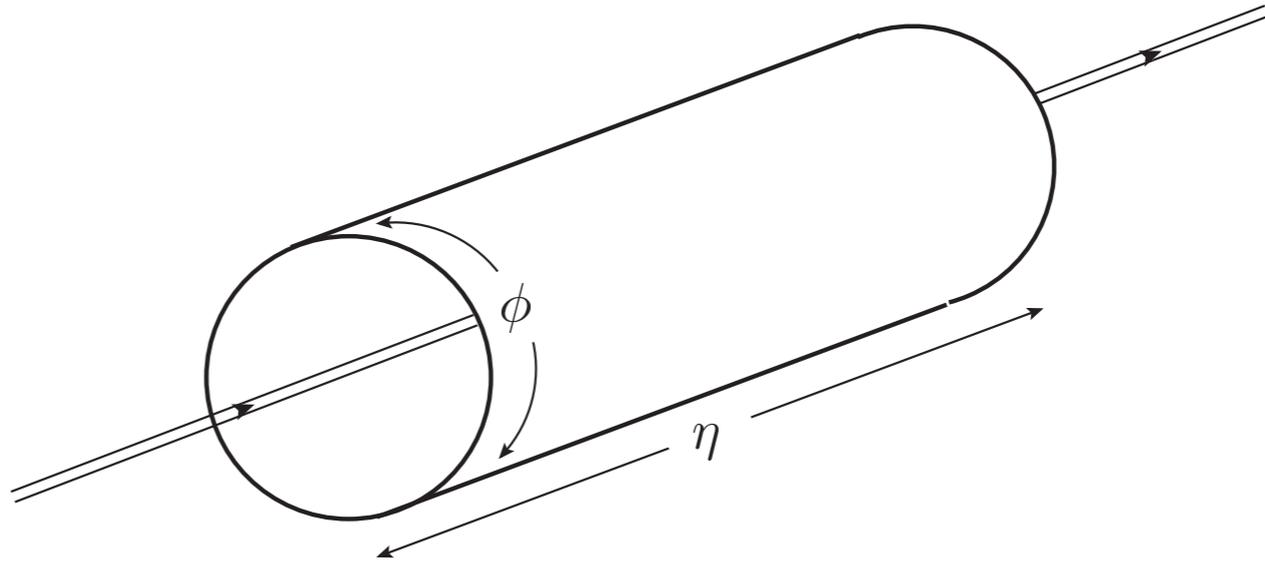
$$\rightarrow \frac{d}{dy} = \frac{d}{dy'}$$

In the massless limit : pseudo-rapidity

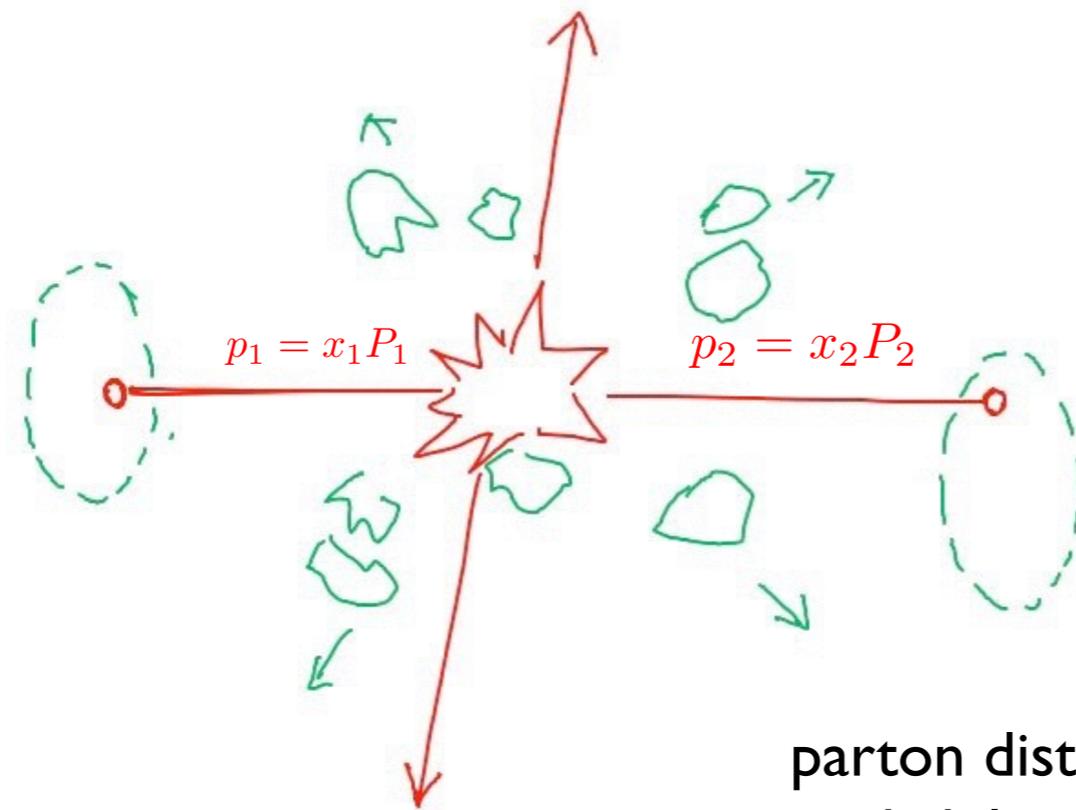
$$y \rightarrow \frac{1}{2} \ln \frac{1 + \cos \theta}{1 - \cos \theta} = \ln \cot \frac{\theta}{2} \equiv \eta$$

Coordinate System

$$\eta = -\ln \left[\cot \left(\frac{\theta}{2} \right) \right]$$



Parton Distribution Function (PDF)



Partons can be gluon,
or different flavors of quarks,
labelled by a, b...

parton distribution function $f_a(x)$:
probability of finding parton a with momentum fraction x

- $f_a(x)$ can not be computed.
- However, we can measure them using certain processes.
- They are universal! Can be used everywhere!

Prediction for hadron collisions

$$a + b \rightarrow \dots$$

$$\sigma = \sum_{a,b} \int dx_1 dx_2 f_a(x_1) f_b(x_2) \hat{\sigma}$$

PDF, long distance
Universal

“Hard scattering”
Short distance
Partonic cross section
Calculable

Factorization!

Intuitively, make sense:

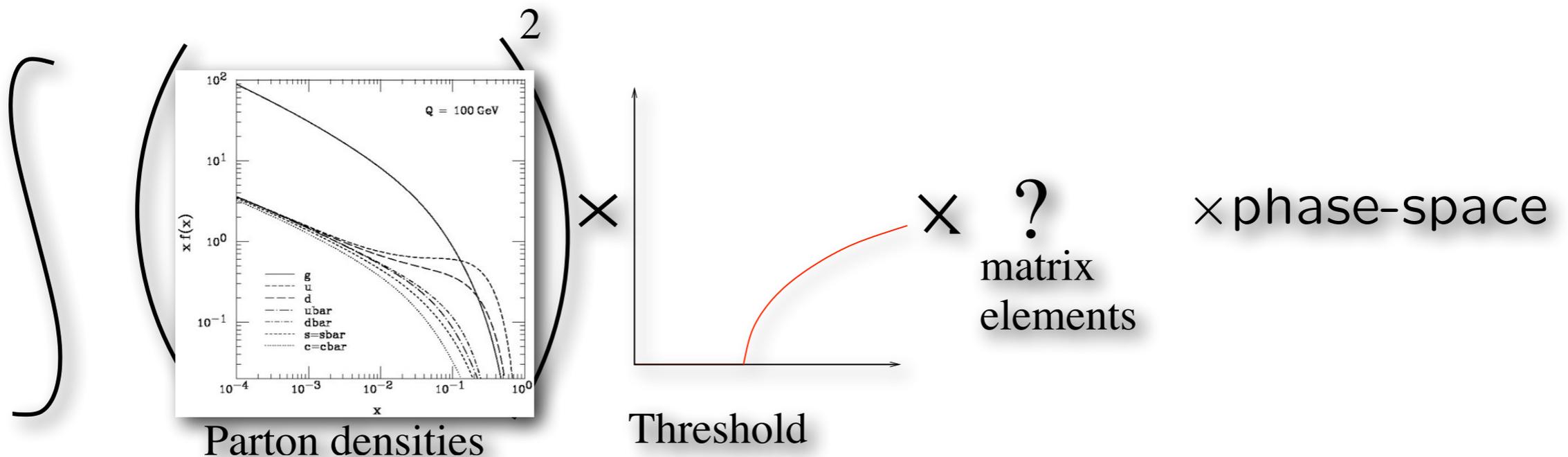
short distance physics should not “know” about long distance physics.

In practice, very difficult to prove.

However, it is used anyway (otherwise we cannot calculate anything).
And, it works very well.

Production.

- Schematics of production at hadron colliders.
- Dominated by parton densities and thresholds (mass and cut).



$$a + b \rightarrow \dots$$

$$\frac{d^2\sigma(a, b \rightarrow \dots)}{d\hat{s} dY} = \frac{1}{\hat{s}} \sum_{a,b} x_1 f_a(x_1) x_2 f_b(x_2) \hat{\sigma}(a, b \rightarrow \dots)$$

Partonic cross section

A useful representation

$$P_1 = (E, 0, 0, E), \quad P_2 = (E, 0, 0, -E) \quad p_1 = x_1 P_1, \quad p_2 = x_2 P_2$$

Define Parton center of mass rapidity: $Y \quad e^Y = \sqrt{\frac{x_1}{x_2}}$

We can verify $\cosh Y = \frac{(x_1 + x_2)E}{\sqrt{\hat{s}}} \Rightarrow$ boost of parton c.o.m frame

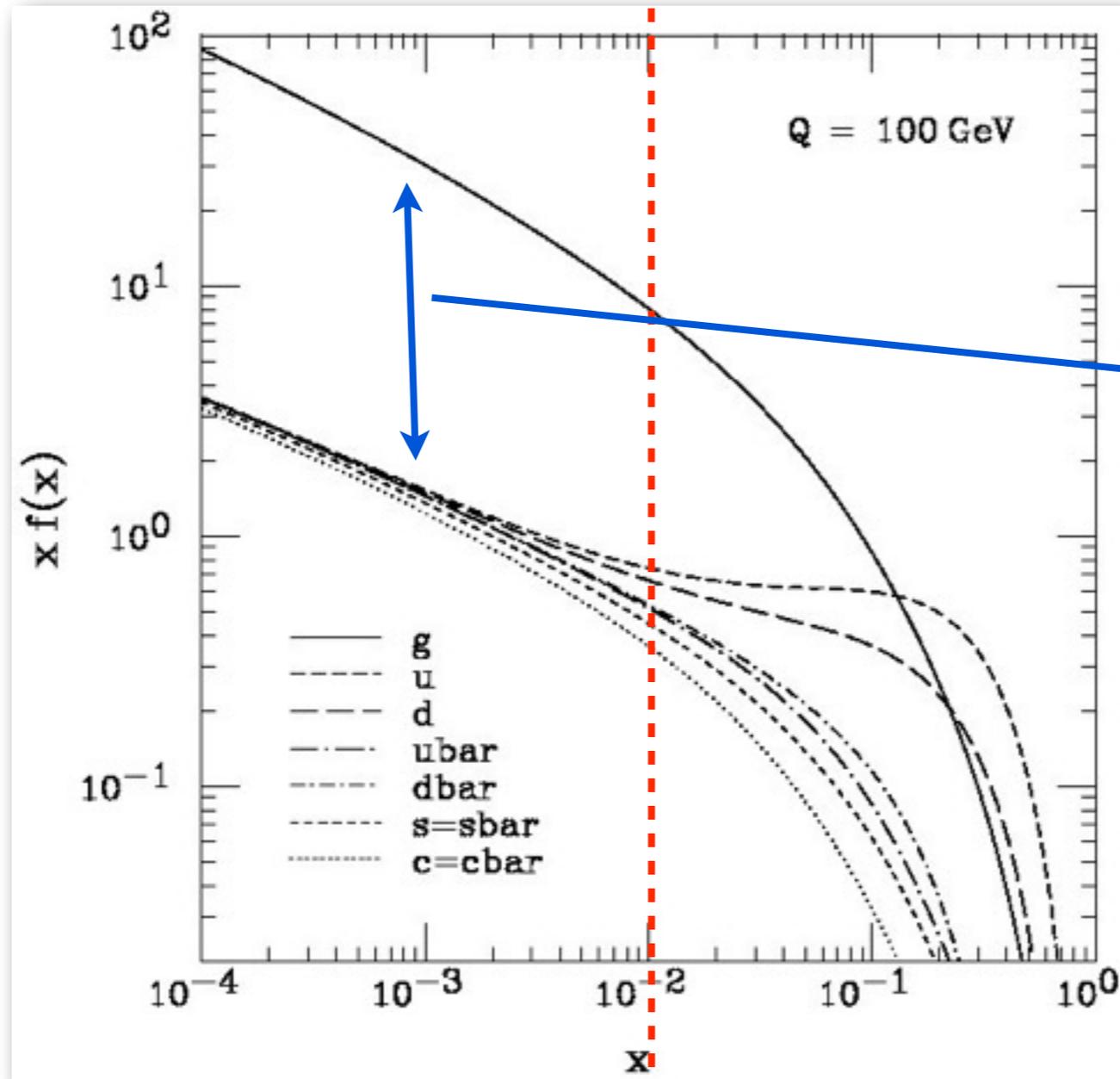
Starting with $\frac{d^2\sigma(a, b \rightarrow \dots)}{dx_1 dx_2} = \sum_{a,b} f_a(x_1) f_b(x_2) \hat{\sigma}(a, b \rightarrow \dots)$

Using Jacobian: $\frac{\partial|\hat{s}, Y|}{\partial|x_1, x_2|} = \frac{\hat{s}}{x_1 x_2}$

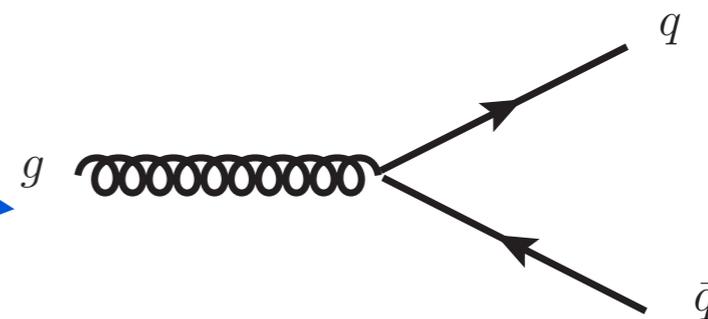
We obtain:

$$\frac{d^2\sigma(a, b \rightarrow \dots)}{d\hat{s} dY} = \frac{1}{\hat{s}} \sum_{a,b} \underline{x_1 f_a(x_1)} \underline{x_2 f_b(x_2)} \hat{\sigma}(a, b \rightarrow \dots)$$

Parton Distribution Function



$$x = \frac{p_{\text{parton}}}{P_{\text{proton}}}$$

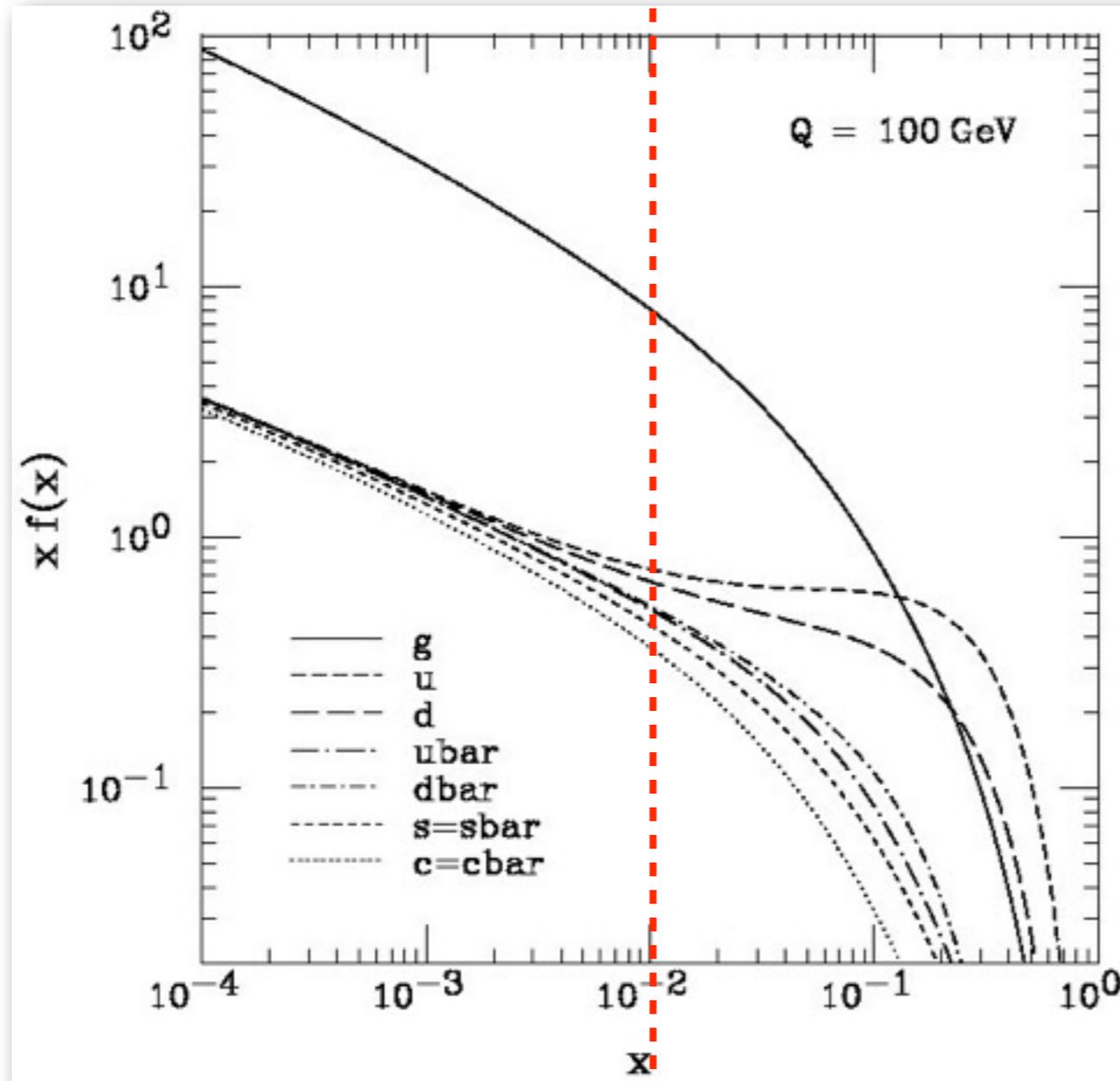


gluon splitting
main "source" for quark PDF

gluon dominated
 $q \approx \bar{q} \ll g$

Parton Distribution Function

$$x = \frac{p_{\text{parton}}}{P_{\text{proton}}}$$



gluon dominated
 $q \approx q_{\text{bar}} \ll \text{gluon}$

valence (u, d) \uparrow
 others fall with gluon

Parton luminosity

$$\sigma = \int dx_1 \int dx_2 f_1(x_1) f_2(x_2) \hat{\sigma}$$

define $\tau = x_1 x_2$ $x = x_1$ $\frac{\hat{s}}{s} = \tau$

Jacobian for variable change

$$\frac{\partial(x_1, x_2)}{\partial(\tau, x)} = \frac{1}{x}$$

$$\sigma = \int d\tau \int_x^1 dx \frac{1}{x} f_1(x) f_2\left(\frac{\tau}{x}\right) \hat{\sigma}$$

parton luminosity $L(\tau)$

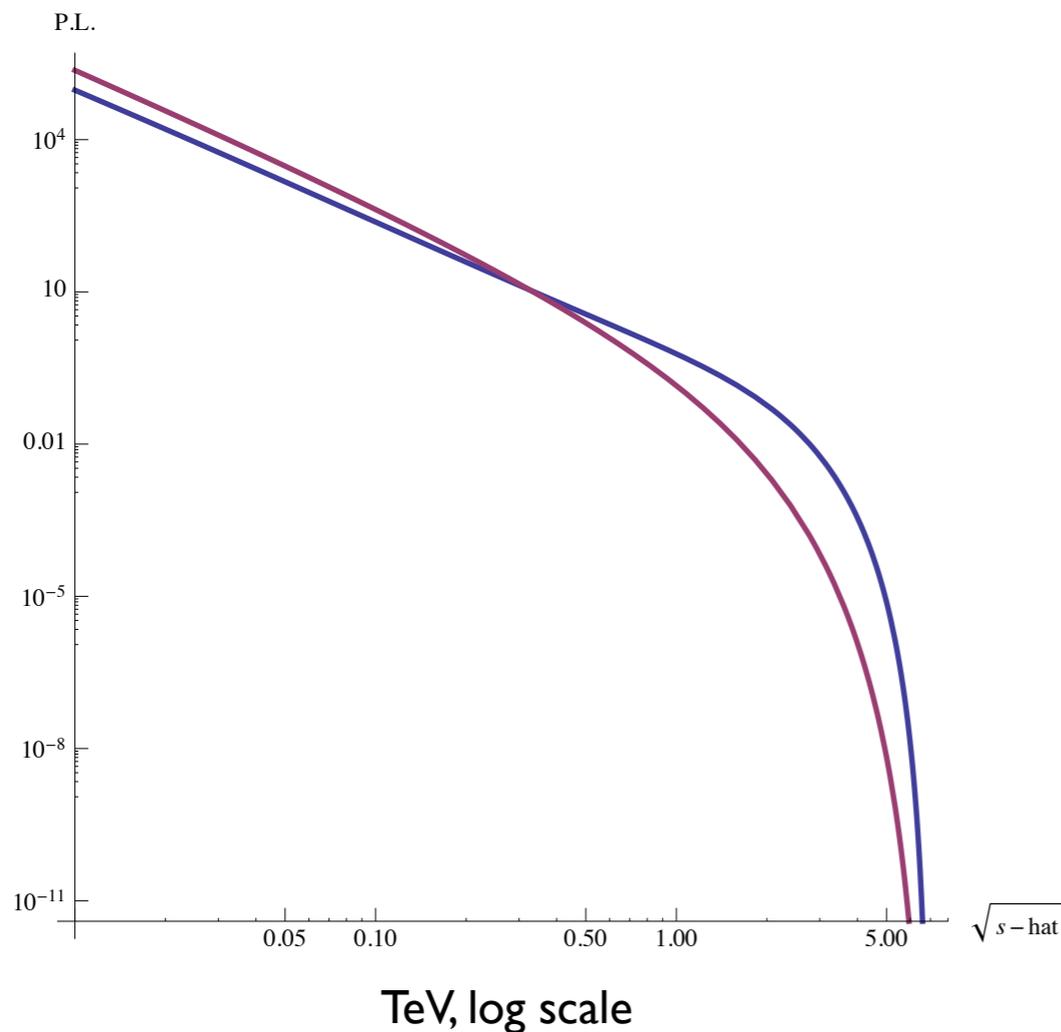
Another parameterization, parton luminosity

- The cross section can be written as

$$\sigma = \sum_{a,b} \int d\tau \frac{dL_{ab}}{d\tau} \hat{\sigma}$$

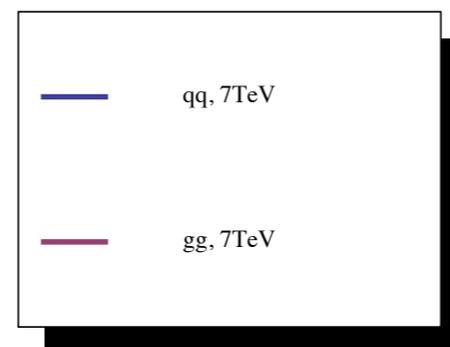
parton luminosity
 $\tau = \frac{\hat{s}}{S} = x_1 x_2$

$$L_{ab}(\tau) = \frac{1}{1 + \delta_{ab}} \int_{\tau}^1 \frac{dx}{x} \left[f_a(x) f_b\left(\frac{\tau}{x}\right) + f_a\left(\frac{\tau}{x}\right) f_b(x) \right]$$



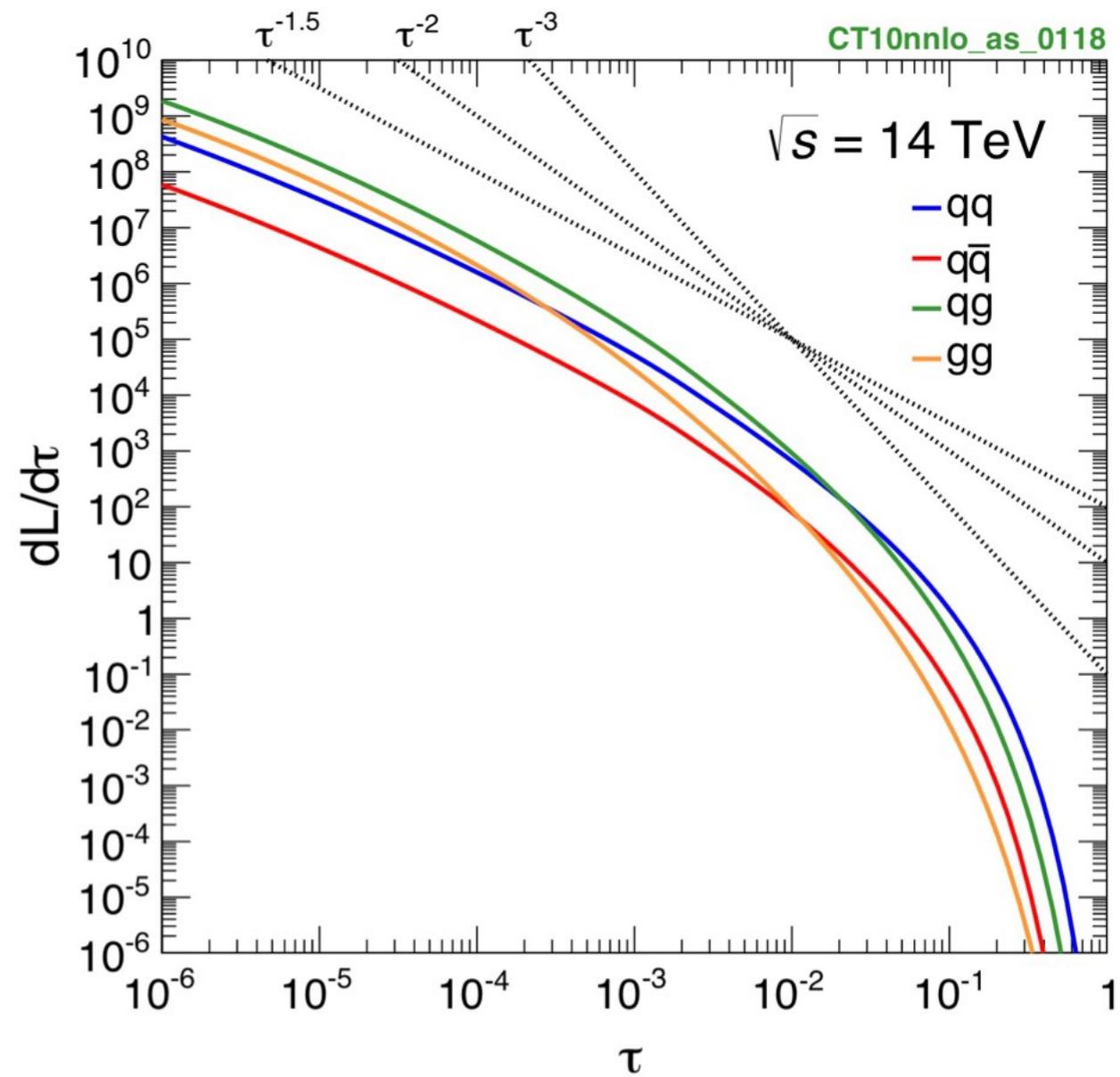
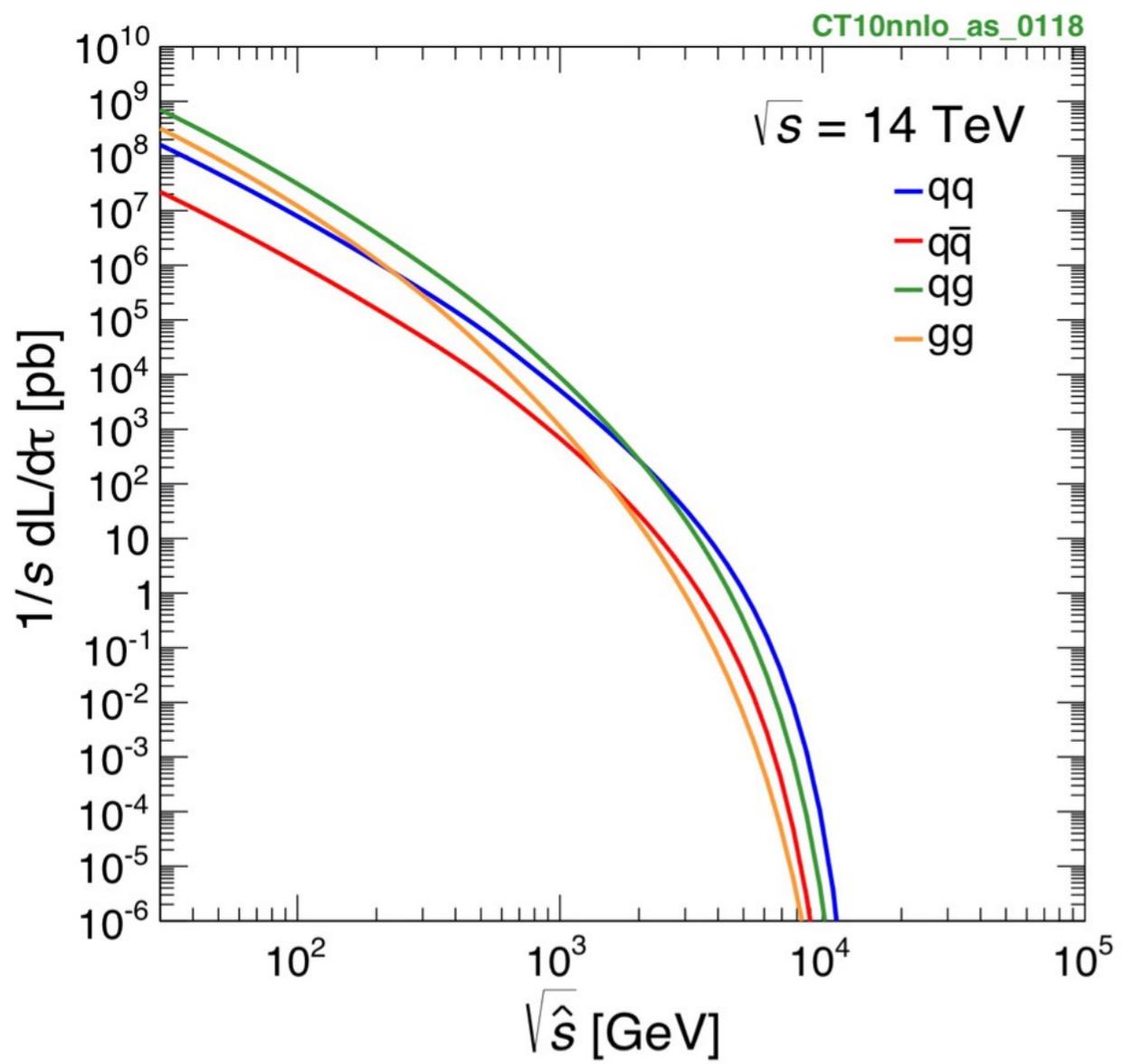
Very sharp falling

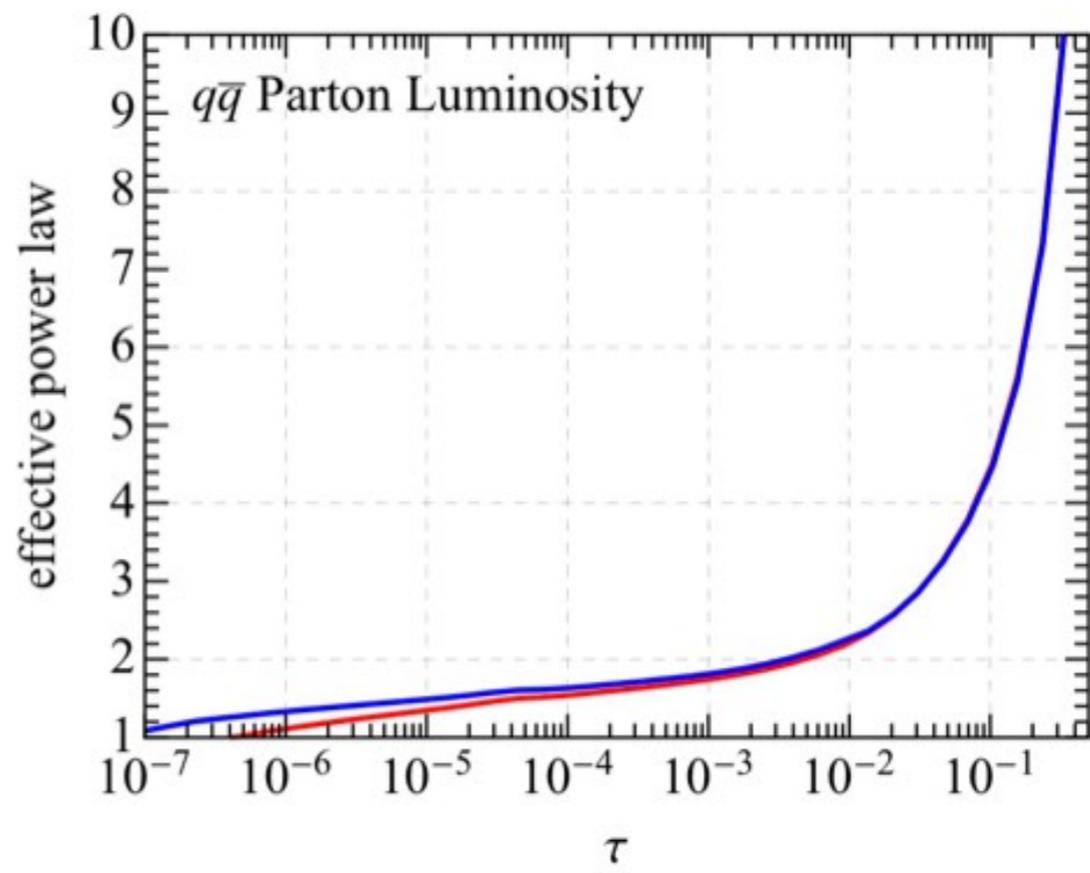
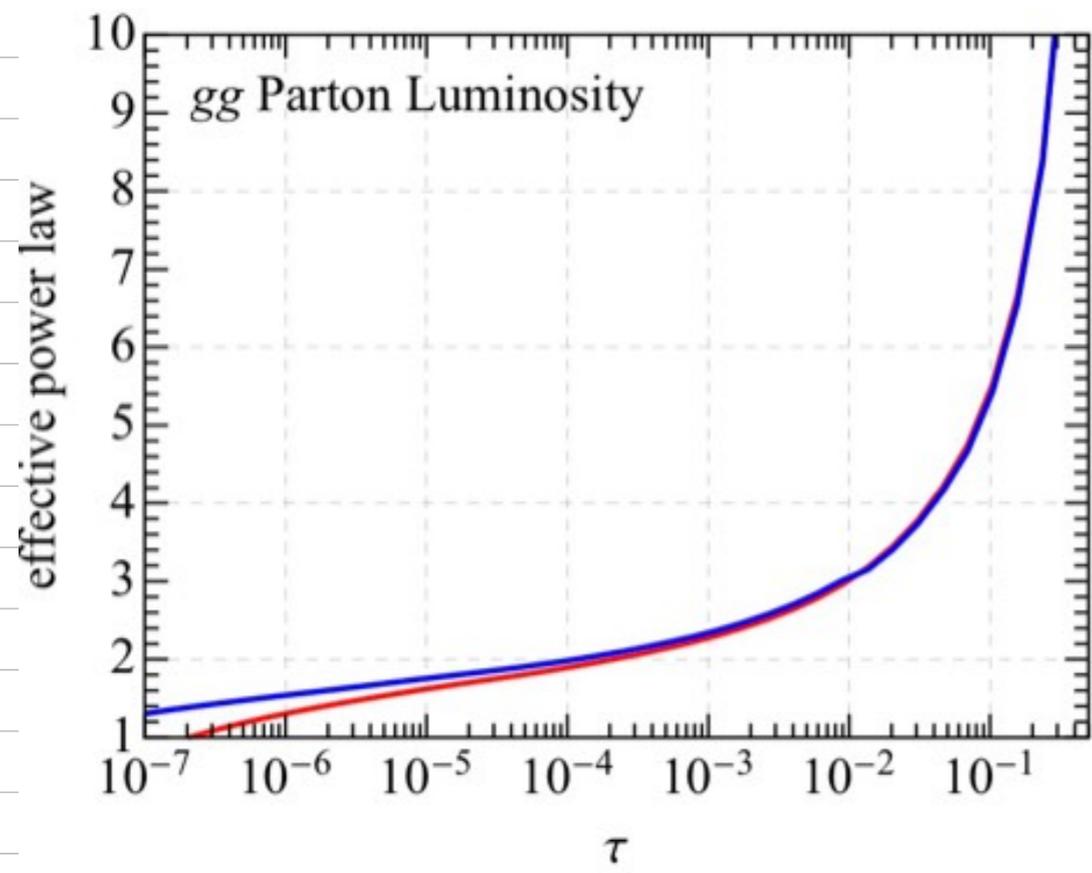
$$\propto \frac{1}{\tau^{3-3.5}}$$



Falls by a factor of 10 for every 600 GeV

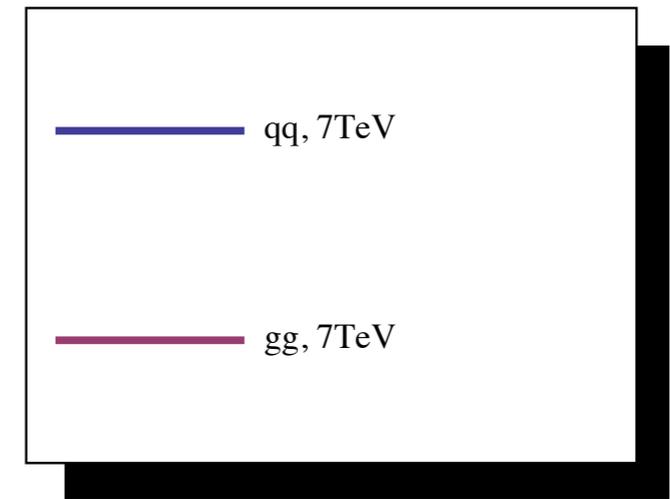
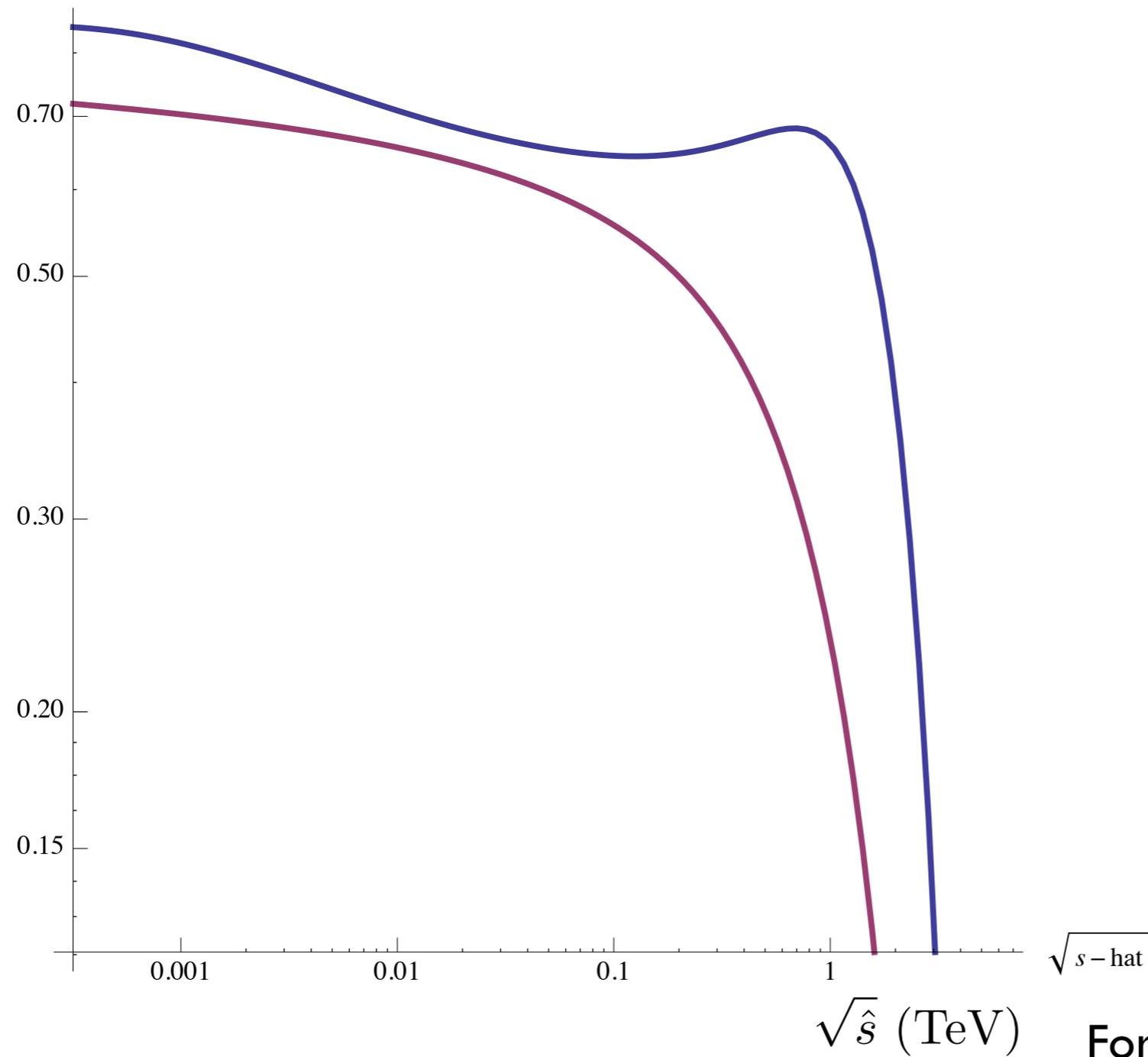
⇒ Production dominantly on threshold





7 TeV vs 14 TeV

$$\frac{P.L.[7 - \text{TeV}]}{P.L.[14 - \text{TeV}]}$$



For 7 TeV, PL shuts off at around TeV,
For 14 TeV, around 2 TeV.

Reach scales roughly with E_{cm} (same x).

Rough estimates of discovery reach

$$\sigma \sim L_p \cdot \hat{\sigma} \sim \frac{1}{\tau^a} \hat{\sigma}$$

L_p : parton luminosity, $\hat{\sigma}$: parton cross section

Production of new physics particle of mass M

Fast falling parton luminosity \Rightarrow
dominant contribution from
parton cross section near threshold

$$\hat{s} \sim M^2 \rightarrow \tau \sim \frac{M^2}{S}$$

$$\hat{\sigma} \sim \frac{1}{M^2}$$

Number of new physics particle produced:

$$N = \sigma \cdot \mathcal{L}$$

\mathcal{L} : luminosity

Discovery reach

Consider 2 colliders.

Collider 1: $E_{\text{cm}} = E_1$, or $S_1 = E_1^2$. Collider 2: $E_{\text{cm}} = E_2$, or $S_2 = E_2^2$.

$$E_2 > E_1$$

Reach for new physics at these 2 colliders

Collider 1: M_1 . Collider 2: M_2 .

Assume the reach is obtained from the same number of signal events

$$\frac{1}{\tau_1^a} \frac{1}{M_1^2} \mathcal{L}_1 = \frac{1}{\tau_2^a} \frac{1}{M_2^2} \mathcal{L}_2 \quad \text{used} \quad \hat{\sigma} \sim \frac{1}{M^2}$$

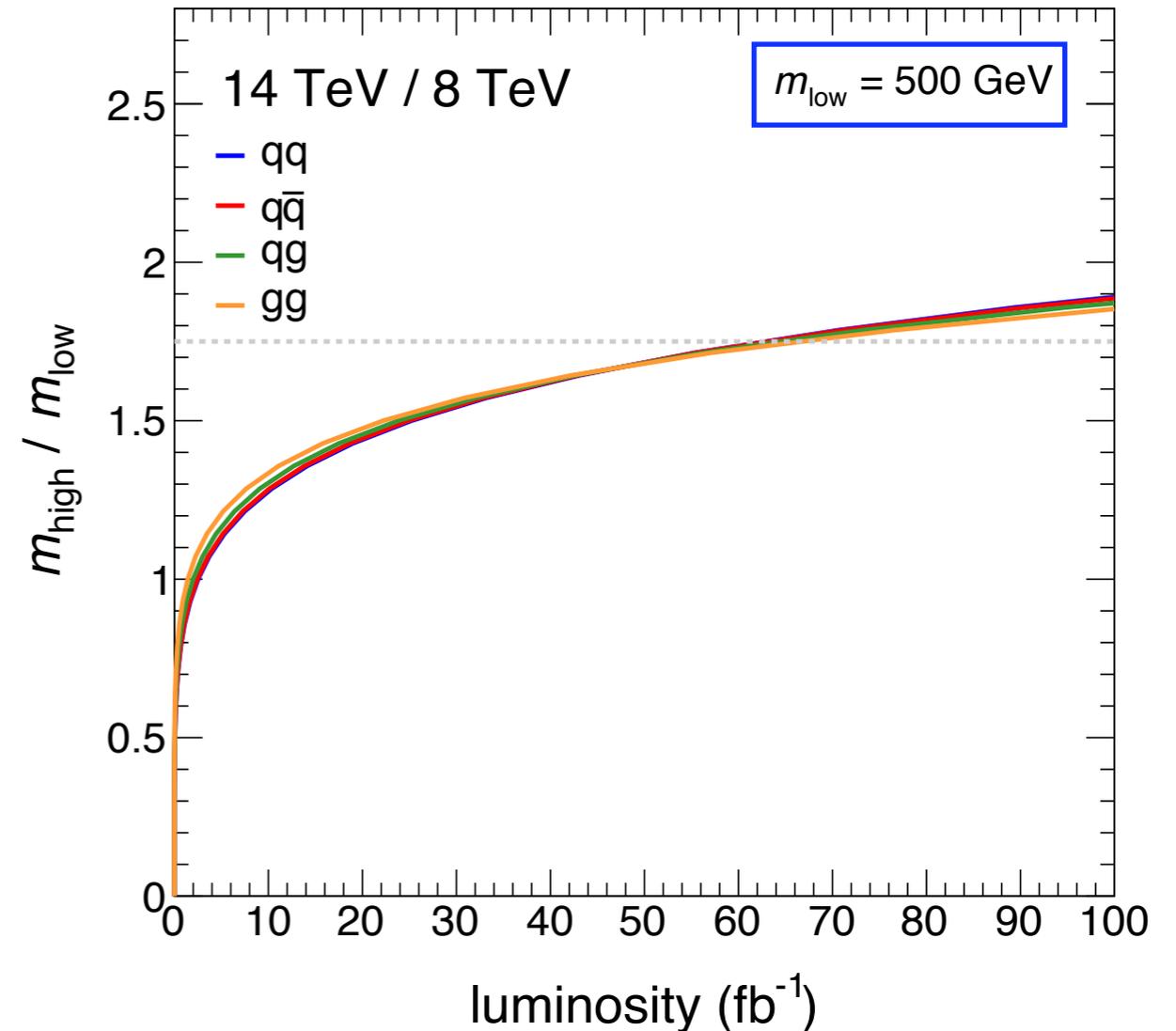
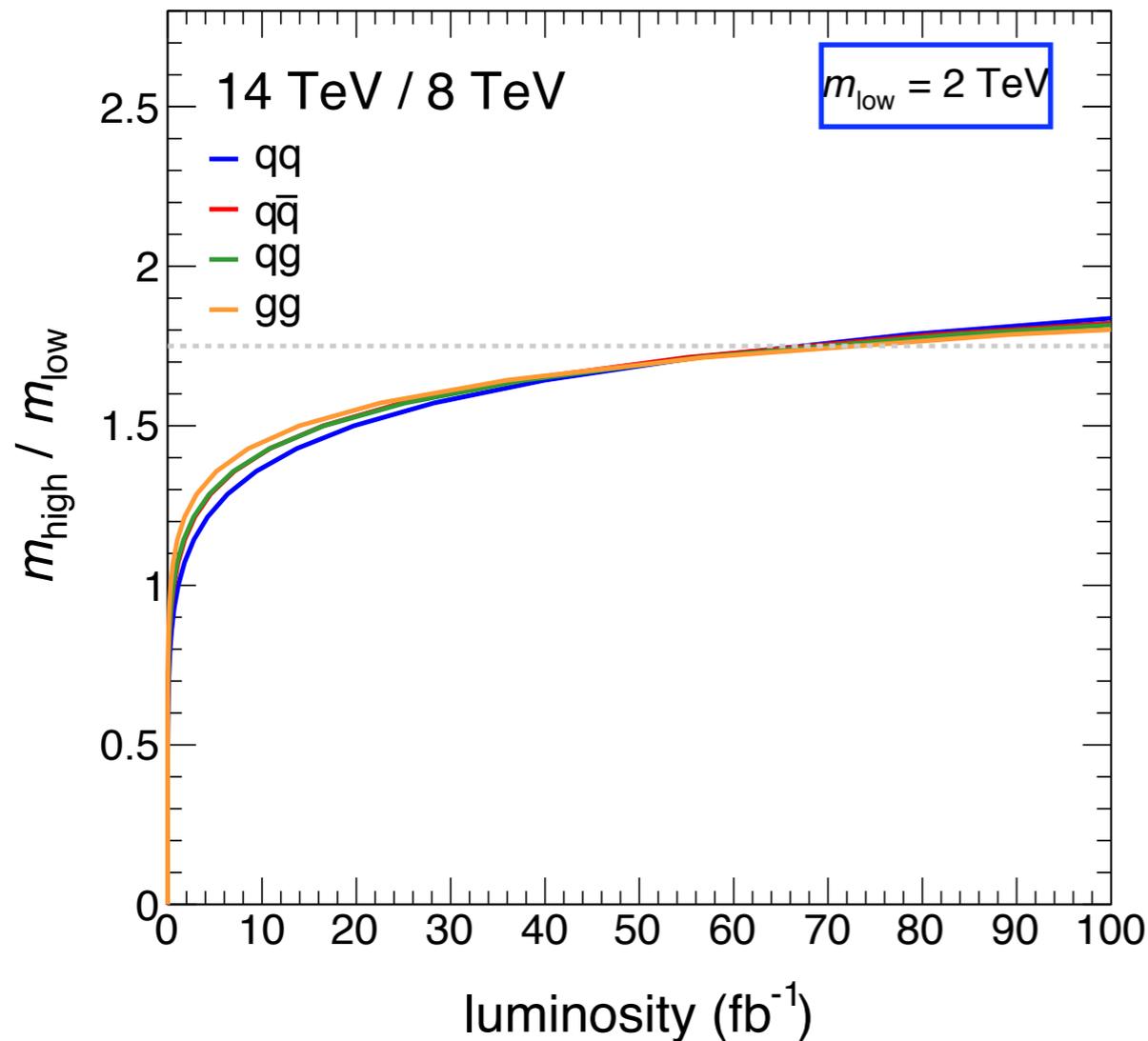
We have

$$\frac{M_2}{M_1} = \left(\frac{S_2}{S_1} \right)^{1/2} \left(\frac{S_1 \mathcal{L}_2}{S_2 \mathcal{L}_1} \right)^{\frac{1}{2a+2}} \quad \text{used} \quad \hat{s} \sim M^2 \rightarrow \tau \sim \frac{M^2}{S}$$

As data accumulates

Run I limit 2 TeV, e.g. pair of 1 TeV gluino.

500 GeV, e.g. pair of 250 GeV electroweak-ino



Rapid gain initial 10s fb^{-1} , slow improvements afterwards.

Reaching the “slow” phase after Moriond 2017

Phase space

- General phase space factor:

$$d\Pi_n = \Pi_f \left(\int \frac{d^3 p_f}{(2\pi)^3} \frac{1}{2E_f} \right) (2\pi)^4 \delta^{(4)}(p_a + p_b - \sum p_f)$$

- One additional final state particle

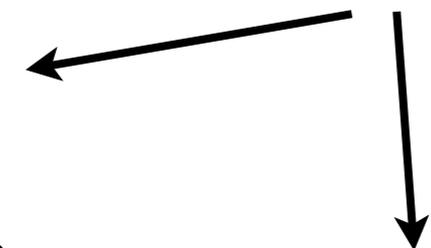
$$\sim \text{an additional factor of } \frac{1}{16\pi^2}$$

- For example

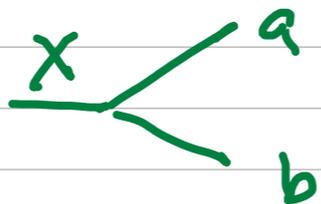
$$d\Pi_2 = \frac{1}{4\pi} \frac{1}{2} \lambda^{1/2}(1, m_1^2/\hat{s}, m_2^2/\hat{s}) d\dots$$

$$d\Pi_3 = \frac{1}{(4\pi)^3} \lambda^{1/2}(1, m_1^2/m_{23}^2, m_2^2/m_{23}^2) 2|\vec{p}_1| dE_1 d\dots$$

... variables $\subset \{0, 1\}$



2-body



$$X_\mu = a_\mu + b_\mu.$$

X may or may not be a particle.

$$\begin{aligned} d\pi_2 &= (2\pi)^4 \delta^{(4)}(X_\mu - a_\mu - b_\mu) \frac{d^3\vec{a}}{(2\pi)^3 2a_0} \frac{d^3\vec{b}}{(2\pi)^3 2b_0} \\ &= \frac{1}{8\pi} \lambda^{1/2} \left(1, \frac{a^2}{X^2}, \frac{b^2}{X^2} \right) \frac{d\Omega}{4\pi} = \frac{1}{4\pi} \frac{|\vec{P}_a|}{X} \frac{d\Omega}{4\pi} \end{aligned}$$

$$\lambda(x, y, z) = x^2 + y^2 + z^2 - 2xy - 2yz - 2xz$$

Assume: $a^2 = b^2 = m^2$ for simplicity

$$\lambda^{1/2} = \left(1 - \frac{4m^2}{X^2} \right)^{1/2}$$

Near threshold $X^2 = (2m + \delta)^2$

$$\lambda^{1/2} \approx \left(\frac{\delta}{2m} \right)^{1/2} + \dots$$

$$d\pi_2 \propto \delta^{1/2}$$

3 body.

$$Y_\mu = p_{1\mu} + p_{2\mu} + p_{3\mu}$$

$$d\pi_3 = (2\pi)^4 \delta^{(4)}(Y - p_1 - p_2 - p_3) \prod_{i=1}^3 \frac{d^3\vec{p}_i}{(2\pi)^3 2p_{i0}}$$

Decompose

$$Y = X + p_3 \quad X = p_1 + p_2$$

$$d\pi_3 = \frac{1}{2\pi} d\pi_2(Y \rightarrow X p_3) d\pi_2(X \rightarrow p_1, p_2) dX^2$$

Way above threshold, energy is the only dim-ful quantity

$$d\pi_3 \sim \frac{1}{16\pi^2} E^2 d\pi_2 \quad \text{suppressed w.r.t. 2-body}$$

Near threshold. $Y^2 \sim (3m + \delta)^2$

$$d\pi_2(Y \rightarrow X p_3) \sim d\pi_2(X \rightarrow p_1, p_2) \sim \delta^{1/2}$$

$$\int dX^2 \sim m\delta$$

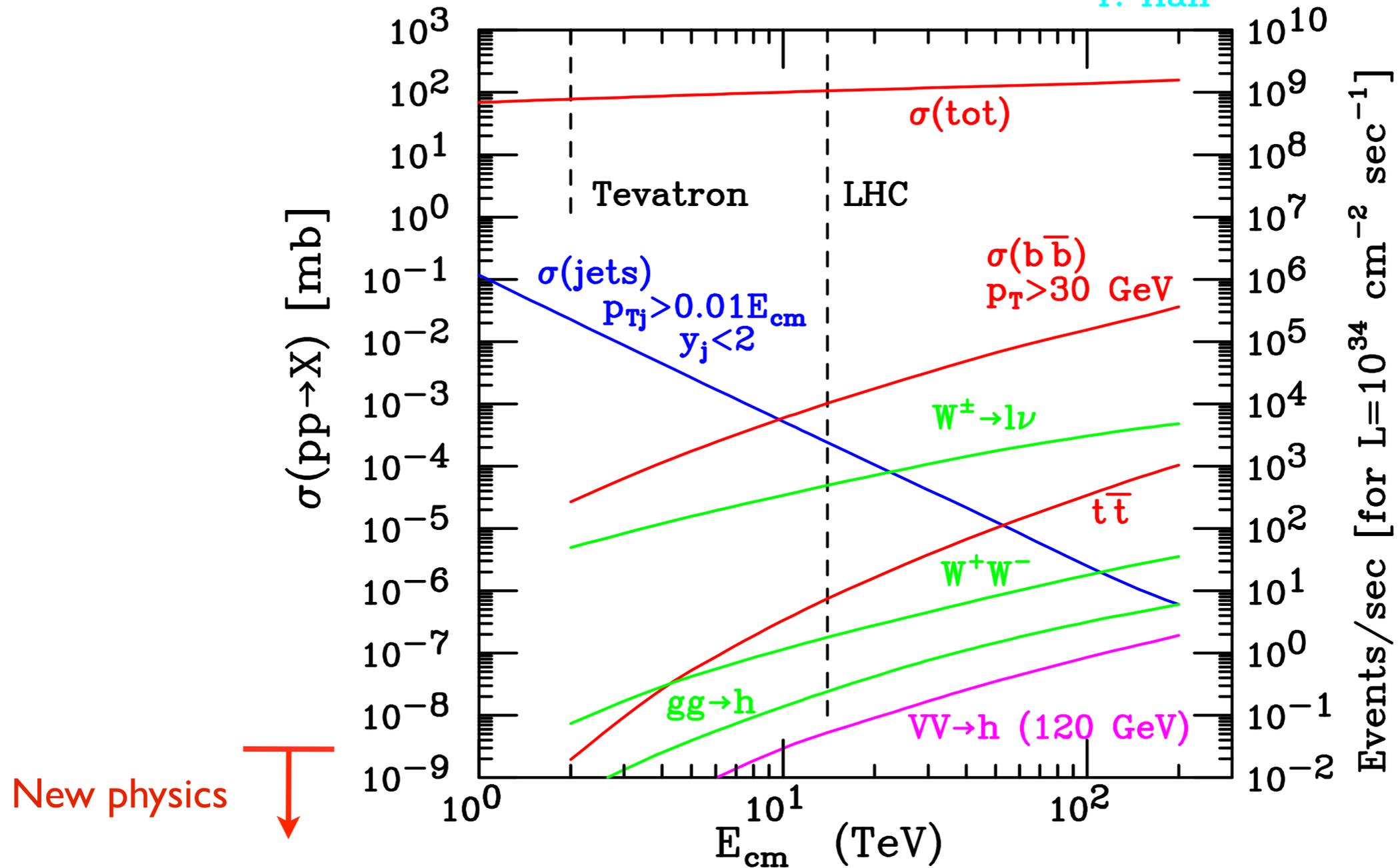
$$d\pi_3 \propto \delta^2 \quad \text{open slower than 2-body}$$

Rate also depends on

- Coupling constants
 - More final state particles, higher power of coupling constants.
 - QCD process dominates over weak processes.
- Singularities (enhancements) of matrix elements
 - Resonances.
 - Collinear and soft regime...

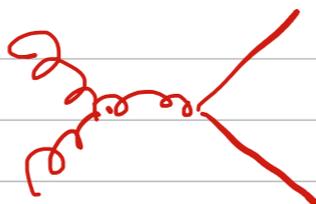
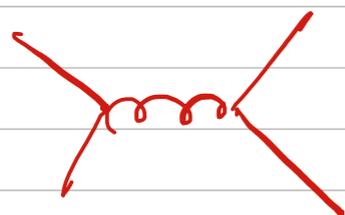
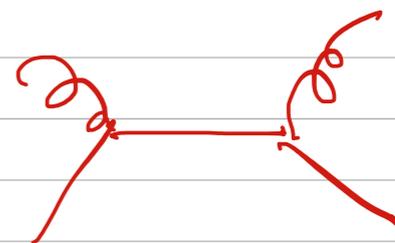
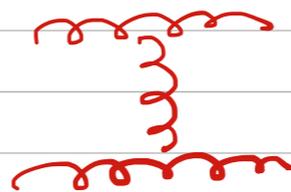
Understanding the rates

T. Han

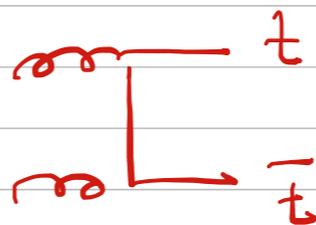
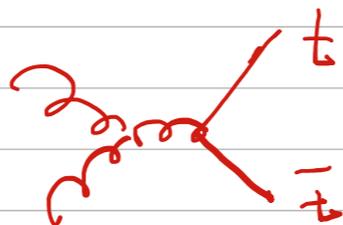


Example: considering $t\bar{t}$ vs W^+W^- ,
 The relevant factors are:
 top is twice as heavy as W (2 times higher threshold)
 α_s^2 vs α_w^2
 $t\bar{t}$ is gg dominated, W^+W^- is qqbar.

di jet



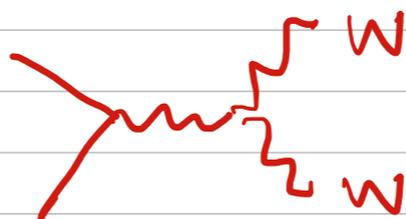
$t\bar{t}$



W



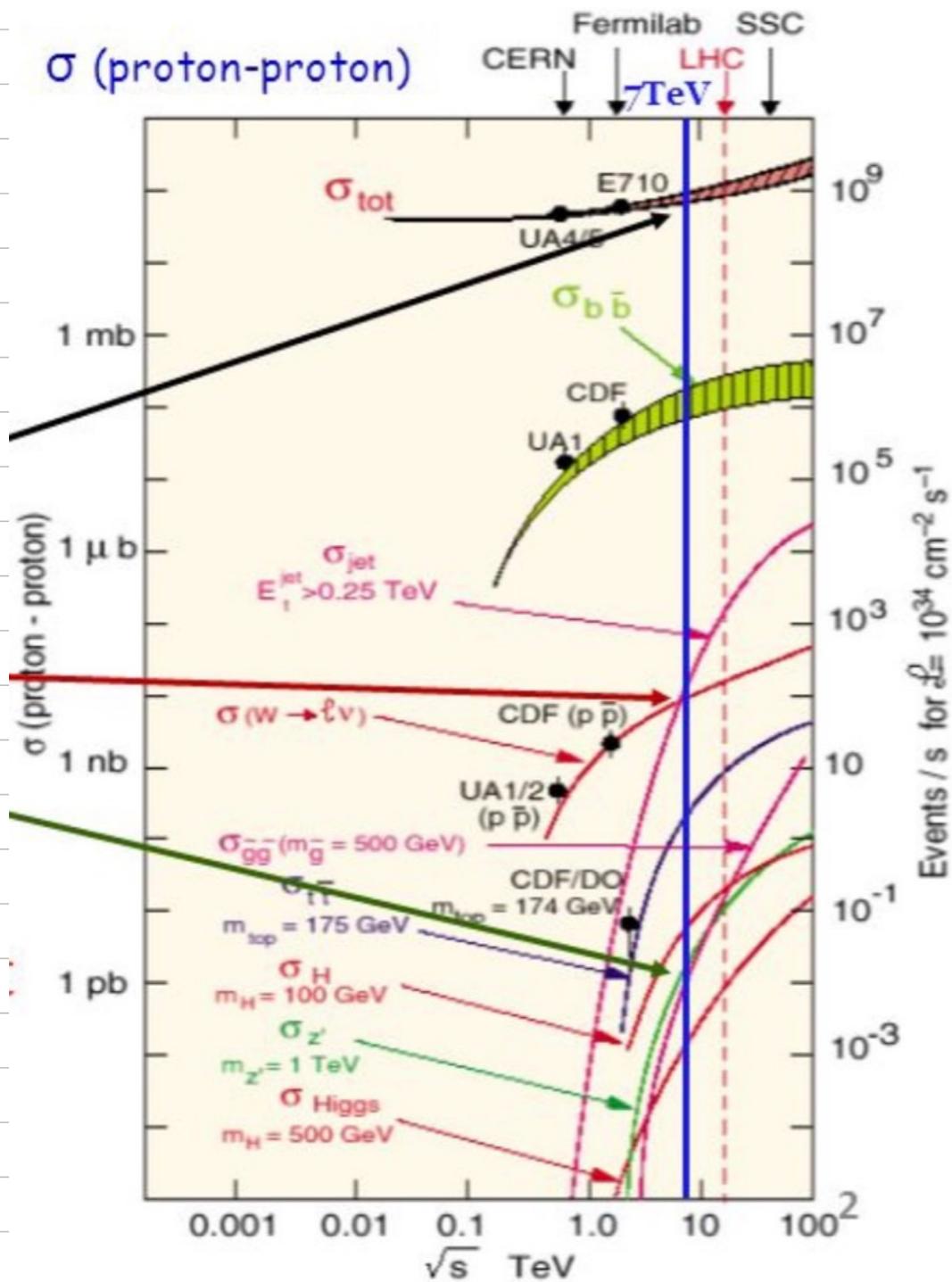
WW



h



PP → X



X:

$W \rightarrow \ell\nu$

20 nb

(W inclusive)

100 nb)

$Z \rightarrow \ell^+\ell^-$

2 nb

$t\bar{t}$

900 pb

h

20 pb

WW

100 pb

QCD di-jet

100 nb

$P_T > 250 \text{ GeV}$

Qualitative understanding of SM rates

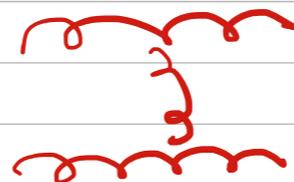
	$t\bar{t}$	W	
PDF	$gg \dots$	$q\bar{q}$	$gg(350) \lesssim q\bar{q}(160)$
coupling	α_s^2	α_w^2	$\alpha_s^2 \sim 10 \alpha_w^2$
mass threshold	350	160	$\sigma_{t\bar{t}} \sim \sigma_{WW}$

	W	h	
PDF	$q\bar{q}$	gg	$q\bar{q}(80) \sim \frac{1}{5} gg(125)$
coupling	α_w	$(\frac{1}{16\pi^2})^2 \alpha_s^2$	$\alpha_w \sim 3 \times 10^4 (\frac{1}{16\pi^2})^2 \alpha_s^2$
mass threshold	80	125	$\sigma_W \sim 5 \times 10^3 \sigma_h$

di-jet vs $t\bar{t}$

$$\sigma(\text{di-jet}, p_T^2 > 250) \sim 100 \sigma_{t\bar{t}}$$

- Many more diagrams for di-jet. $\mathcal{O}(10)$ enhancement
- Forward singularity in di-jet



etc.

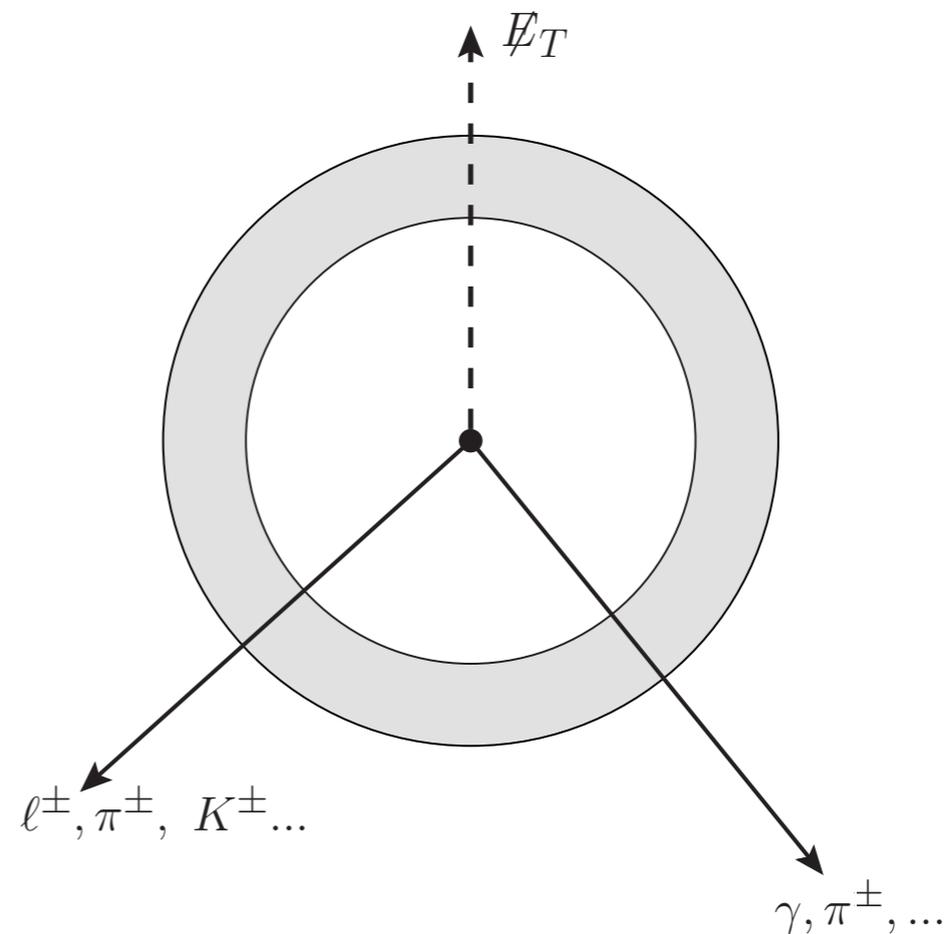
Why is it hard to discover TeV-scale new physics at the LHC

- p p collider, “prefers” to produce lighter states.
- Production rates scale roughly as $\sigma_{pp \rightarrow M} \sim \frac{1}{M^6}$
- TeV new physics $M_{\text{NP}} \sim 5 - 10 \times M_{\text{SM}(W,Z,t,\dots)}$
 - $\sigma_{\text{SM}} \geq 10^6 \times \sigma_{\text{NP}}$
- Dominated by QCD: A messy environment.
- Need:
 - Precise knowledge of the SM processes.
 - Anticipation of potential new physics states and their properties.

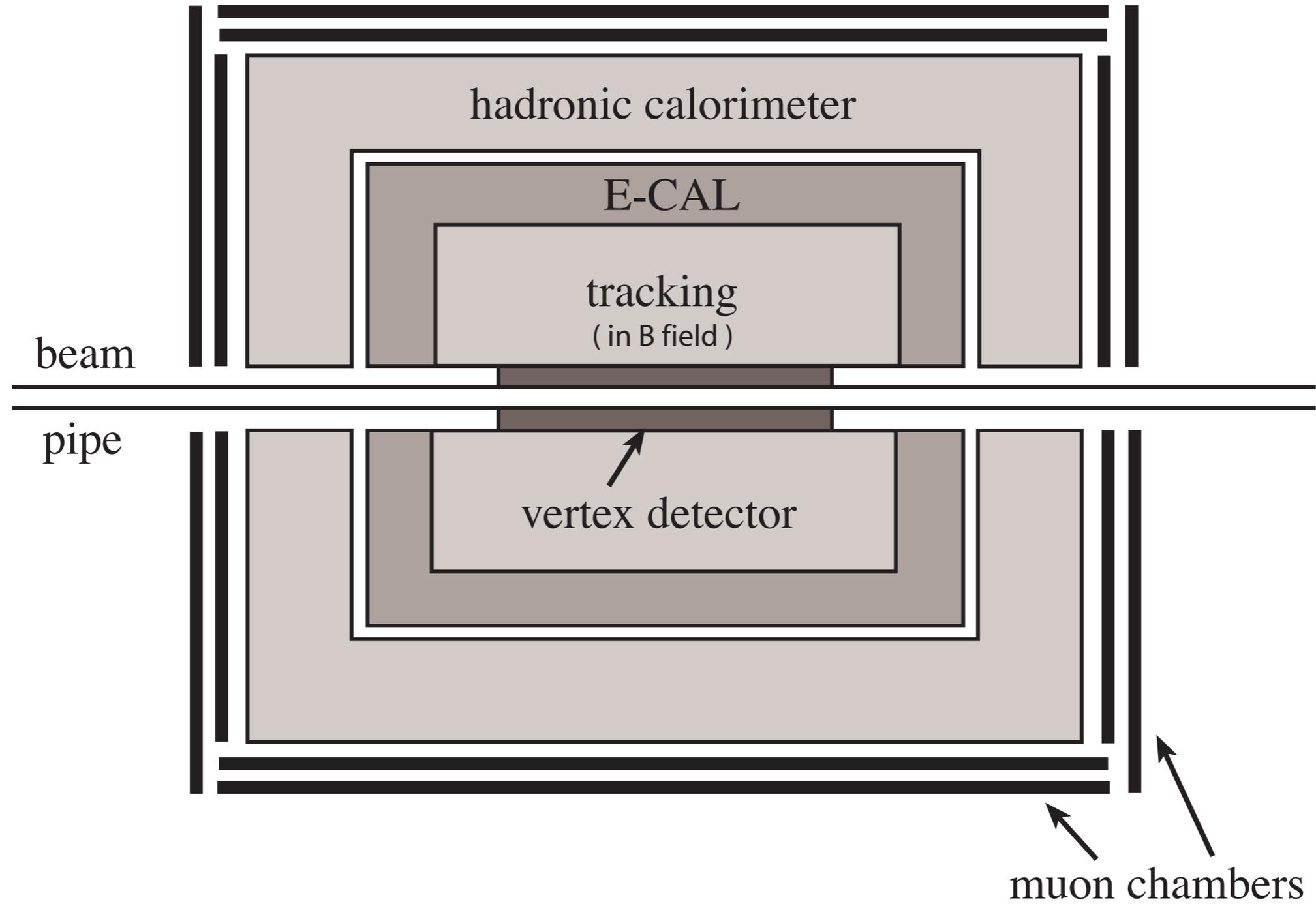
Being produced does not mean
we can see them!

Final state Objects

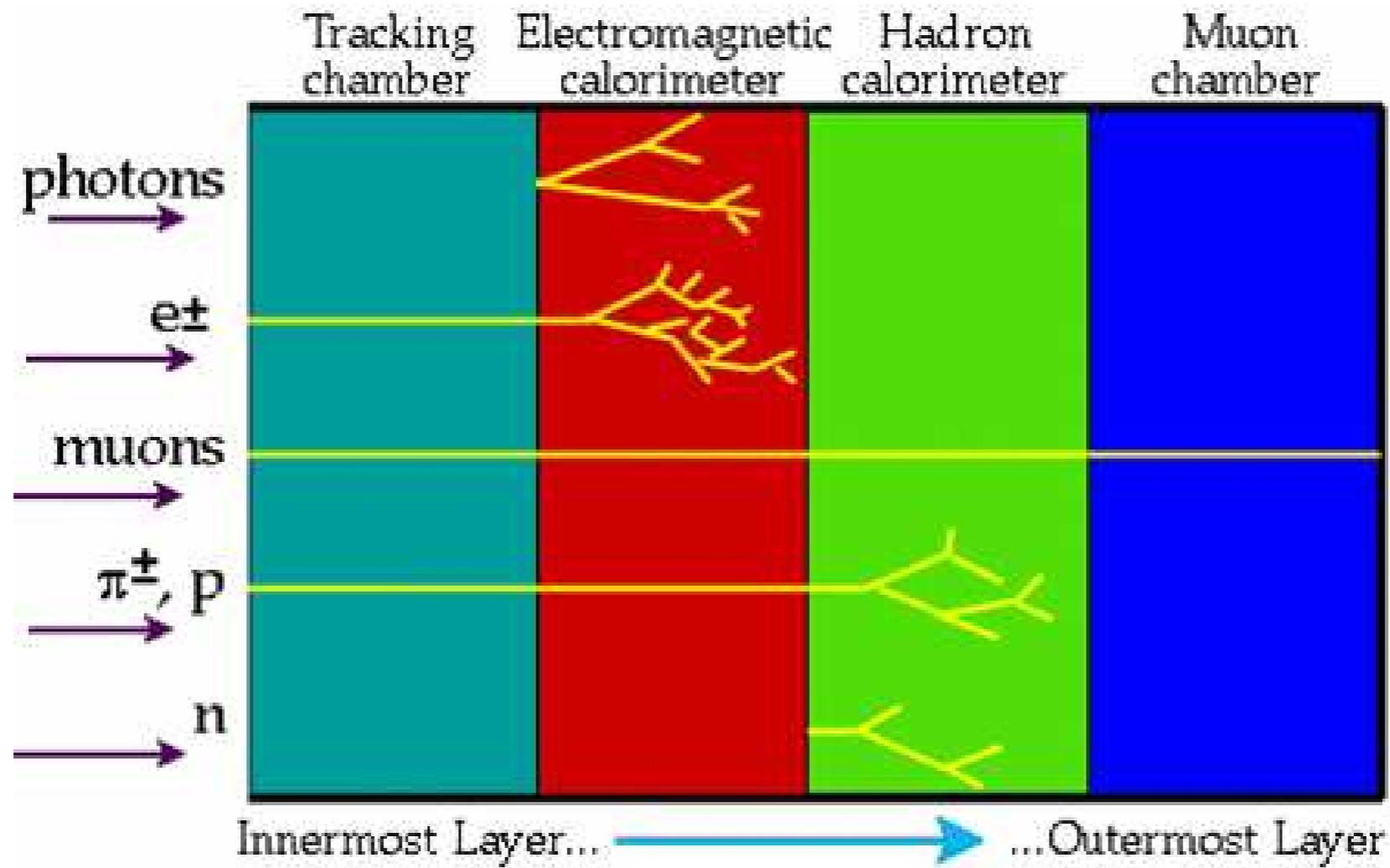
- Colored particles: cluster of hadronic energy, **jet**
- Leptons: **electron, muon**
- Photon
- Heavy flavor: **bottom (charm)**
- Missing energy (**MET**)



Modern detector (cartoon)



Identifying particles



From SM processes

- QCD: quark, gluon \longrightarrow jets
- QCD heavy flavor: b, c.
- Z: $Z \rightarrow (q\bar{q}, \ell^+\ell^-, \nu\bar{\nu}) \rightarrow$ jets, lepton pair, \cancel{E}_T
- W: $W^\pm \rightarrow (q\bar{q}', \ell^\pm\nu) \rightarrow$ jets, lepton + \cancel{E}_T
- Top: $t \rightarrow b + (W \rightarrow q\bar{q}' \text{ or } \bar{\ell}\nu)$
- Tau lepton: narrow jet(s), lepton.

SM Rates at 7 TeV:

- QCD di-jet: $p_T^j > 100 \text{ GeV}$, 300 nb

- Heavy flavor: $b\bar{b}$, $p_T^b > 100 \text{ GeV}$, 1 nb

- $W^{\pm} \dots$: $W^{\pm} \rightarrow \ell\nu$, 14 nb

$W^{\pm}(\rightarrow \ell\nu) + 1 \text{ jet}$, $p_T^j > 100 \text{ GeV}$, 70 pb

one lepton + jets + MET

$W^{\pm}(\rightarrow \ell\nu) + 2 \text{ jet}$, $p_T^j > 100 \text{ GeV}$, 2 pb

$W^{\pm}(\rightarrow \ell\nu) + 1 \text{ jet}$, $p_T^j > 200 \text{ GeV}$, 5 pb

- $Z + \dots$: $Z(\rightarrow \ell^+ \ell^-)$, 1.4 nb

di-lepton + jets

$Z(\rightarrow \ell^+ \ell^-) + 1 \text{ jet}$, $p_T^j > 100 \text{ GeV}$, 10 pb

New Physics: $\sim \text{pb}$

SM rates at 7 TeV

- **di-boson:** W^+W^- : 30 pb **di-lepton + MET, ~ 1.2 pb**
 $W^+W^- + 1 \text{ jet, } p_T^j > 100 \text{ GeV, } 2 \text{ pb}$
di-lepton+jet+MET ~ 0.1 pb
 W^+Z : 7 pb, W^-Z : 3.7 pb
tri-lepton + MET ~ 0.1 pb

- **top pair: 160 pb! Always has 6 objects.**

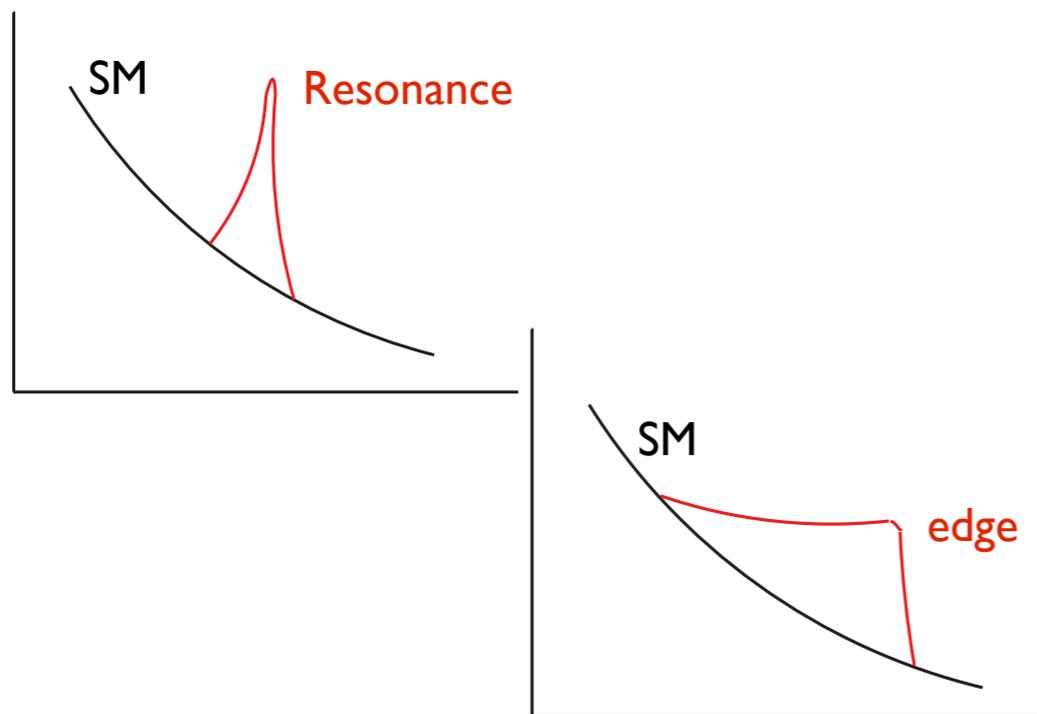
$$t\bar{t} \rightarrow bbW^+W^- \rightarrow bbjj\ell\nu, bb\ell\nu\ell\nu, bbjjjj$$

- **(MET+lepton+Jet 40%, Heavy flavor...)**
- **Looks like new physics, pair production of a massive particle followed by a decay cascade.**

Two possible ways of discovery:

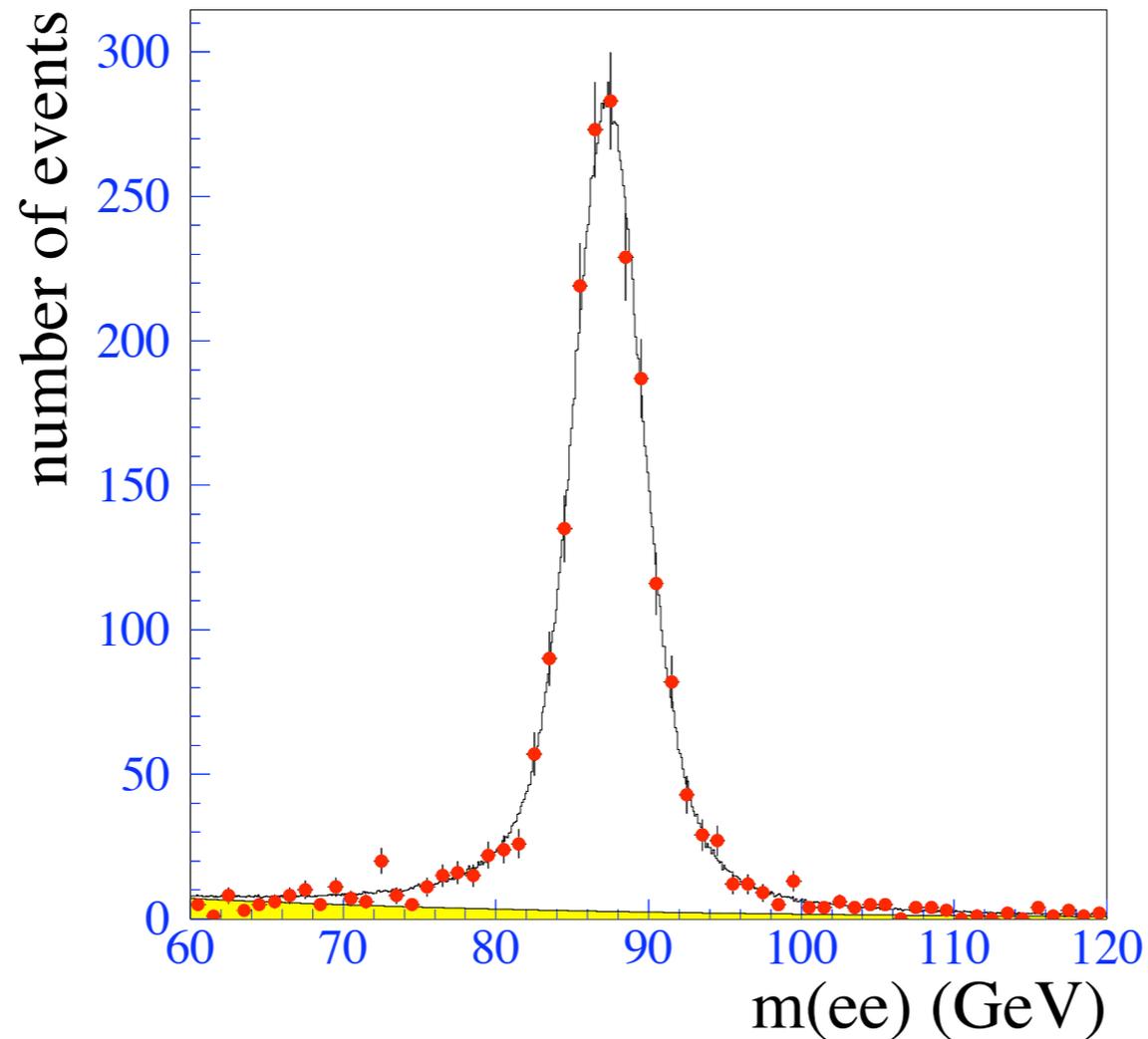
final state	rate estimate
begin with ≥ 2 hard jets	10^5 Hz
in addition	
hard jet	10^2 Hz
or $\cancel{E}_T \gtrsim 10^2$ GeV	$\sim 10^2$ Hz
or 1 lepton	10^2 Hz
or 2 lepton	1 Hz
or $2\ell = e^\pm + \mu^\pm$	10^{-4} Hz

- Rate: final states with more energetic (hard) objects, for example:
 $(\geq 2 \text{ jets}) + \cancel{E}_T$
 $(\geq 2 \text{ jets}) + (\geq 1\ell) + \cancel{E}_T$



- Special kinematical features, resonances, edges, ...

Resonance



$$pp \rightarrow Z^0 \rightarrow e^+e^-$$

$$\hat{s} = m_{ee}^2 = (p_{e_1} + p_{e_2})^2$$

Invariant mass (Lorentz inv.)

$$\frac{d\hat{\sigma}}{dm_{ee}^2 dp_{eT}^2} \propto \frac{\Gamma_Z M_Z}{(m_{ee}^2 - M_Z^2)^2 + \Gamma_Z^2 M_Z^2}$$



From matrix element: Breit-Wigner

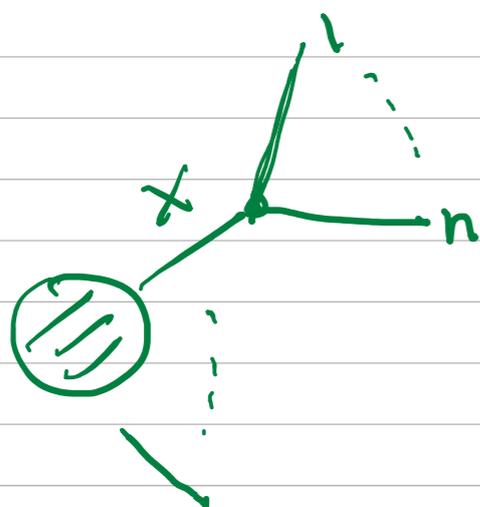
Narrow width approximation



$$|M|^2 \propto \frac{1}{(s_x - m_x^2)^2 + \Gamma_x^2 m_x^2} \approx \frac{\pi}{m_x \Gamma_x} \delta(s_x - m_x^2) \text{ if } \Gamma_x \ll m_x$$

(from $\lim_{\epsilon \rightarrow 0} \frac{\epsilon}{\epsilon^2 + x^2} = \pi \delta(x)$)

General final state

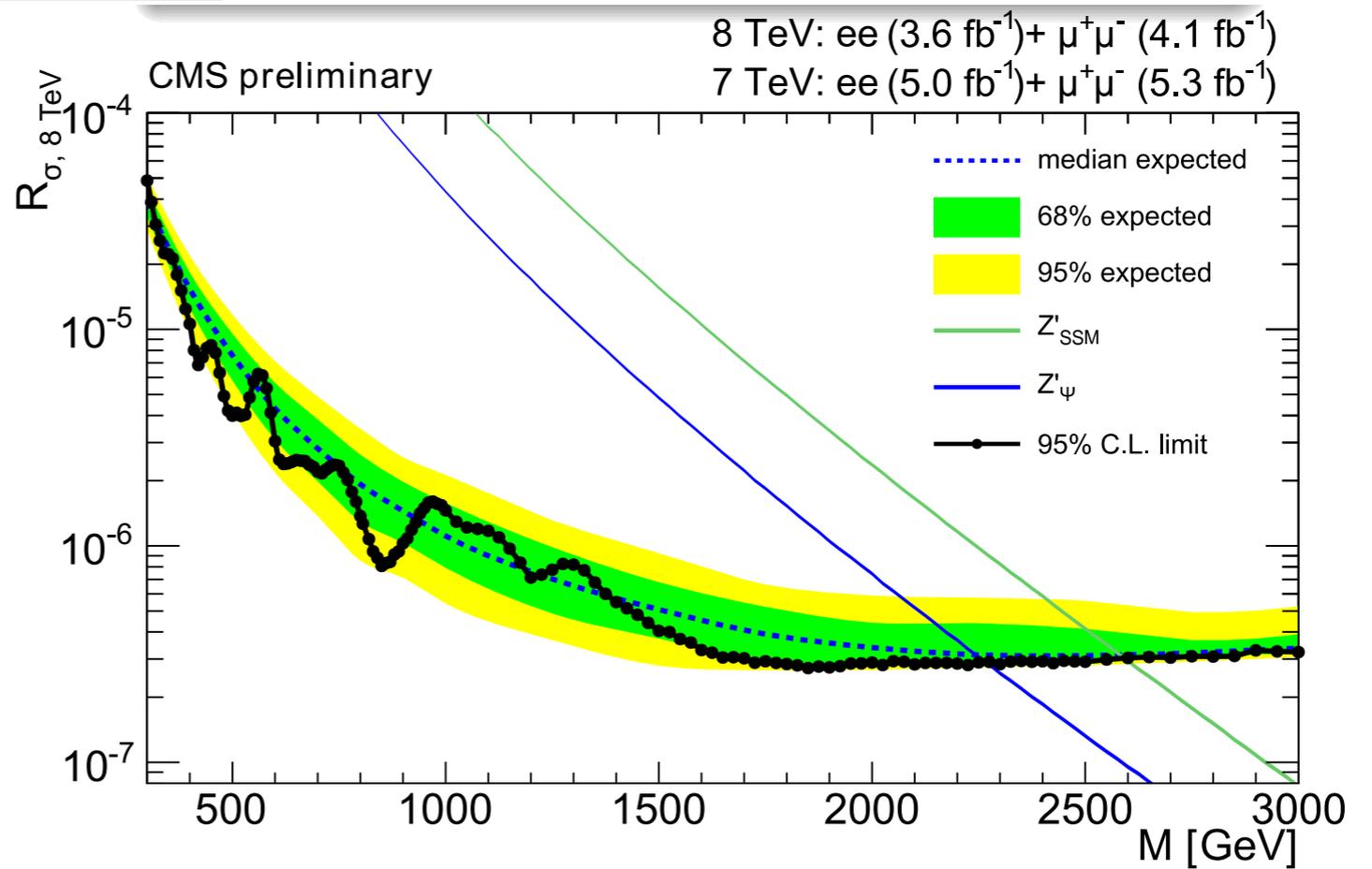
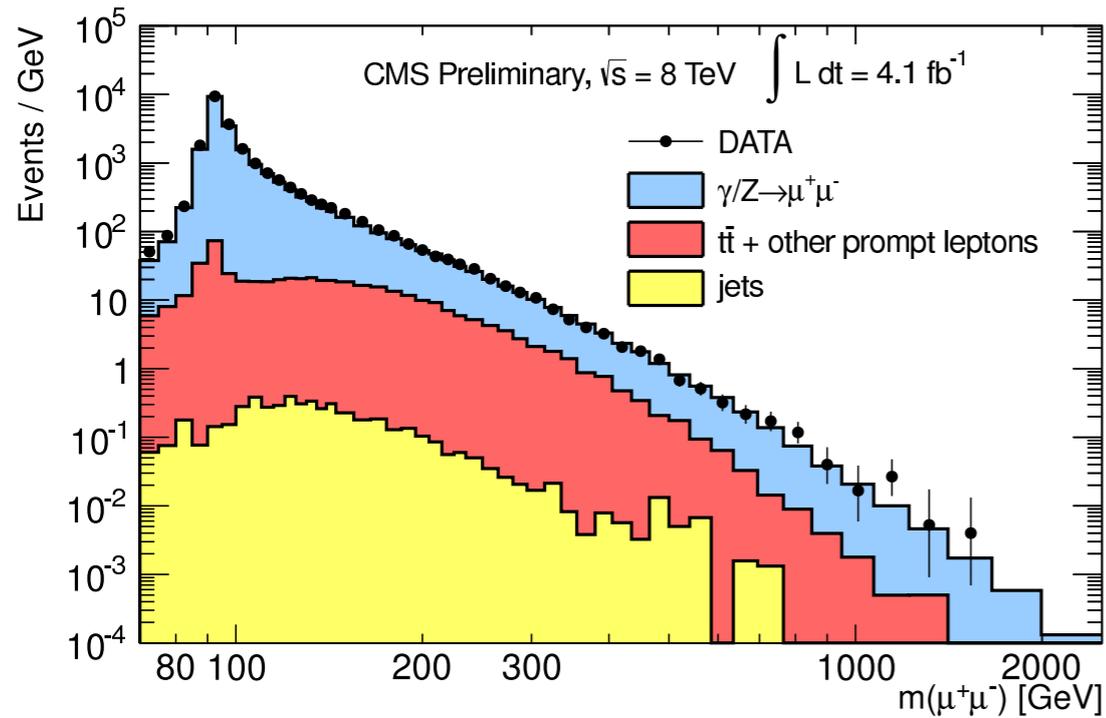


$$d\Gamma \propto ds_x \frac{1}{(s_x - m_x)^2 + \Gamma_x^2 m_x^2} d\Gamma (X \rightarrow 1, \dots, n)$$

NWA
 \Rightarrow

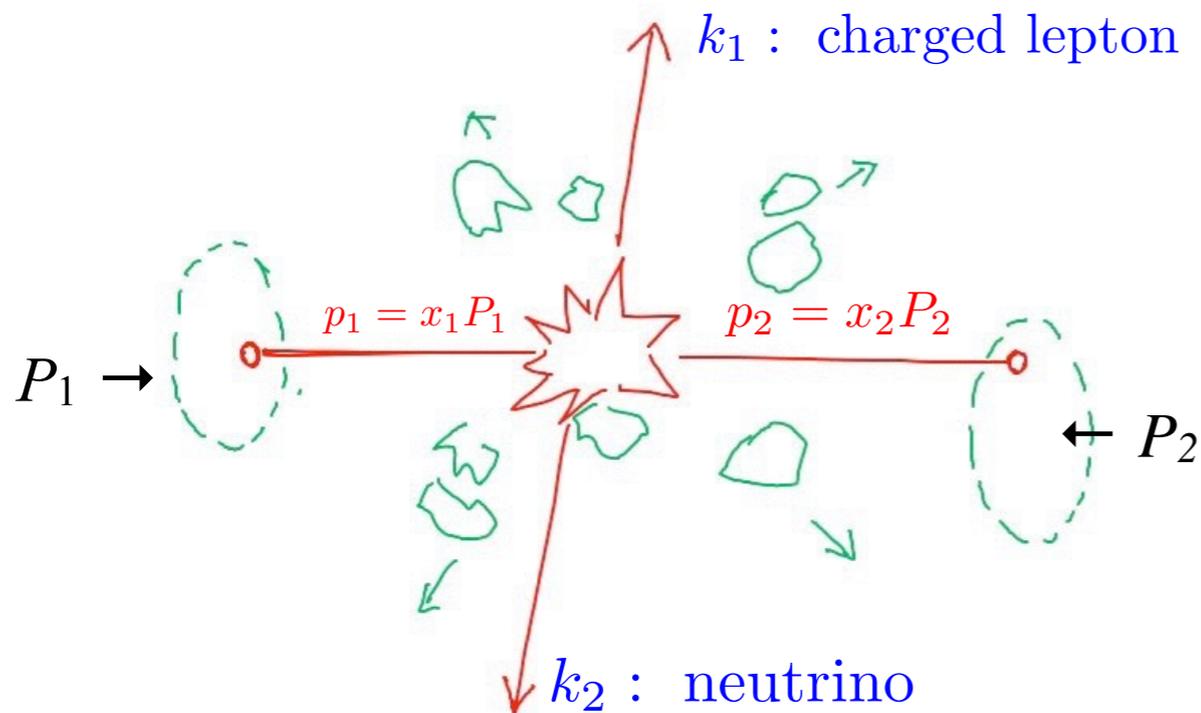
$$\frac{\Gamma (X \rightarrow 1, 2, \dots, n)}{\Gamma_x} \approx B_r (X \rightarrow 1, \dots, n)$$

New resonance, Z' , search



Almost a resonance:

- What if we don't observe all the final state particles.
For example, consider $W \rightarrow l\nu$
- Cannot form an interesting Lorentz invariant variable.
- At least can look for something invariant under boost along z-direction, e.g., transverse component



$$k_{1T}^2 = \frac{1}{4} \hat{s} \sin^2 \hat{\theta}$$

$\hat{\theta}$ in parton c.o.m frame

$$\frac{d}{dk_{1T}^2} = \frac{d}{d \cos \hat{\theta}} \frac{d \cos \hat{\theta}}{dk_{1T}^2}$$

$$\frac{d \cos \hat{\theta}}{dk_{1T}^2} = -\frac{2}{\hat{s}} \left[1 - \frac{4k_{1T}^2}{\hat{s}} \right]^{-1/2}$$

recall $\hat{s} = m_W^2$ k_{1T} distribution singular at $\frac{m_W}{2}$!

Jacobian peak

Transverse mass

$$m_{12}^2 = (E_e + E_\nu)^2 - (\vec{k}_{1T} + \vec{k}_{2T})^2 - (k_{1z} + k_{2z})^2$$

Define

$$\vec{p}_T = \vec{k}_{2T} \quad E_T = |\vec{k}_{2T}| \quad E_{eT} \equiv |\vec{k}_{1T}| = |\vec{k}_{2T}| \equiv E_{\nu T}$$

Define transverse mass

$$m_T^2 = (E_{eT} + E_{\nu T})^2 - (\vec{k}_{1T} + \vec{k}_{2T})^2$$

End point

$$m_{12}^2 > m_T^2 \quad \text{end point at } m_T = m_{12} = m_N$$

Proof for the end point.

$$m_{12}^2 = (E_e + E_\nu)^2 - (\vec{k}_{1T} + \vec{k}_{2T})^2 - (k_{1z} + k_{2z})^2$$

$$E_e = \sqrt{E_{eT}^2 + k_{1z}^2}$$

$$E_\nu = \sqrt{E_{\nu T}^2 + k_{2z}^2}$$

$$m_T^2 = (E_{eT} + E_{\nu T})^2 - (\vec{k}_{1T} + \vec{k}_{2T})^2$$

$$(E_e + E_\nu)^2 = E_{eT}^2 + E_{\nu T}^2 + k_{1z}^2 + k_{2z}^2 + 2\sqrt{E_{eT}^2 + k_{1z}^2}\sqrt{E_{\nu T}^2 + k_{2z}^2}$$

$$m_{12}^2 - m_T^2$$

$$= 2\sqrt{E_{eT}^2 + k_{1z}^2}\sqrt{E_{\nu T}^2 + k_{2z}^2} - 2k_{1z}k_{2z} - 2E_{eT}E_{\nu T} \geq 0$$



$$\textcircled{1} = \left(\sqrt{\quad}\sqrt{\quad}\right)^2 = E_{eT}^2 E_{\nu T}^2 + k_{1z}^2 k_{2z}^2 + E_{eT} k_{2z}^2 + E_{\nu T} k_{1z}^2$$

$$\textcircled{2} = \left(k_{1z}k_{2z} + E_{eT}E_{\nu T}\right)^2 = E_{eT}^2 E_{\nu T}^2 + k_{1z}^2 k_{2z}^2 + 2k_{1z}k_{2z}E_{eT}E_{\nu T}$$

$$\textcircled{1} - \textcircled{2} = E_{eT}^2 k_{2z}^2 + E_{\nu T}^2 k_{1z}^2 - 2k_{1z}k_{2z}E_{eT}E_{\nu T}$$

$$= \left(E_{eT}k_{2z} - E_{\nu T}k_{1z}\right)^2 \geq 0$$

Jacobian peak in m_T

If W produced without transverse boost.

$$m_T = 2|k_{1T}| = 2|k_{2T}|$$

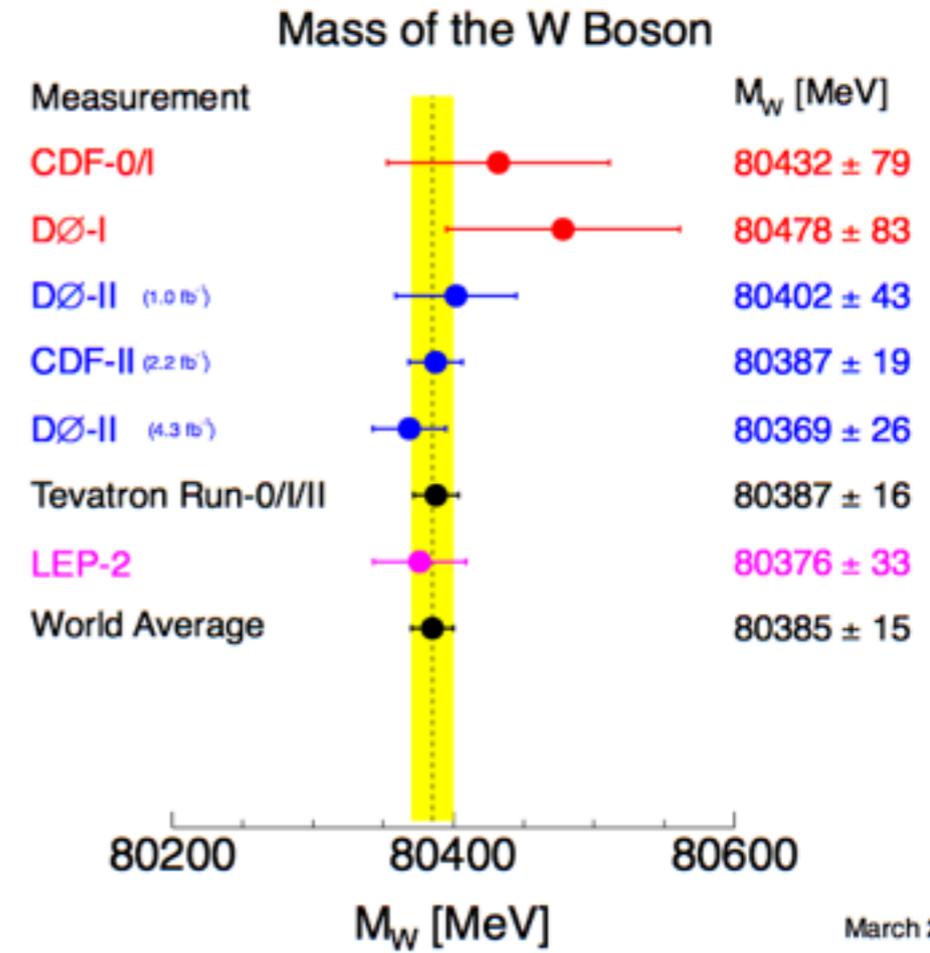
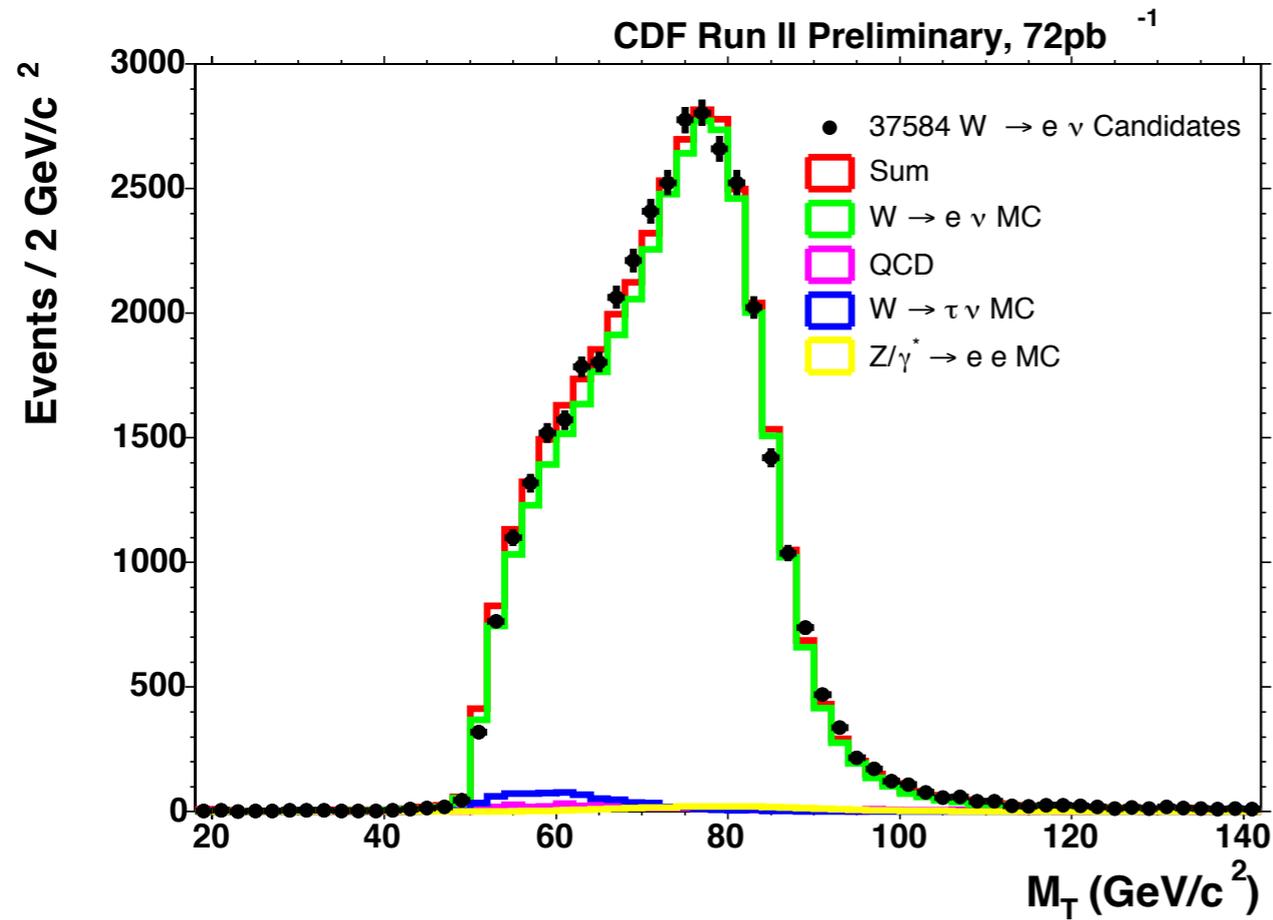
$$\frac{d}{dm_T^2} = \frac{1}{4} \frac{d}{dk_{iT}^2} \rightarrow \text{Jacobian peak at } m_T^2 = m_W^2$$

$$\frac{d\hat{\sigma}}{dm_T^2} \sim \frac{1}{4\pi} \frac{(G_F m_W)^2}{2} \frac{1}{(\hat{s} - m_W^2)^2 + (\Gamma_W m_W)^2} \frac{2 - m_T^2/\hat{s}}{(1 - m_T^2/\hat{s})^{1/2}}$$

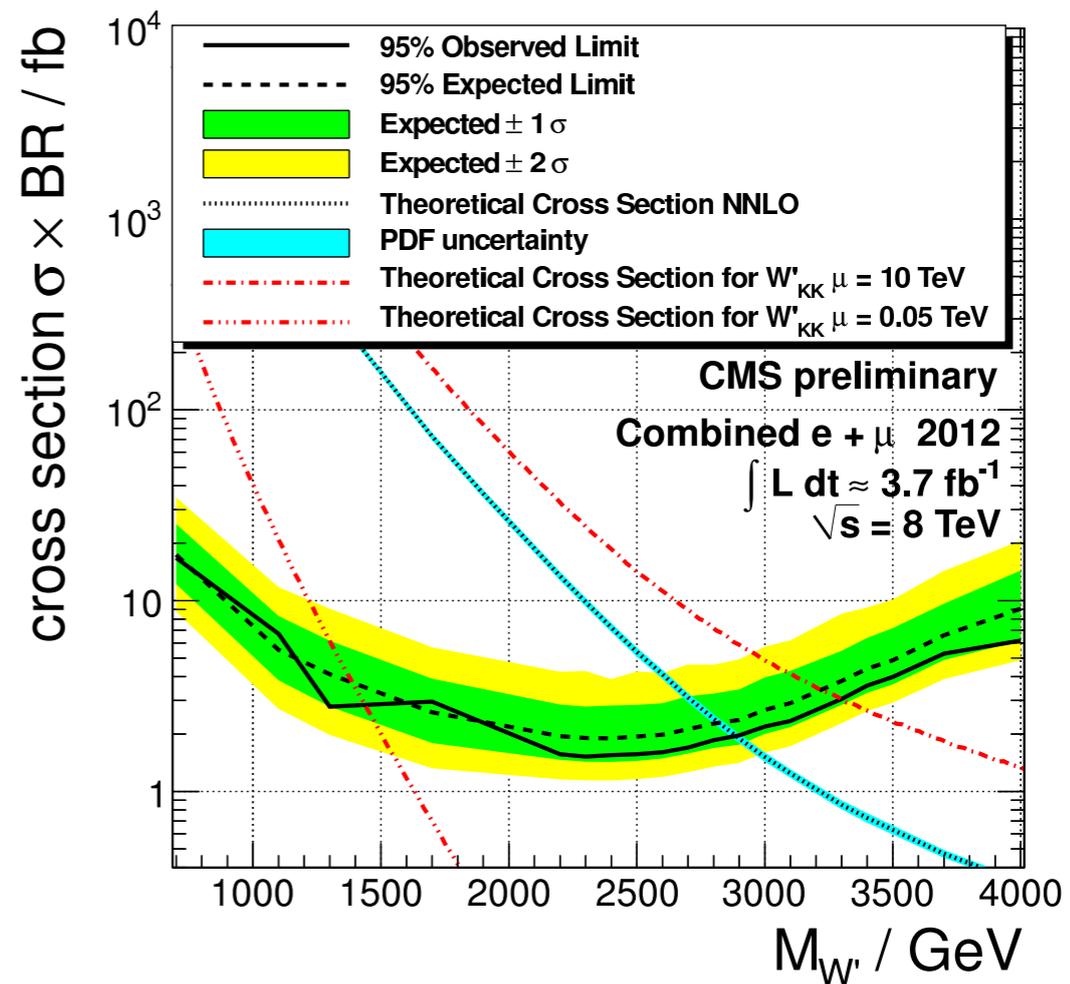
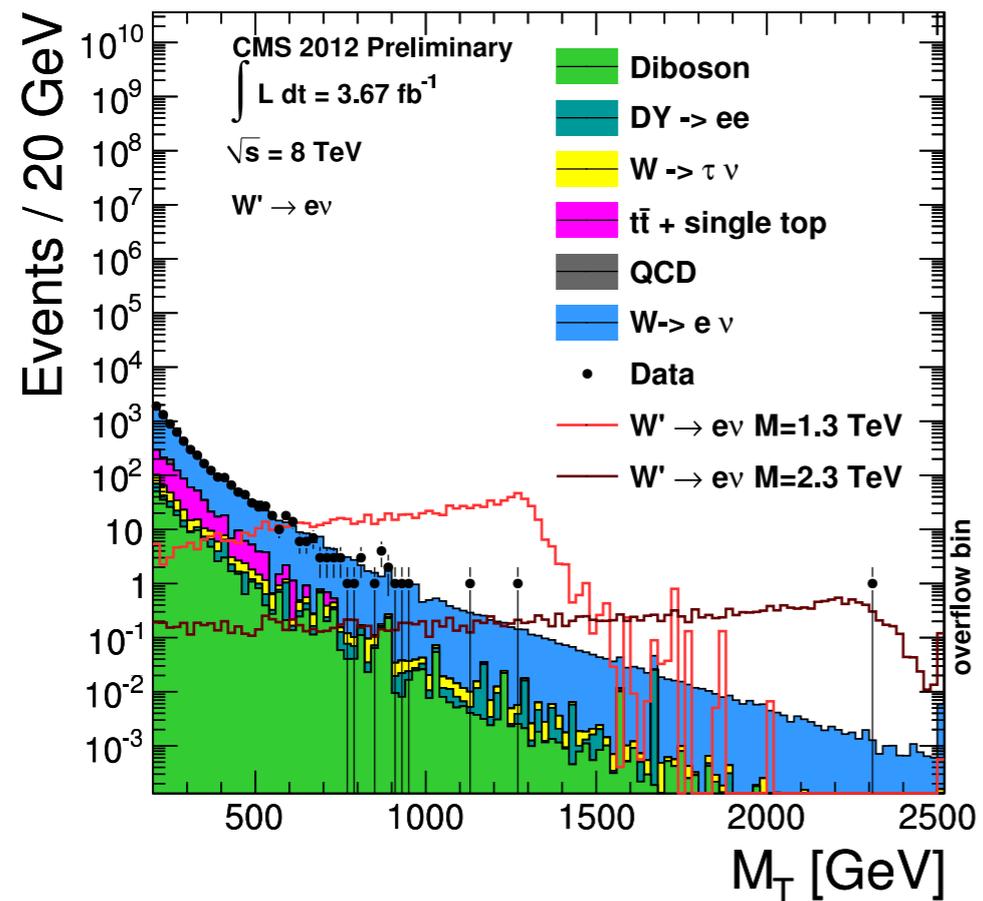
Position of Jacobian peak smeared by width, resolution

Shape of Jacobian peak changed by transverse boost.

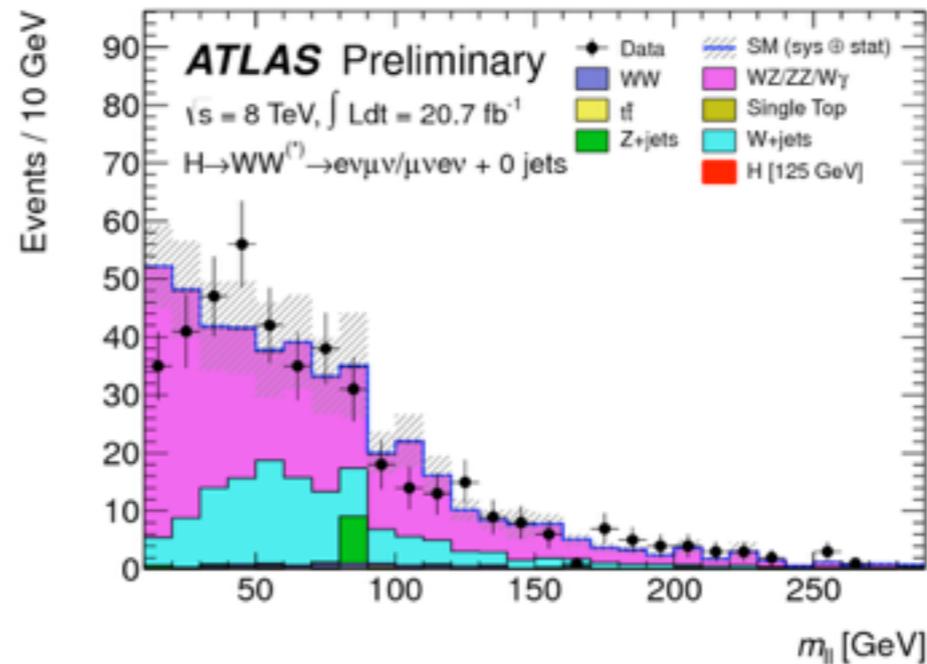
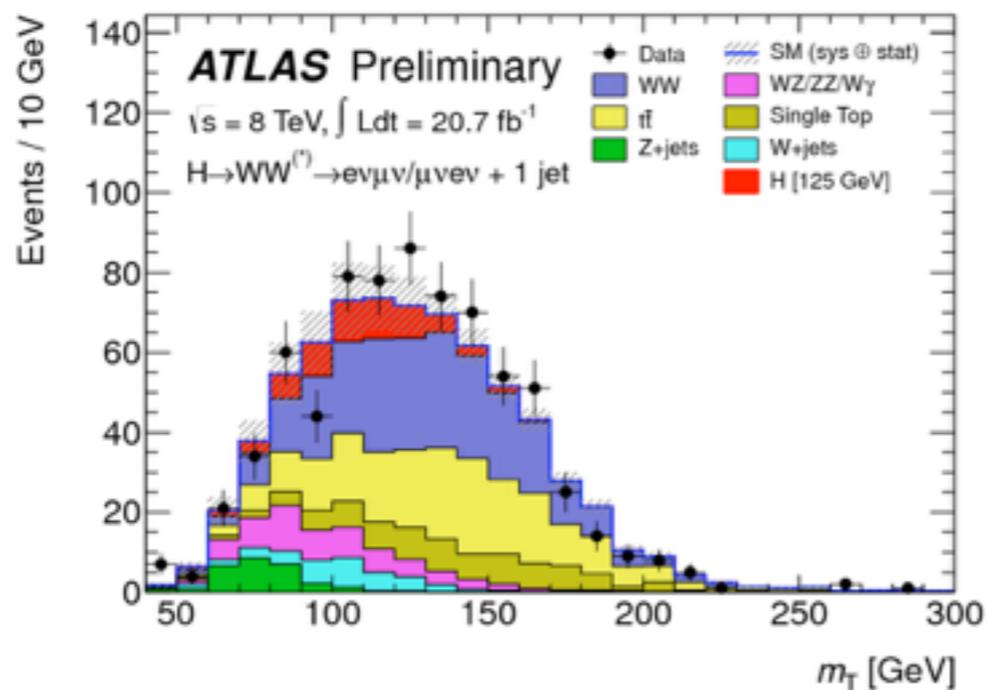
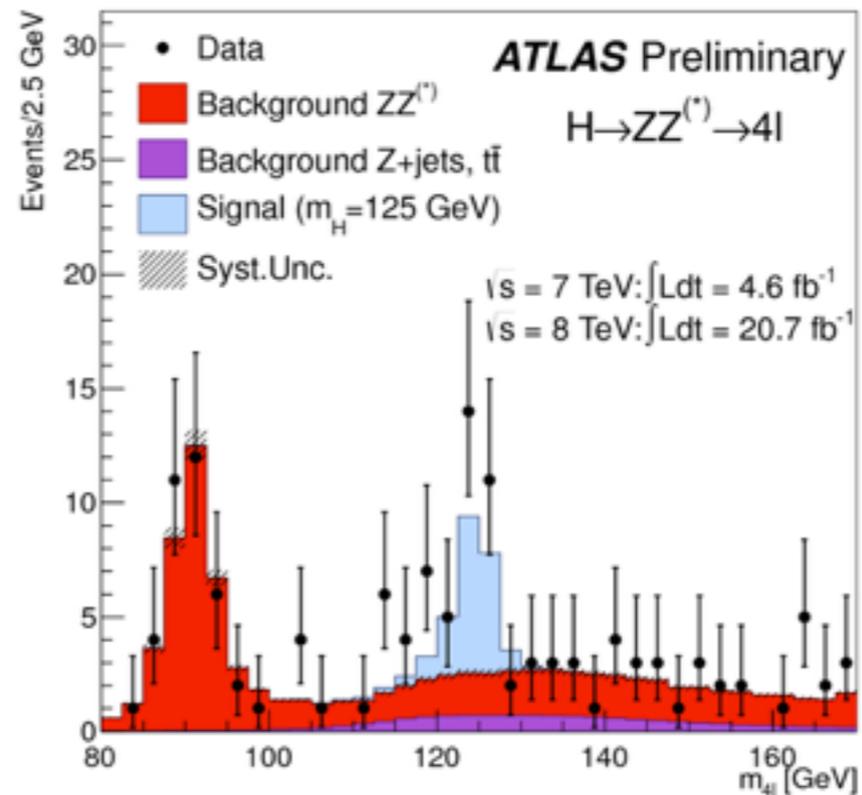
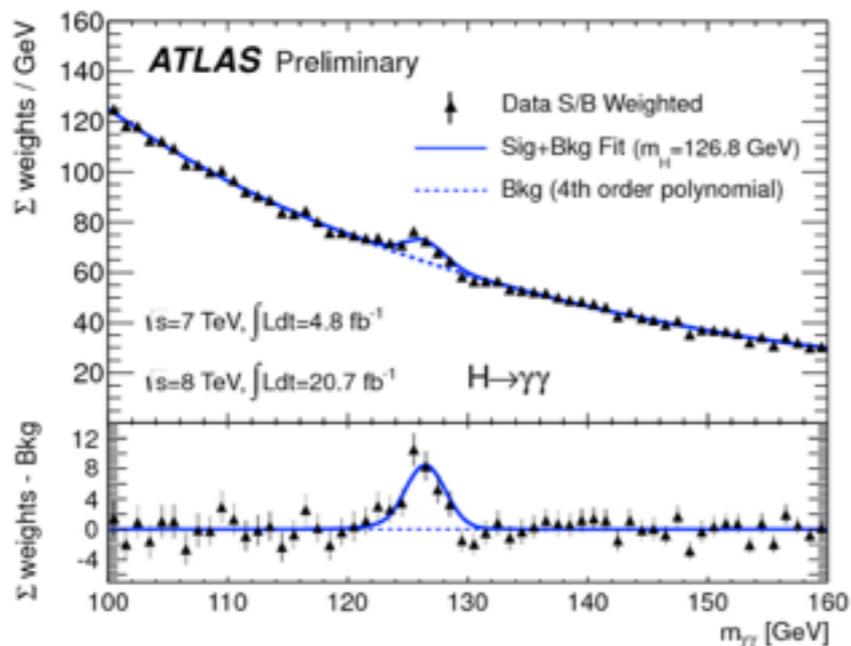
Measuring the W mass



W' search



Seeing Higgs



Complicated New physics signals

Partners:

New physics states with similar interactions to those of the Standard Model particles, such as the superpartners in Supersymmetry.

TeV Supersymmetry (SUSY)

- Supersymmetry. $|\text{boson}\rangle \Leftrightarrow |\text{fermion}\rangle$
- An extension of spacetime symmetry.
- New states: “Partners”

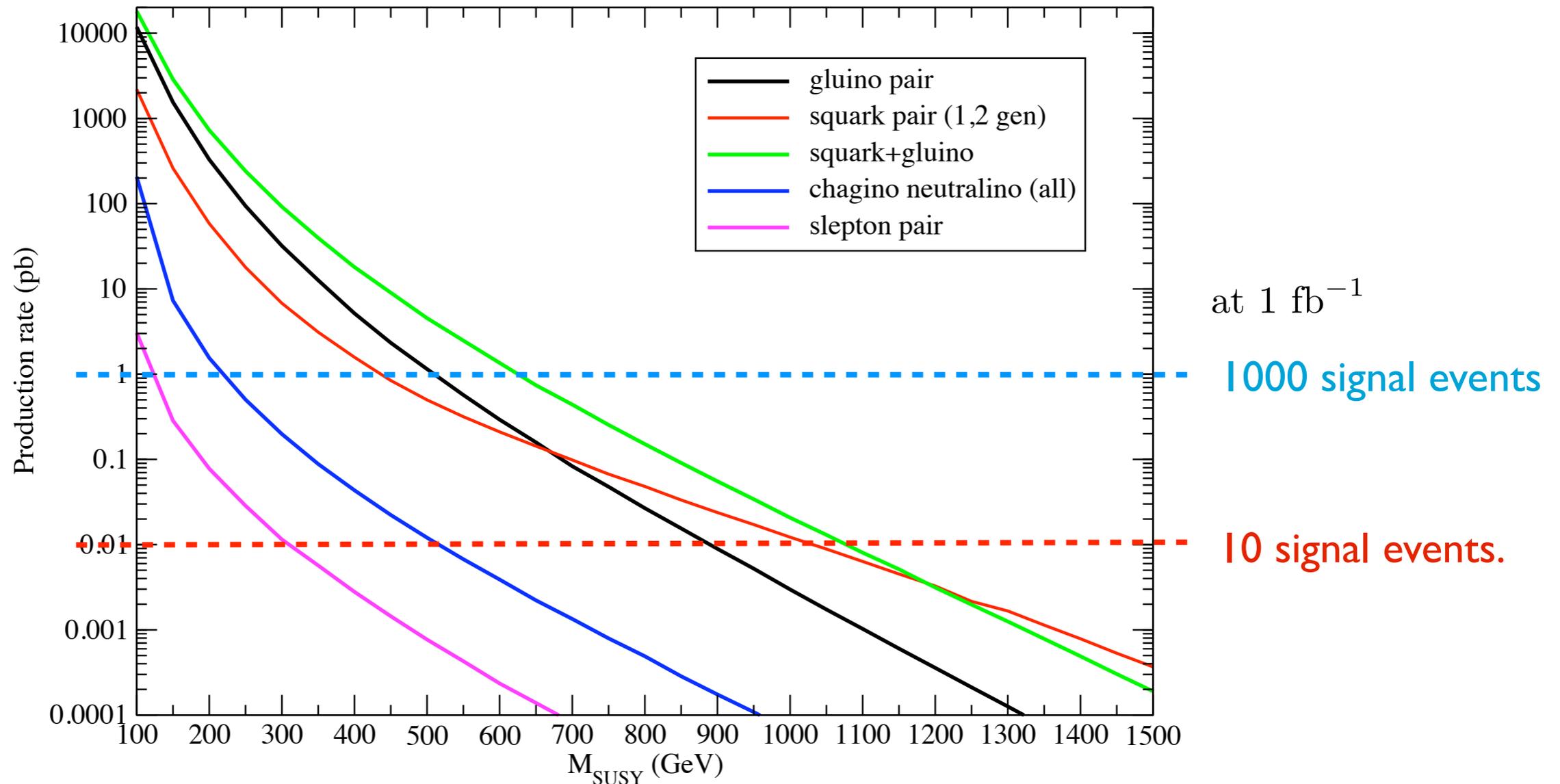
	spin		spin
gluon, g	1	gluino: \tilde{g}	1/2
W^\pm, Z	1	gaugino: \tilde{W}^\pm, \tilde{Z}	1/2
quark: q	1/2	squark: \tilde{q}	0
...		...	
SM		(super)partner	

- Couplings relate to SM interactions via supersymmetry.
 - \sim same strength.

Production.

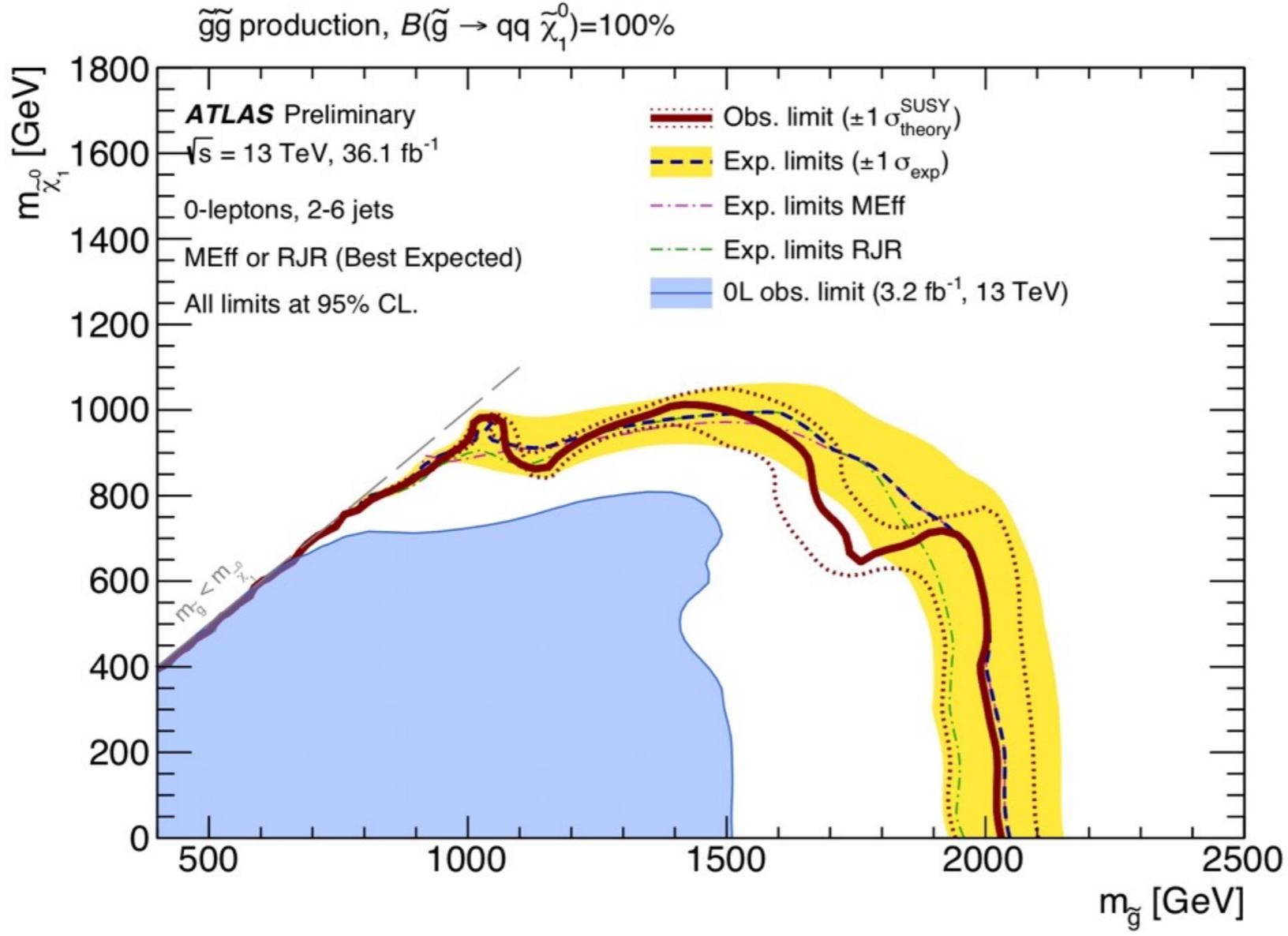
SUSY production rates at 7 TeV

Scale the horizontal axis by a factor of 2 for $E_{cm} = 14$ TeV



Dominated by the production of colored states.

Similar pattern for other scenarios. Overall rates scaled by spin factors.



Qualitative understanding of gluino reach.

$$\sigma (m_{\text{gluino}} = 2 \text{ TeV}) \sim 1 \text{ fb}$$

Main signal: jets + MET

SM background:

jets + $Z \rightarrow \nu\nu$ - QCD dijet ($P_T^2 > 250$) 100 nb

- scaling PDF from 500 GeV \rightarrow 4 TeV gives
a factor of 10^{-3}

- Adding a Z $10^{-2} - 10^{-3}$

- Adding one or two more jets $10^{-2} - 10^{-3}$

\rightarrow fb-ish

jet + $W \rightarrow e\nu$ - similar. - $\sigma_W \sim O(10) \sigma_Z$

- But need to miss lepton. $\sim O(10^{-1})$

$t\bar{t}$ - PDF from $t\bar{t}$ threshold to 4 TeV
gives a factor of $10^{-5} - 10^{-6}$

- MET from $W \rightarrow l\nu$, need to hide lepton.

\sim another factor of 10 (also perhaps b-veto)

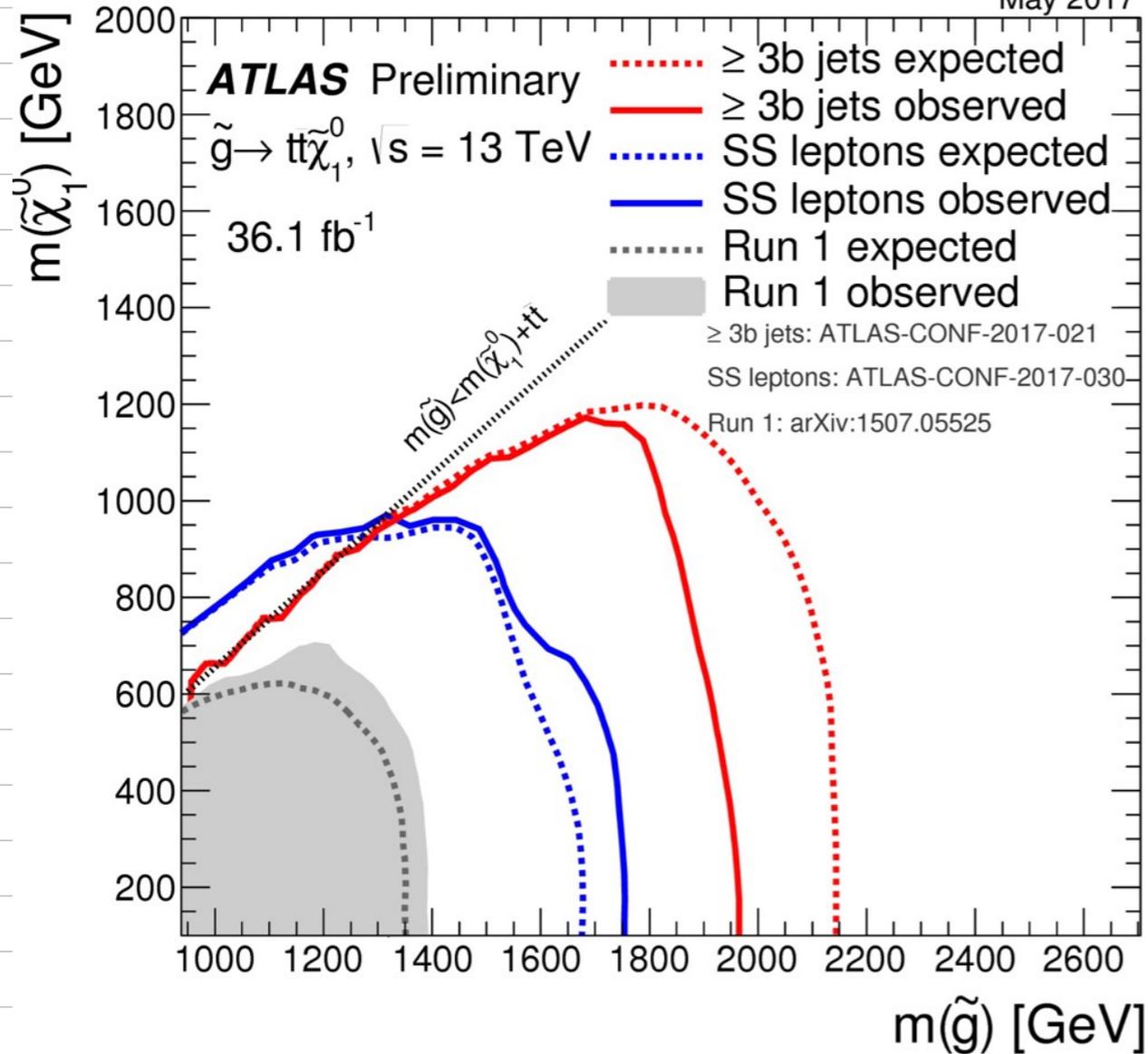
\rightarrow fb-ish.

- Which channel dominant depends on cuts.

- For $M_{\text{gluino}} > 2\text{TeV}$, background falls slower
(e.g., jets + Z from $q\bar{q}$).

Also, signal drops very fast. "run out of rate"

May 2017



Reach in multi-bjet channel.

$t\bar{t} + b_{jet}$ background.

Similar argument as the
gluino $\rightarrow \tilde{\delta}\tilde{\delta} + Met$ case.

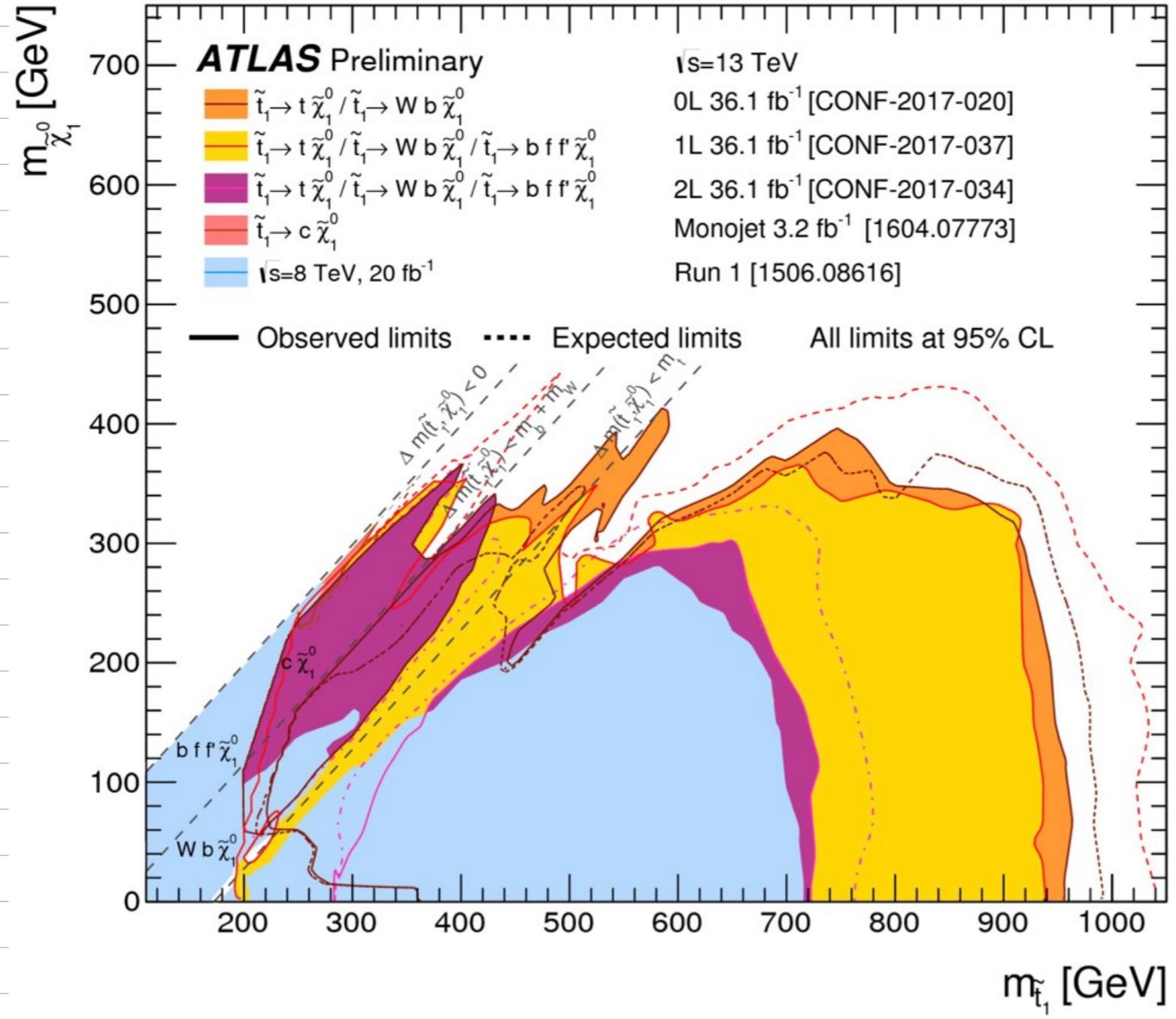
SSDL channel.

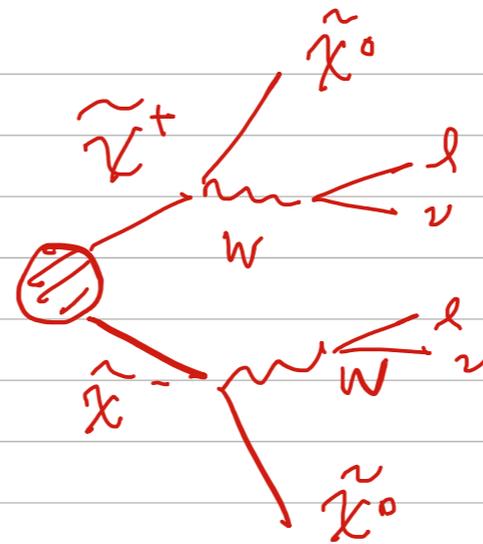
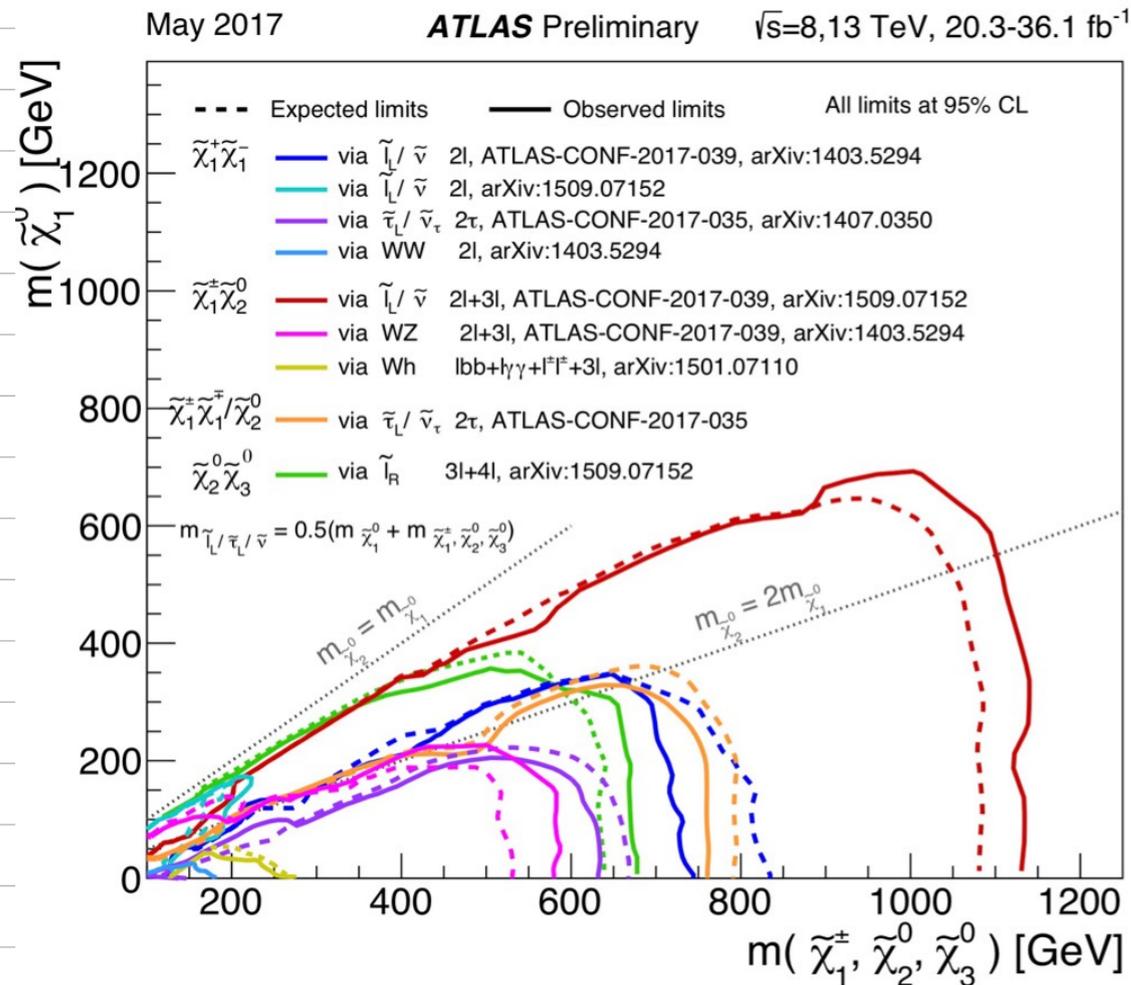
Rate smaller by about
a factor of 10

Reach weaker by 50%.

Cautious: reach in SSDL more "fool-proof"
multi-jet channel need very good modeling
of background

\tilde{t}_1, \tilde{t}_1 production, $\tilde{t}_1 \rightarrow b f f \tilde{\chi}_1^0$ / $\tilde{t}_1 \rightarrow c \tilde{\chi}_1^0$ / $\tilde{t}_1 \rightarrow W b \tilde{\chi}_1^0$ / $\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0$ Status: May 2017





WW energy $\sim 500 \text{ GeV}$

Production rate for 600 GeV chargino $\sim 1 \text{ pb}$

SM background



Rate for $W^+ W^-$ on threshold $\sim 100 \text{ pb}$

Scaling w/ PDF \rightarrow a factor of 10^{-2}

for WW energy about 500 GeV

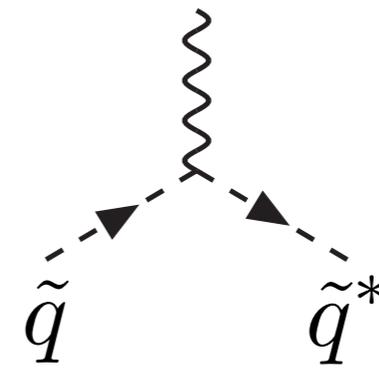
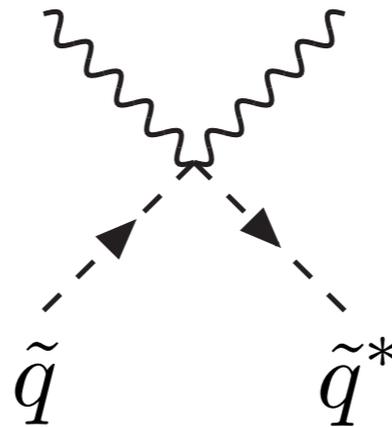
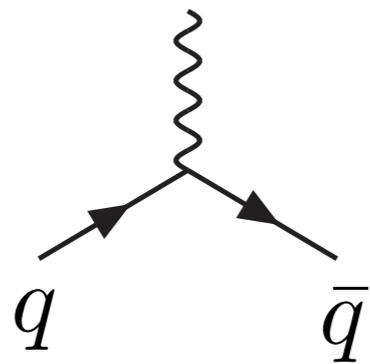
Interactions.

More details: for example, S. Martin “Supersymmetry Primer”

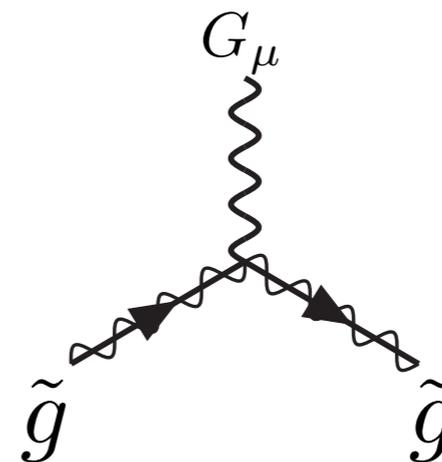
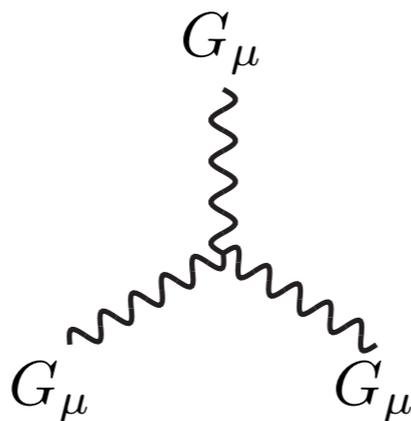
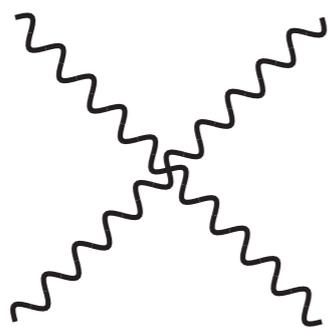
- Superpartners have the same gauge quantum numbers as their SM counter parts.

► Similar gauge interactions.

G_μ, W, Z, γ



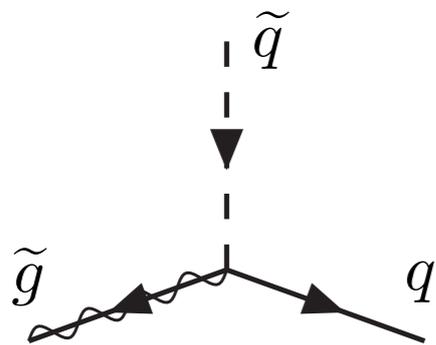
non-Abelian



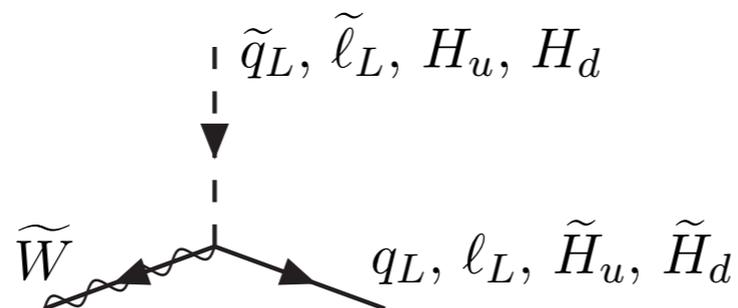
Interactions.

- SUSY \Rightarrow additional couplings
 - strength fixed by corresponding gauge

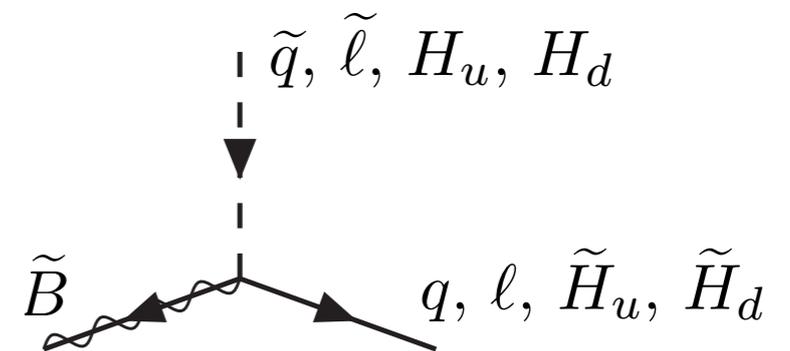
SU(3)_{color}



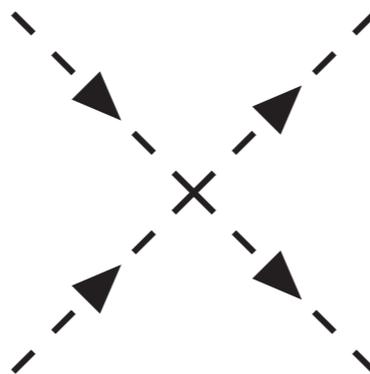
SU(2)_L



U(1)_Y

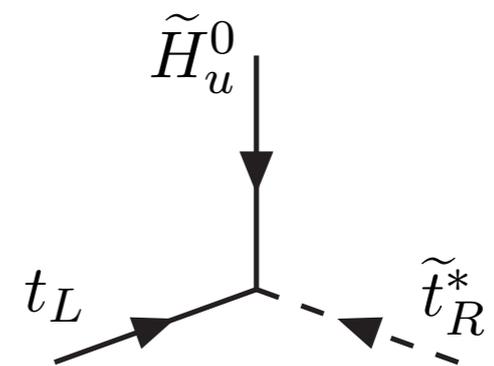
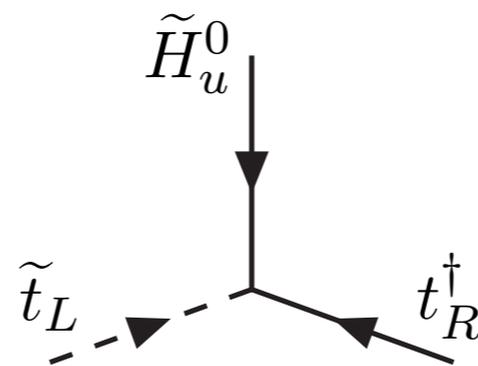
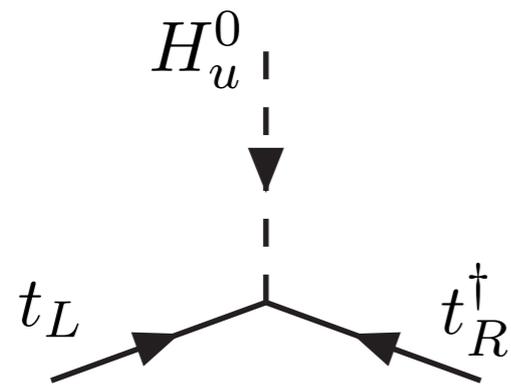


D-term: $\propto g^2$

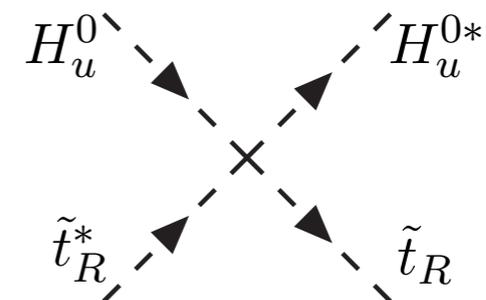


Interactions.

- SM fermions (such as the top quark) receive masses by coupling to the Higgs boson.

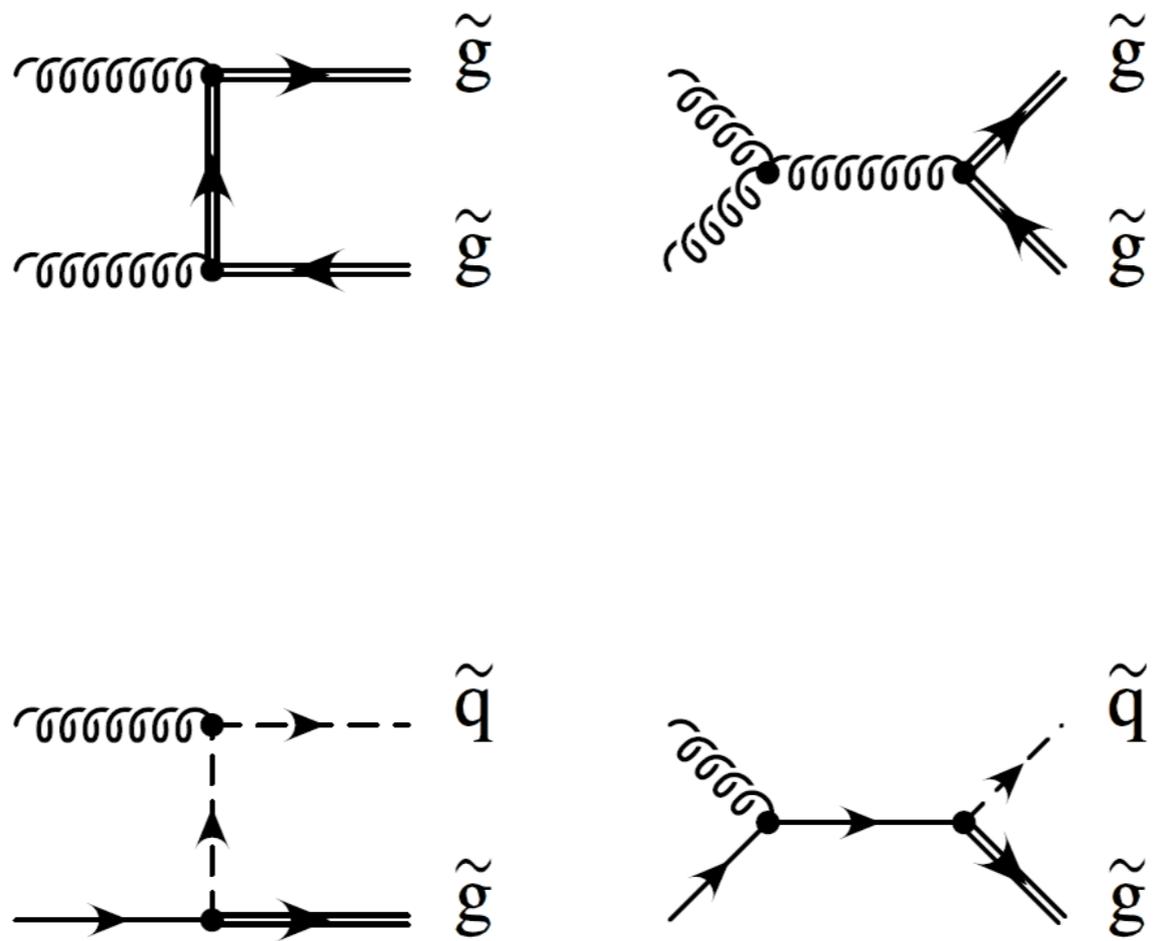


F-terms:



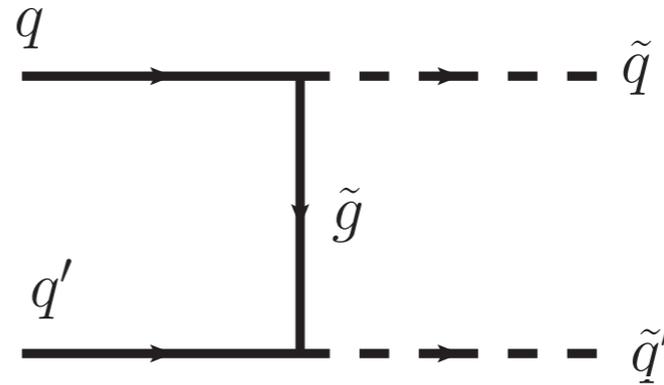
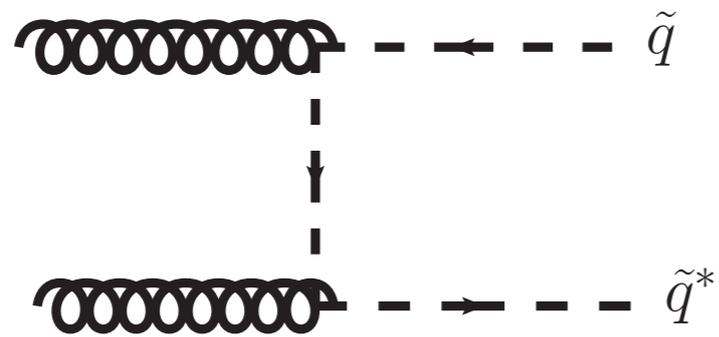
Examples of production: colored

- Squark and gluino production.



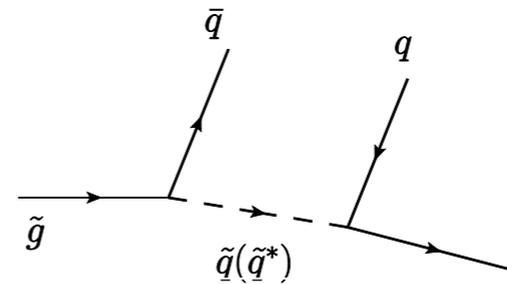
Examples of production

— Squark pair



Decay of squark and gluino

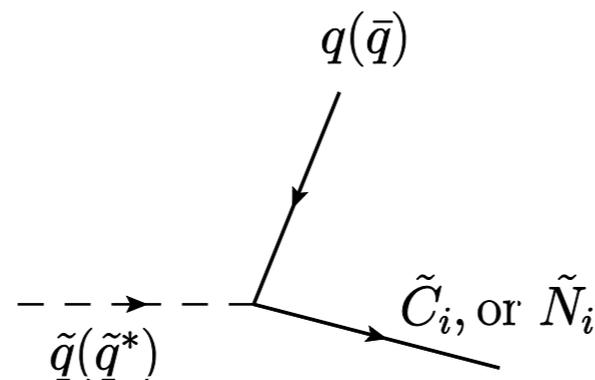
- Gluino always decays into squark (on or off-shell).
 - Gluino \rightarrow squark + Jets



- Squark decay.

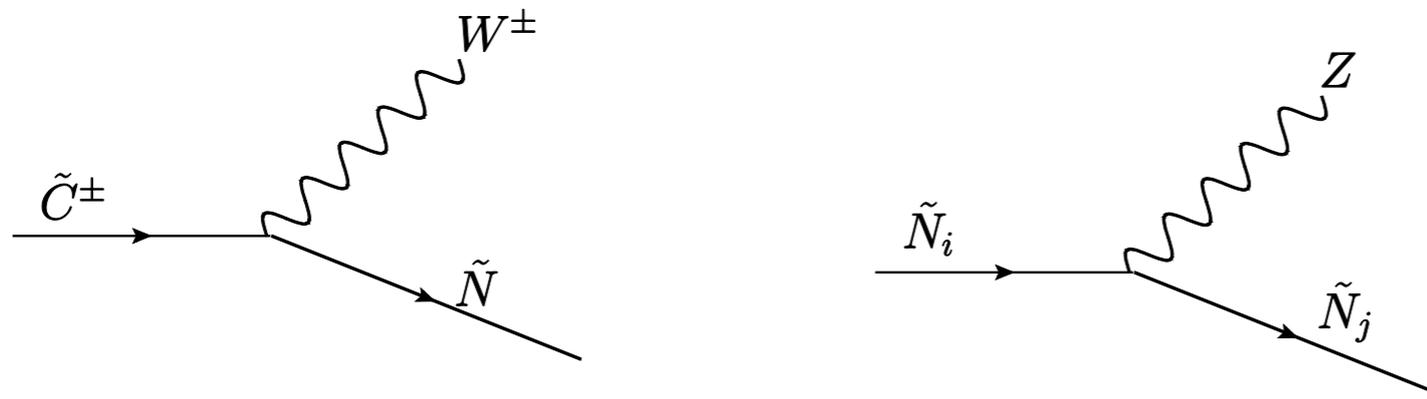
- Jet +

- To gluino, then go through off-shell squark.
- To chargino or neutralino.



Next steps

- To W or Z (maybe Higgs.)



- Lepton (suppressed by $W/Z \rightarrow$ lepton BR.)
 - 1 or 2 leptons.
- Jets (softer, constrained by W and Z mass).

Simple rules.

- Typically, there are many channels through which a superpartner can decay.
- 2 body mode (almost) always dominate over 3-body mode.
 - A factor 1/100 suppression from phase space.
- Charge channel often bigger than the neutral channels.
- Higgsino prefers 3rd generation.
- Wino prefers left-handed.
- Typically, only one or two modes dominates.
 - Signature easier to understand.

Exercise:

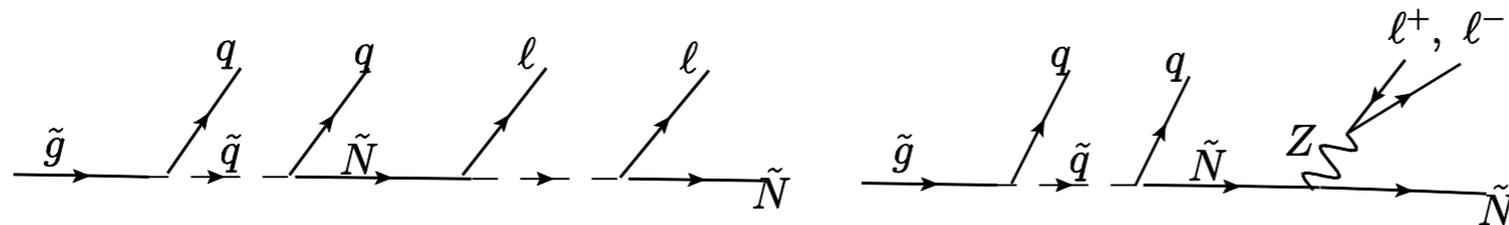
Choose a SUSY spectrum, such as one of the so called SNOWMASS Points and Slopes (SPS) benchmarks, <http://arxiv.org/abs/hep-ph/0202233>

Use a spectrum and coupling calculator such as SUSPECT, SoftSUSY, or just PYTHIA...

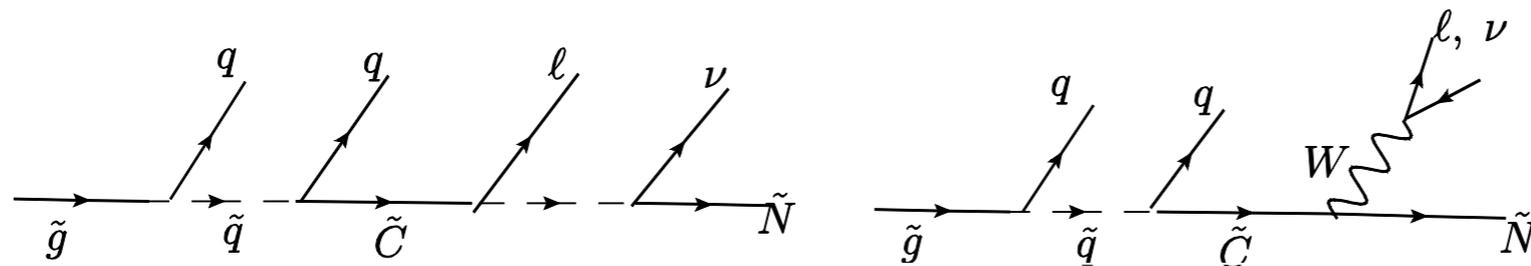
Understand the output.

Long decay chains

- Putting the pieces together.
- Many channels, many final states.



2-lepton chain



1-lepton chain

$$\begin{aligned}
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1q_2\tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1q_2[\tilde{N}_i] \rightarrow q_1q_2[Z]\tilde{N}_0 \rightarrow q_1q_2q_3q_4\tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1q_2[\tilde{C}_i] \rightarrow q_1q_2[W]\tilde{N}_0 \rightarrow q_1q_2q_3q_4\tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1q_2[\tilde{N}_i] \rightarrow q_1q_2[Z]\tilde{N}_0 \rightarrow q_1q_2\ell^+\ell^-\tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1q_2[\tilde{N}_i] \rightarrow q_1q_2q_3q_4(\ell^+\ell^-)\tilde{N}_0
 \end{aligned}$$

Exercise: draw diagrams for tri-lepton, same sign di-lepton

Typical variables I: counts.

- Inclusive counts. Useful for signal \gg background.

$n_j \times \text{jet}$

+

$n_\ell \times \text{lepton}$

+

$n_\gamma \times \gamma$

b-jet

non-b-jet

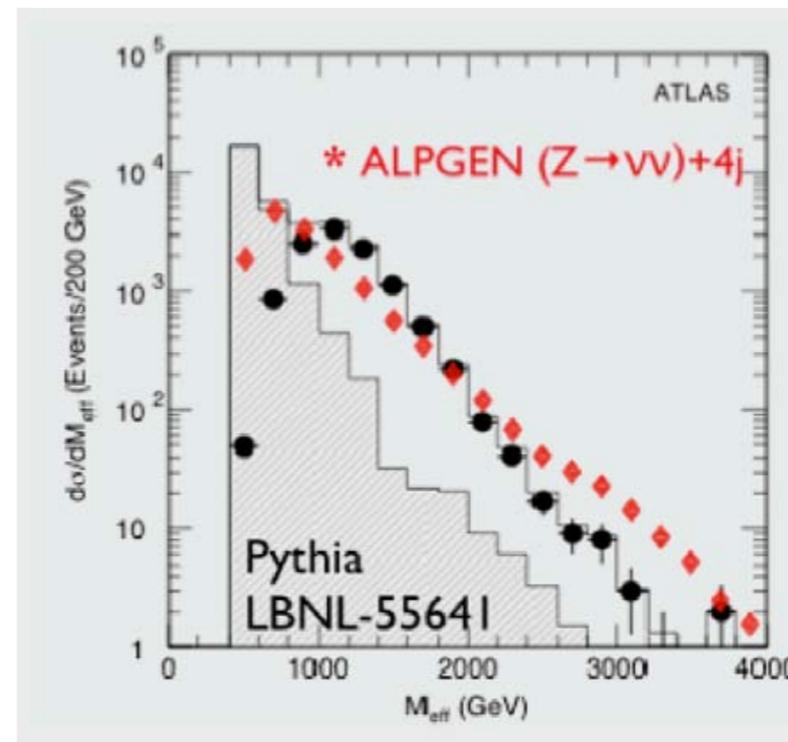
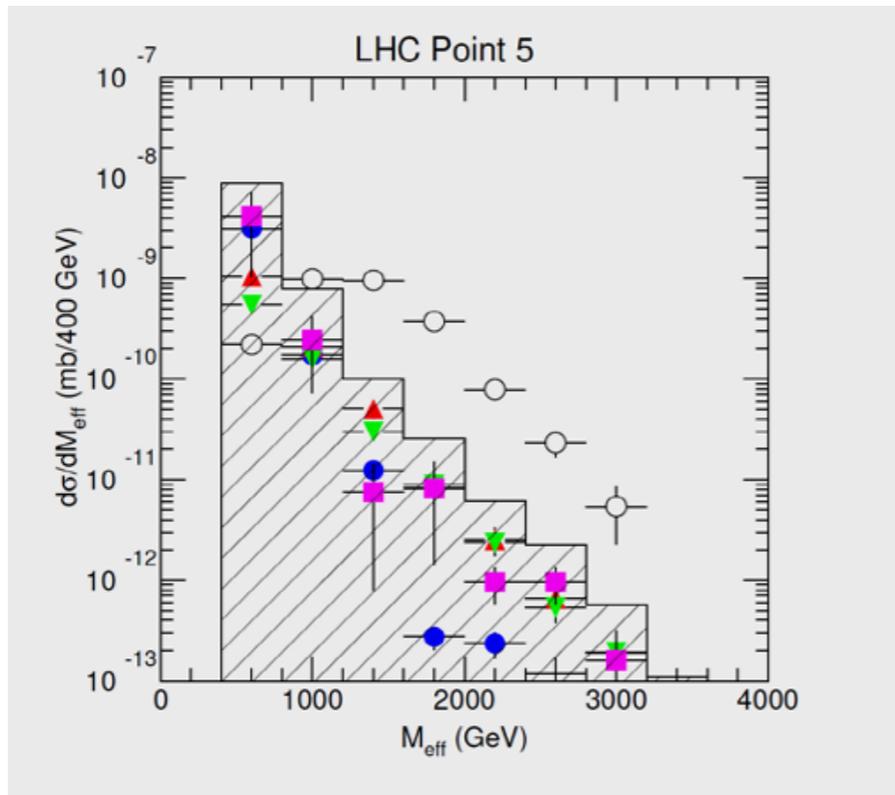
ℓ all flavor and charge

combo: e.g. $2\ell \rightarrow 21$ comb.

Kinematical features: transverse variables.

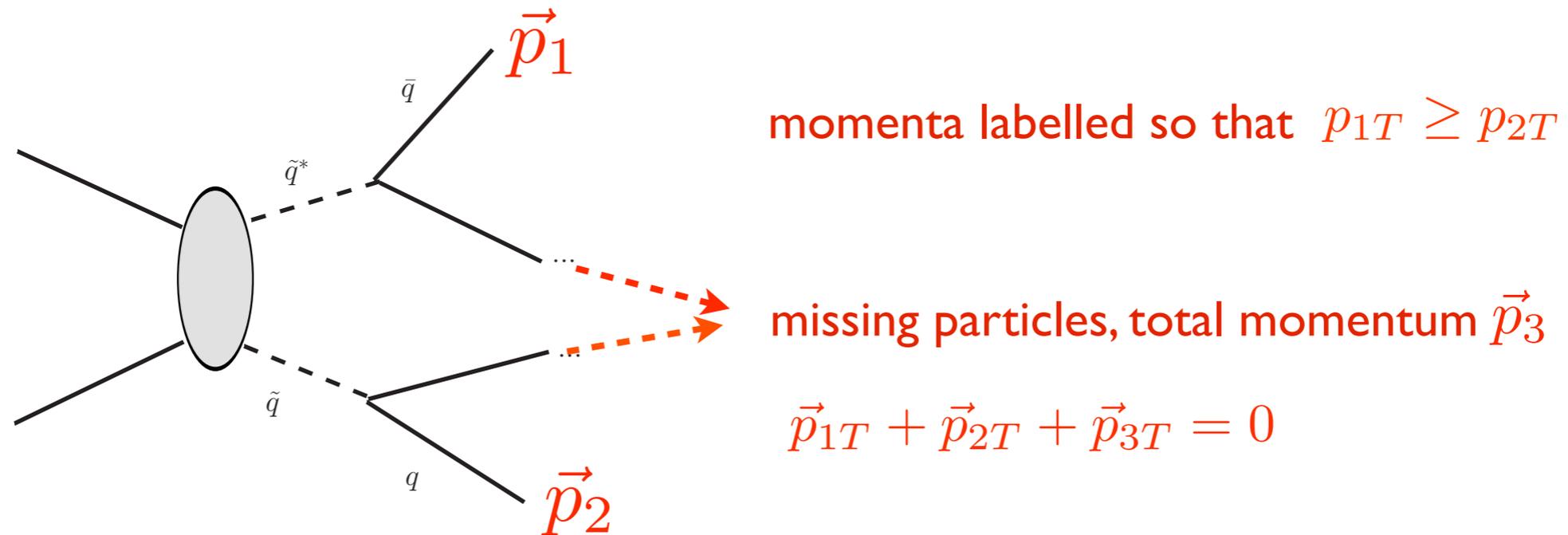
- Multiple hard objects.
- No resonance.
- Transverse variables made of several energetic objects. M_{eff} H_T

$$M_{\text{eff}} = \cancel{E}_T + p_{T,1} + p_{T,2} + p_{T,3} + p_{T,4}$$



Be careful.

Another example: α_T



Define: $\alpha_T = \frac{p_{2T}}{m_T} \quad m_T = \sqrt{(p_{1T} + p_{2T})^2 - (\vec{p}_{1T} + \vec{p}_{2T})^2}$

Define p_T fractions $x_i = \frac{p_{iT}}{\sum_{i=1,3} p_{iT}}$, $x_i \leq 1$ and $\sum_{i=1,3} x_i = 2$

We obtain $\alpha_T = \frac{1}{2} \frac{x_2}{\sqrt{1 - x_3}}$

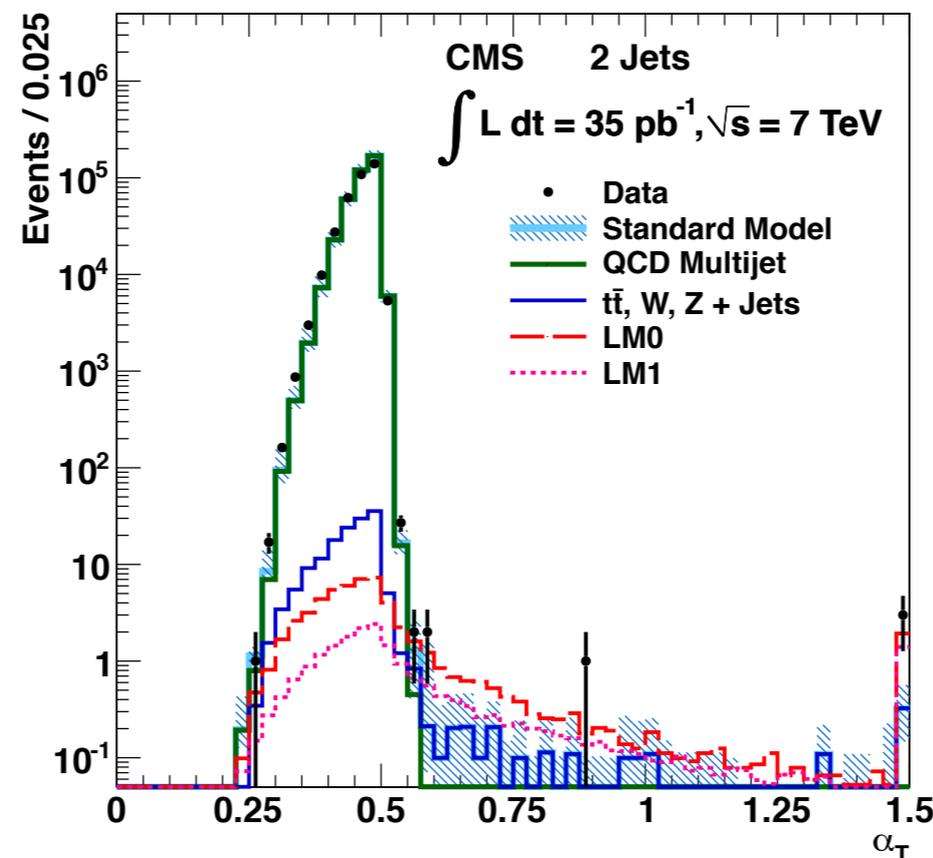
α_T can be either $< 1/2$ (more often), or $> 1/2$

For a nice review, see Michael Peskin, "Razor and Scissors"

Another example: α_T

- In comparison, consider QCD di-jet, with one of the jet (say p_{2T}) energy miss measured.

$$\vec{p}_{2T} = -\lambda \vec{p}_{1T}, \quad \lambda \leq 1 \quad \alpha_T^{\text{di-jet}} = \frac{1}{2} \sqrt{\lambda} \leq \frac{1}{2}$$



Many additional transverse variables: M_{T2} , Razor,

Kinematical variables: invariant masses

- Most useful: di-lepton edges and endpoints.
(Mentioned earlier in neutralino decay).

- Clean.

- Invariant mass distribution also carry spin information. Probably needs high statistics.

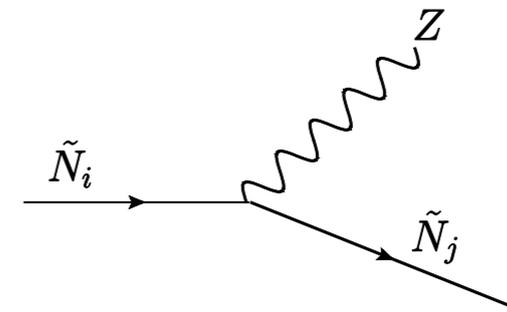
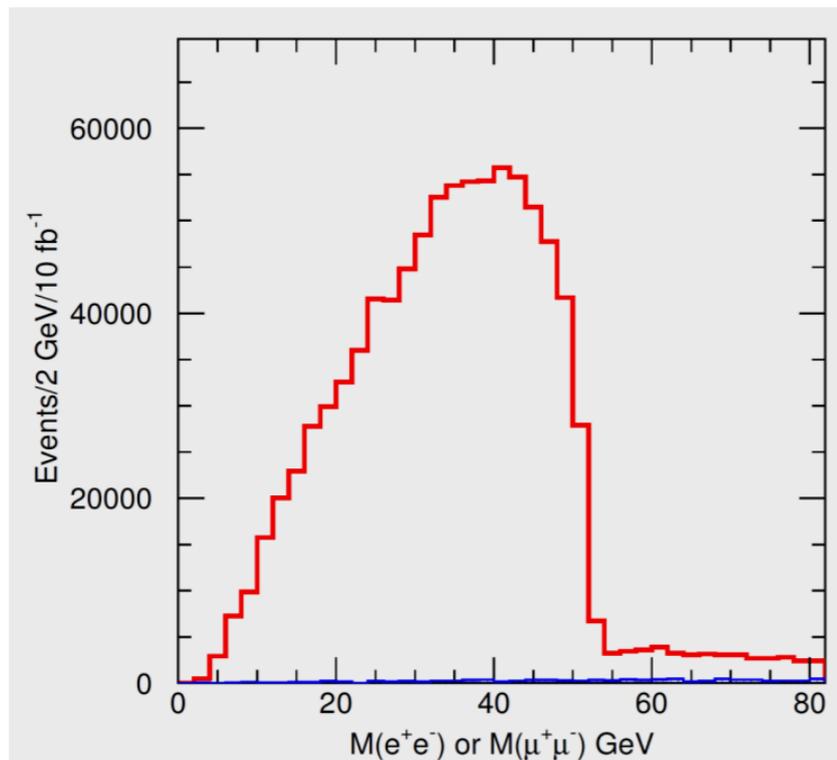
For a review: See LW and I. Yavin, 2008

- More complicated invariant masses in longer decay chains possibly useful, but feature is less sharp. May need high statistics as well.

For example, see Miller and Osland. A set of papers.

Special case: off-shell Z

- 3-body. End-point in di-lepton invariant mass.
 - Same flavor di-lepton.
 - Combinatorials can be suppressed with flavor subtraction.

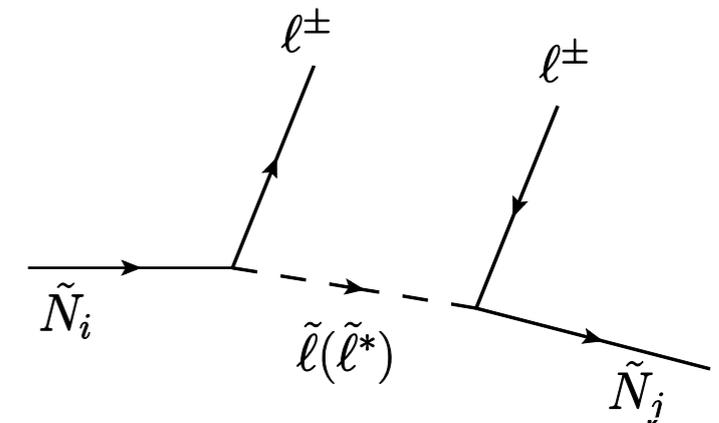
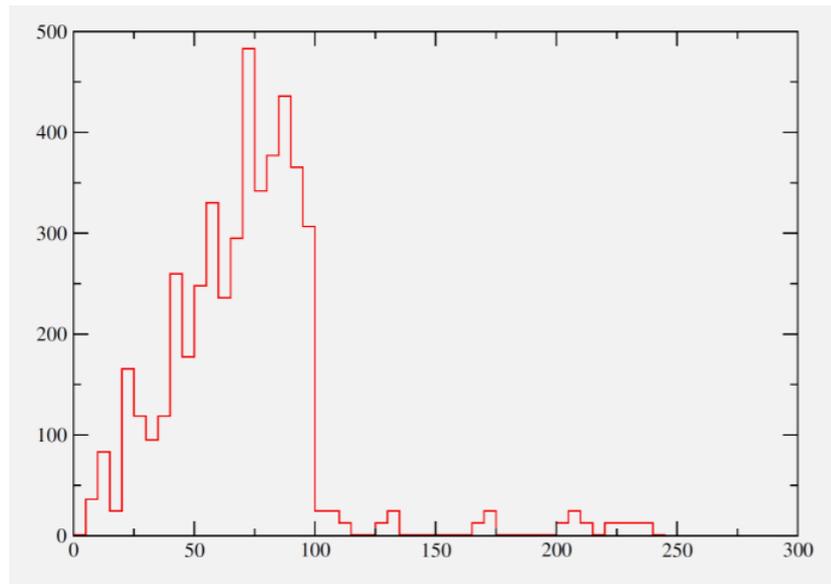


$$M_{\tilde{N}_2} - M_{\tilde{N}_1} < m_Z \longrightarrow \tilde{N}_2 \longrightarrow \tilde{N}_1 + \ell^+ + \ell^- \text{ Only 3-body}$$

$$m_{\ell\ell} = \sqrt{(p_{\ell^+}^2 + p_{\ell^-}^2)} \longrightarrow \text{end-point at } M_{\tilde{N}_2} - M_{\tilde{N}_1}$$

More leptons if we are lucky

- A lot of leptons. No branching ratio suppression.
- On shell slepton, very distinctive feature.
 - Edge in di-lepton invariant mass.



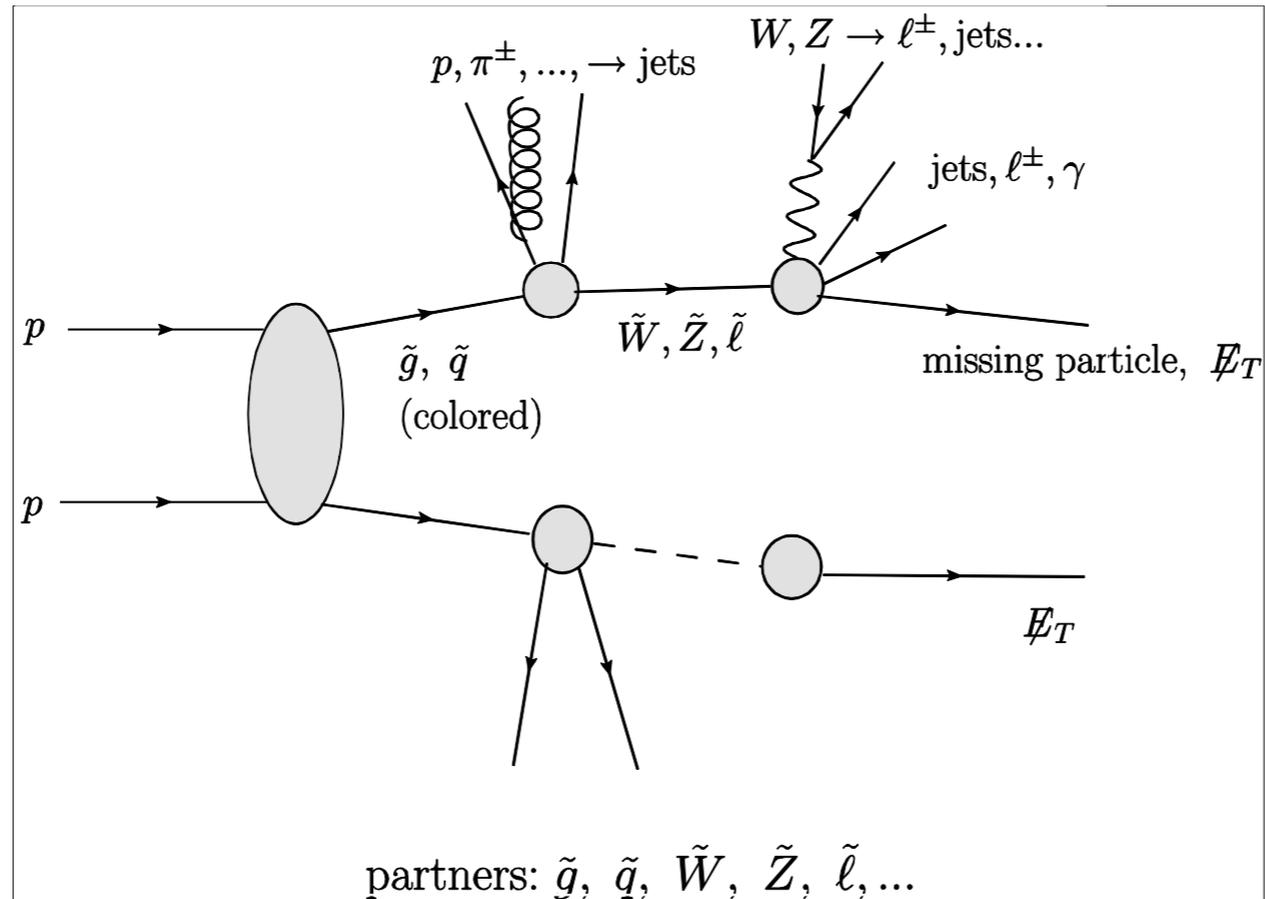
$$m_{\tilde{\ell}} < M_{\tilde{N}_2} \longrightarrow \tilde{N}_2 \rightarrow \tilde{N}_1 + [\tilde{\ell}] \rightarrow \tilde{N}_1 + \ell^+ + \ell^-$$

$$M_{\ell\ell}^{\max} = M_{\tilde{N}_2} \sqrt{1 - \frac{m_{\tilde{\ell}}^2}{M_{\tilde{N}_2}^2}} \sqrt{1 - \frac{M_{\tilde{N}_1}^2}{m_{\tilde{\ell}}^2}}$$

- More complicated edges useful, but need high statistics.

See several papers by: Miller, Osland.

Topology: model independent approach



partners:

Same gauge interactions as the
SM particles
Similar signatures.

$$\tilde{g}, \tilde{q}, \tilde{W}, \tilde{Z}, \tilde{\ell} \dots$$

$$g^{\text{KK}}, q^{\text{KK}}, W^{\text{KK}}, Z^{\text{KK}}, \ell^{\text{KK}} \dots$$

<http://indico.cern.ch/conferenceOtherViews.py?view=standard&confId=94910>

<http://www.lhcnewphysics.org/web/Overview.html>

A promising, and complicated, scenario.

$$> \text{TeV} \quad \begin{array}{l} \text{-----} \tilde{u}, \tilde{d}, \dots \\ \text{-----} \tilde{t}, \tilde{b} \end{array}$$

$$\sim 100\text{s GeV} \quad \begin{array}{l} \text{-----} \tilde{g} \\ \text{-----} \tilde{N} \end{array}$$

$$p p \rightarrow \tilde{g}\tilde{g} \rightarrow t\bar{t}t\bar{t} (\text{or } t\bar{t}b\bar{b}, t\bar{t}t\bar{b} \dots)$$

The Dominant channel

$$\tilde{g} \rightarrow t\bar{t}(b\bar{b}) + \tilde{N}, \text{ or } t\bar{b} + \tilde{C}^- \quad t \rightarrow b\ell^+\nu$$

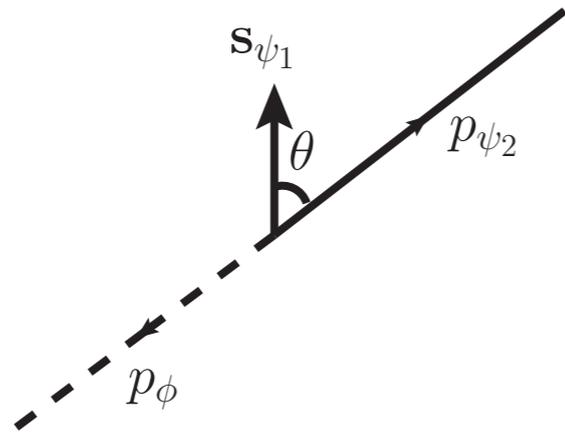
- Multiple b, multiple lepton final state.
- Good early discovery potential.
- Challenging to interpret: top reconstruction

A new method of fitting branching ratio to various final states

Acharya, Grajek, Kane, Kuflik, Suruliz, Wang, arXiv:0901.3367

An example of a challenging
measurement: spin
or distinguishing SUSY with others.

Spin of new resonances

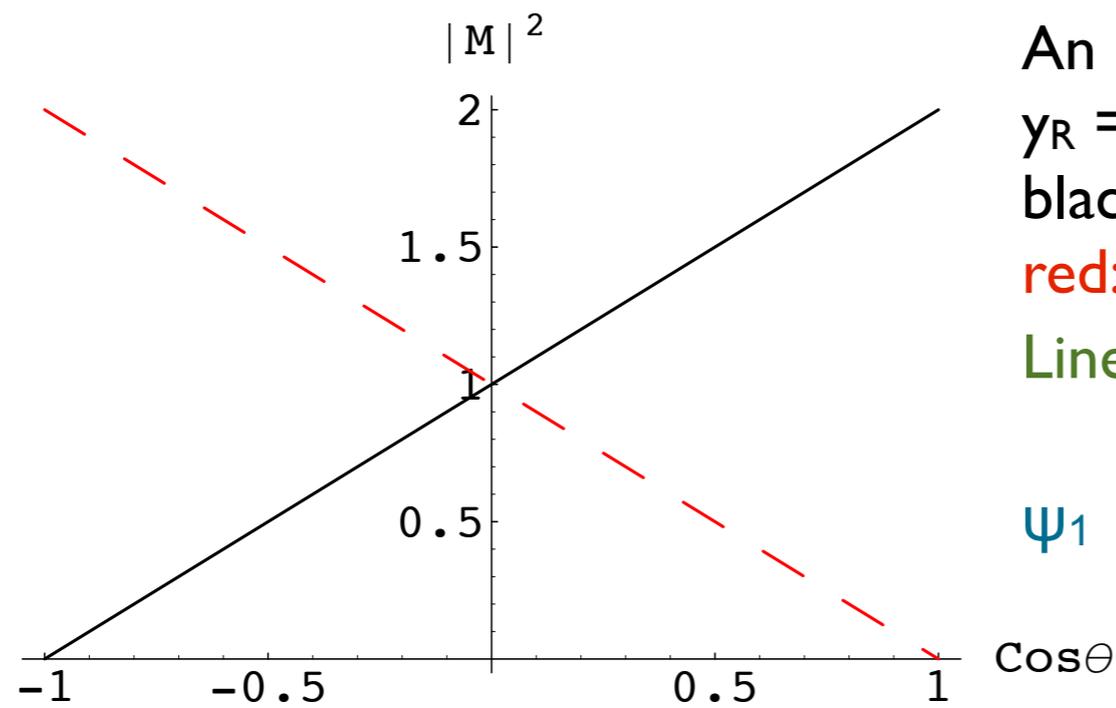


$$\psi_1 \rightarrow \psi_2 + \phi$$

$$y_L \phi \bar{\psi}_2 P_L \psi_1 + y_R \phi \bar{\psi}_2 P_R \psi_1$$

- Example spin of fermion.
 - In the rest frame of the fermion.
 - Define angle θ of the decay product w.r.t. the polarization axis of ψ_1 .
 - Coupling could be chiral if $y_L \neq y_R$

Fermion spin



An Example

$y_R = 0$

black: ψ_1 right-handed,

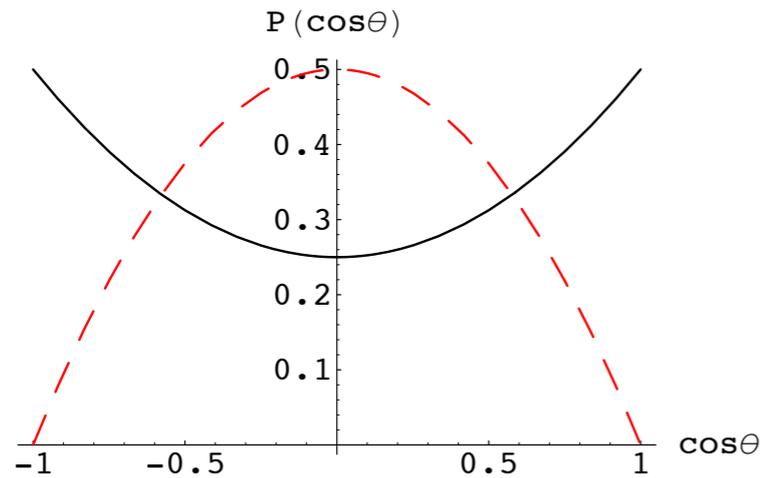
red: ψ_1 left-handed

Linear in $\cos\theta$

ψ_1 not polarized, no correlation, no spin information

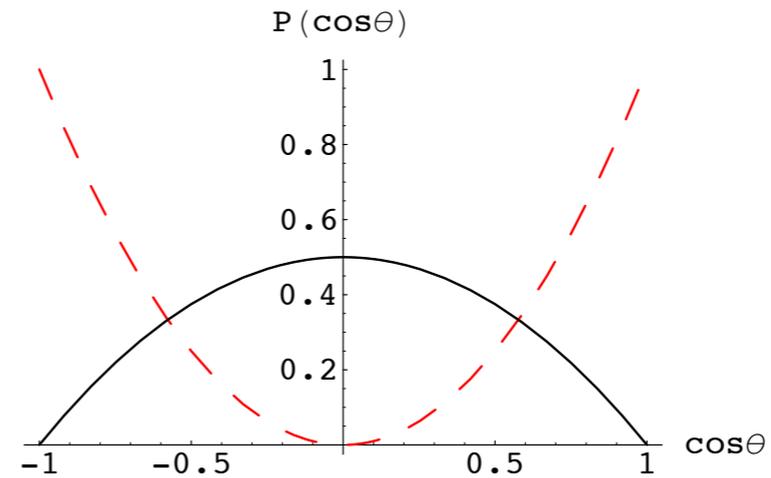
- Go to the rest frame.
- Coupling chiral.
- ψ_1 polarized.

Spin-1



$$A'_{\text{transverse}} \rightarrow \psi_1 + \psi_2$$

$$A'_{\text{longitudinal}} \rightarrow \psi_1 + \psi_2$$



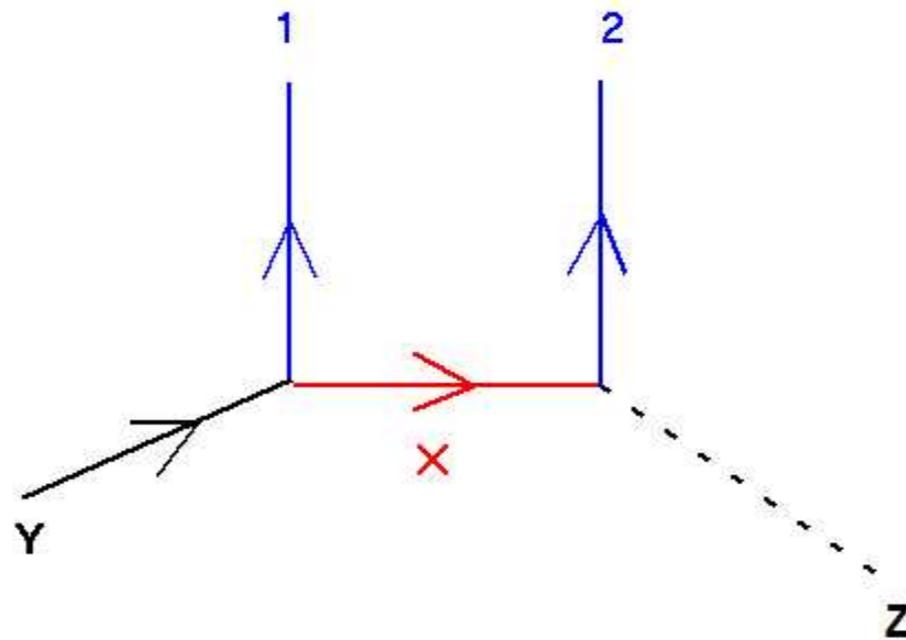
$$A'_{\text{transverse}} \rightarrow \phi_1 + \phi_2$$

$$A'_{\text{longitudinal}} \rightarrow \phi_1 + \phi_2$$

$$|\mathcal{M}|^2 \propto \cos^2 \theta$$

In general: $|\mathcal{M}|^2 \propto \dots + \cos^2 \theta^{J_{\text{mother}}}$

Example of spin measurement



1 and 2 are observable particles, q , ℓ , W^\pm

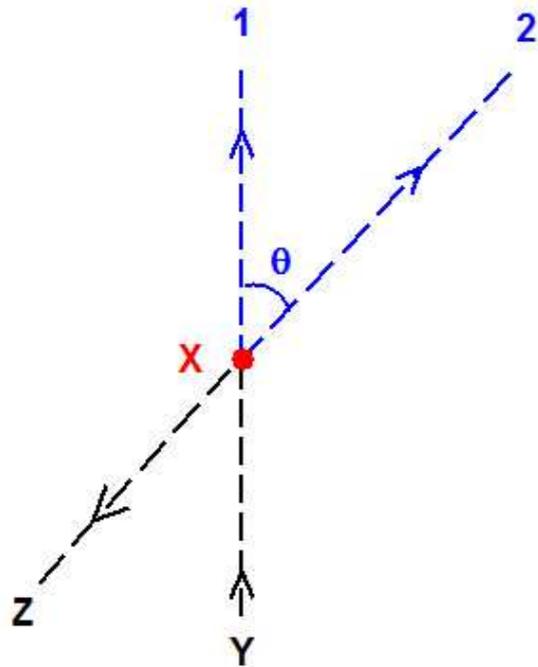
We are interested in the spin of **X** (on-shell).

We choose to use

$$t_{12} = (p_1 + p_2)^2.$$

In general, can not reconstruct the rest frame of X

Consider the rest frame of X



$$t_{12} \propto (1 - \cos \theta)^2$$

Direction of Y and 1 can be chosen to define the polarization of X
For X with spin J_X

$$\frac{d\Gamma}{dt_{12}} = a t_{12}^{2J_X} + b t_{12}^{2J_X-1} + \dots$$

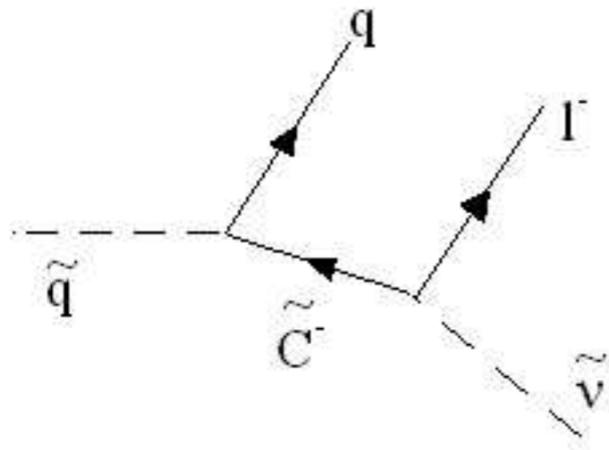
In principle, fitting the degree of this polynomial tells the the spin of X.

In practice, whether the coefficient a, b, ... are non-zero depends on the chirality of the coupling between X and 1, 2, Z, Y, and the mass differences between them.

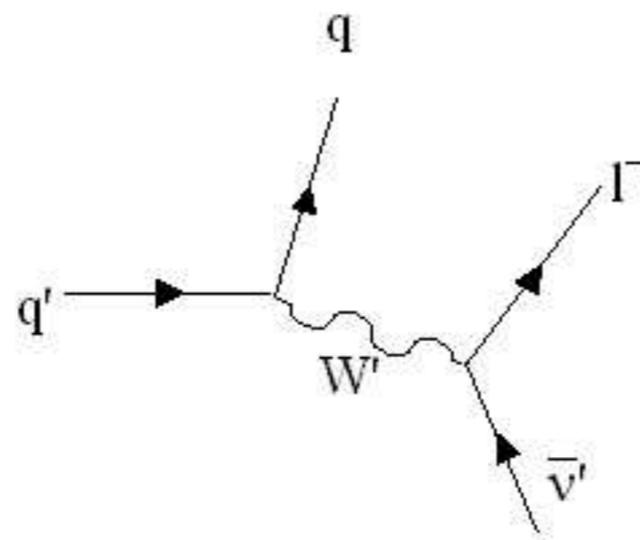
Interpreting the results correctly depending on our understanding the spectrum and couplings.

Example: SUSY vs spin-1 partner

Decay through charged partners $\tilde{\chi}^\pm, W'^\pm \dots$



$\propto t_{ql} + \dots$
 $\tilde{q} - q - \tilde{C}$ chiral
 q boosted
 $\tilde{C} - \tilde{\nu} - l$ chiral

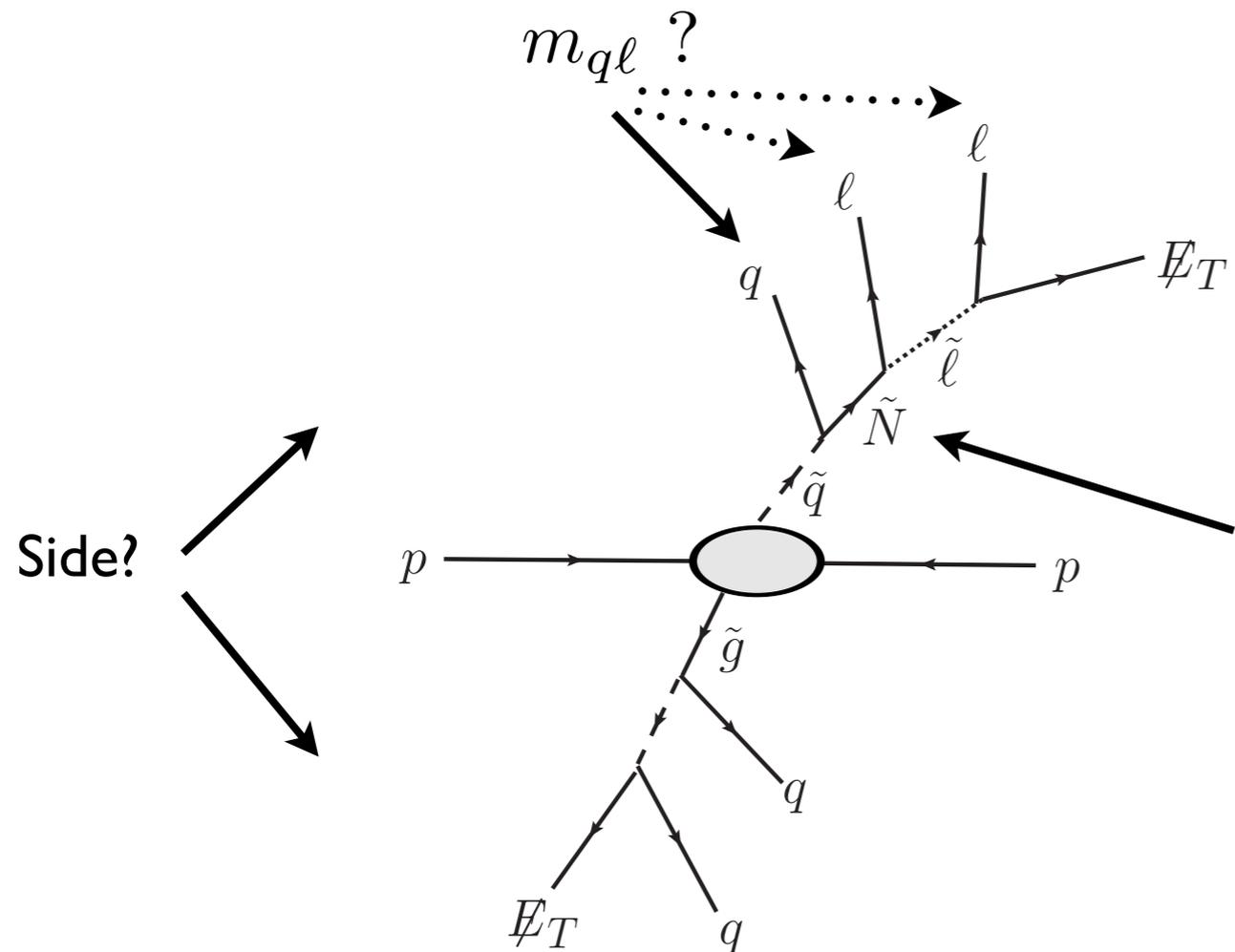


$\propto t_{ql}^2 + \dots$
 $m_{q'} \gg m_{W'}$
 W' boosted

Usually there are more leptons in the decay chain.

Near/far lepton has to be separated.

Spin measurements. Supersymmetry?



Example: spin of \tilde{N}

Clean exclusive sample

Boost (kinematics) vs matrix element (spin)
 \rightarrow Consider m_{ql}

Combinatorics

- No universally applicable method. Different strategies will be used in different scenarios.

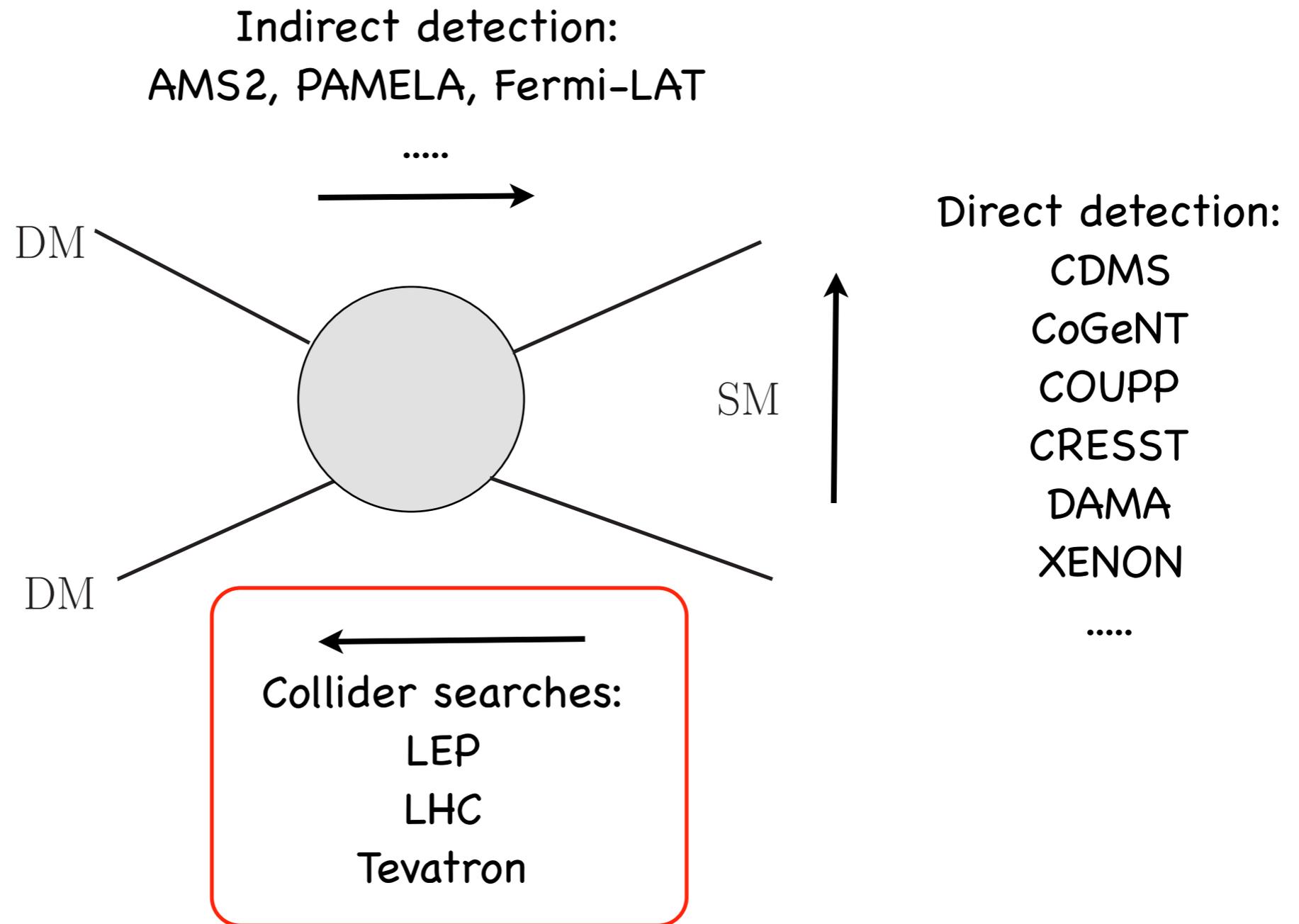
A review: LTW and Yavin, arXiv:0802.2726

- More information of the signal, masses and underlying processes, is crucial.

Lepton colliders

- Fixed c.o.m.
- Much cleaner environment.
- Energy not as high.

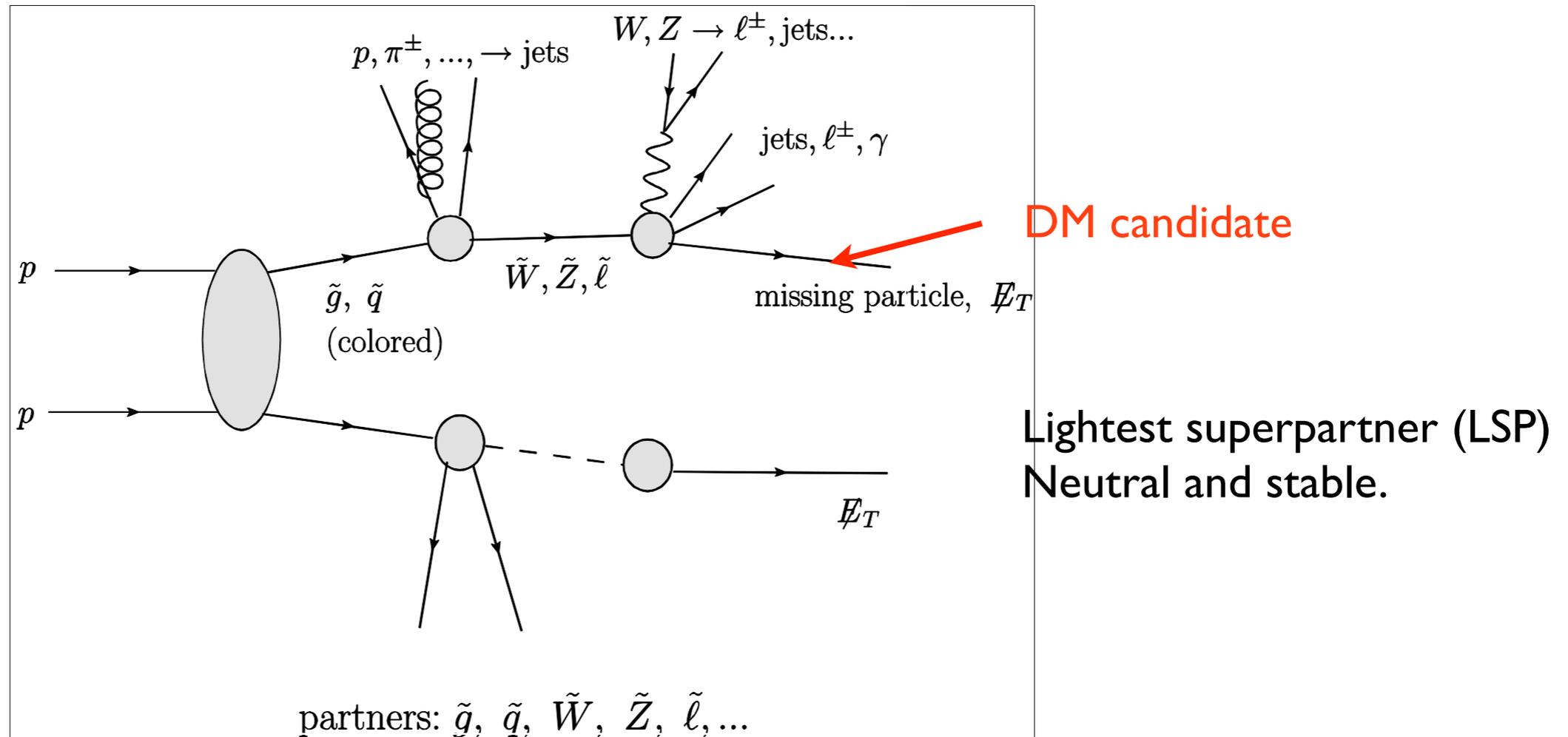
Searching for WIMP dark matter



This talk.

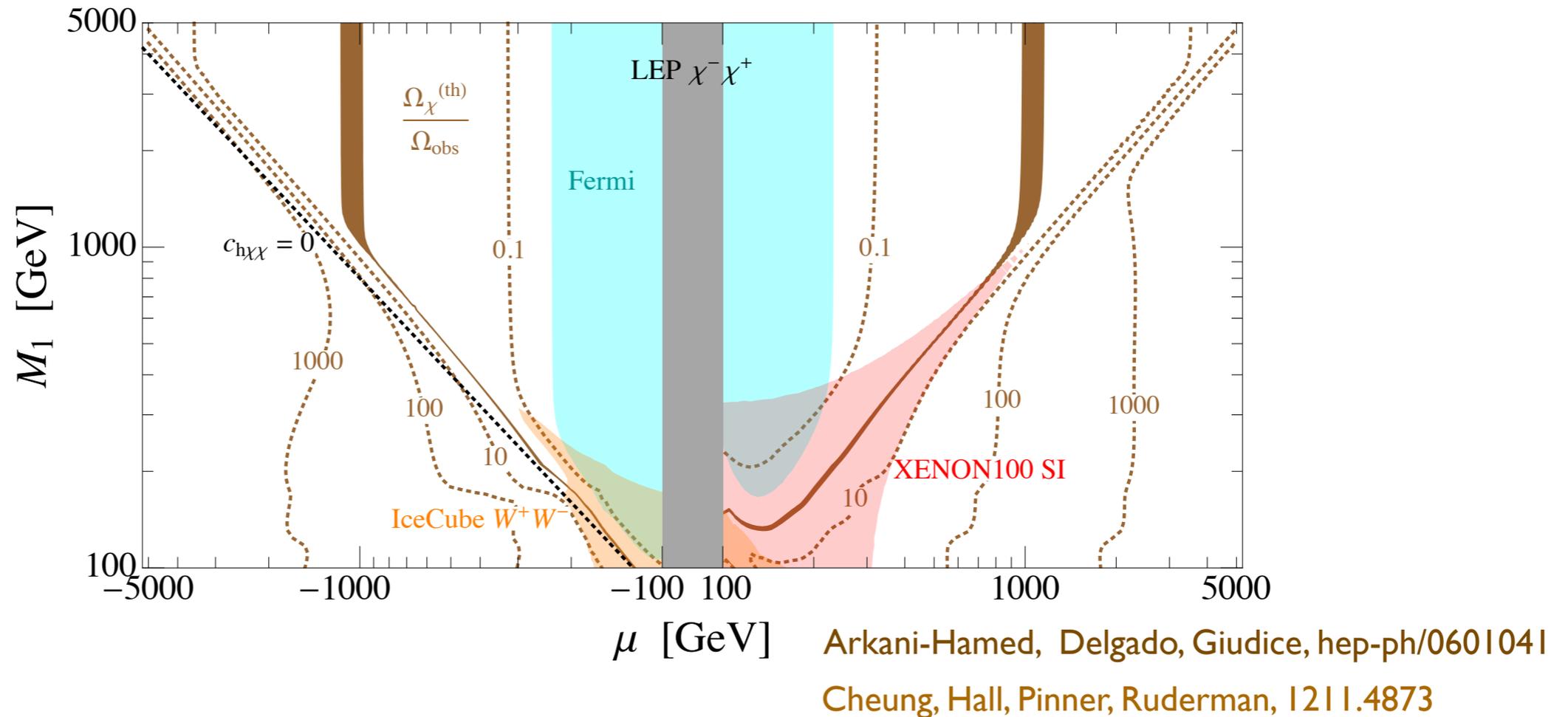
Discovering dark matter:

- DM candidate embedded in an extended TeV new physics scenario



- Could be early discovery.

Narrow parameter space, could still work.



- The so called "well tempered" scenario.

- Also, A-funnel, stau/stop/squark co-ann.

Cahill-Rowley, Hewett, Ismail, Peskin, Rizzo, 1305.2419

Cohen, Wacker, 1305.2914

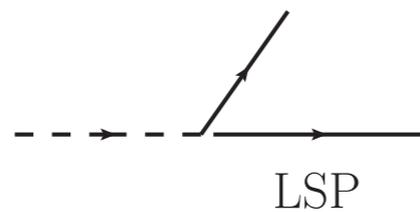
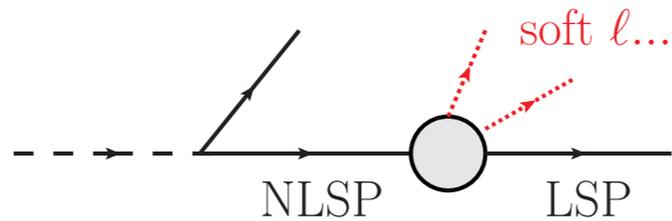
- Challenging to see at the LHC.

Giudice, Han, Wang and LTW, 1004.4902

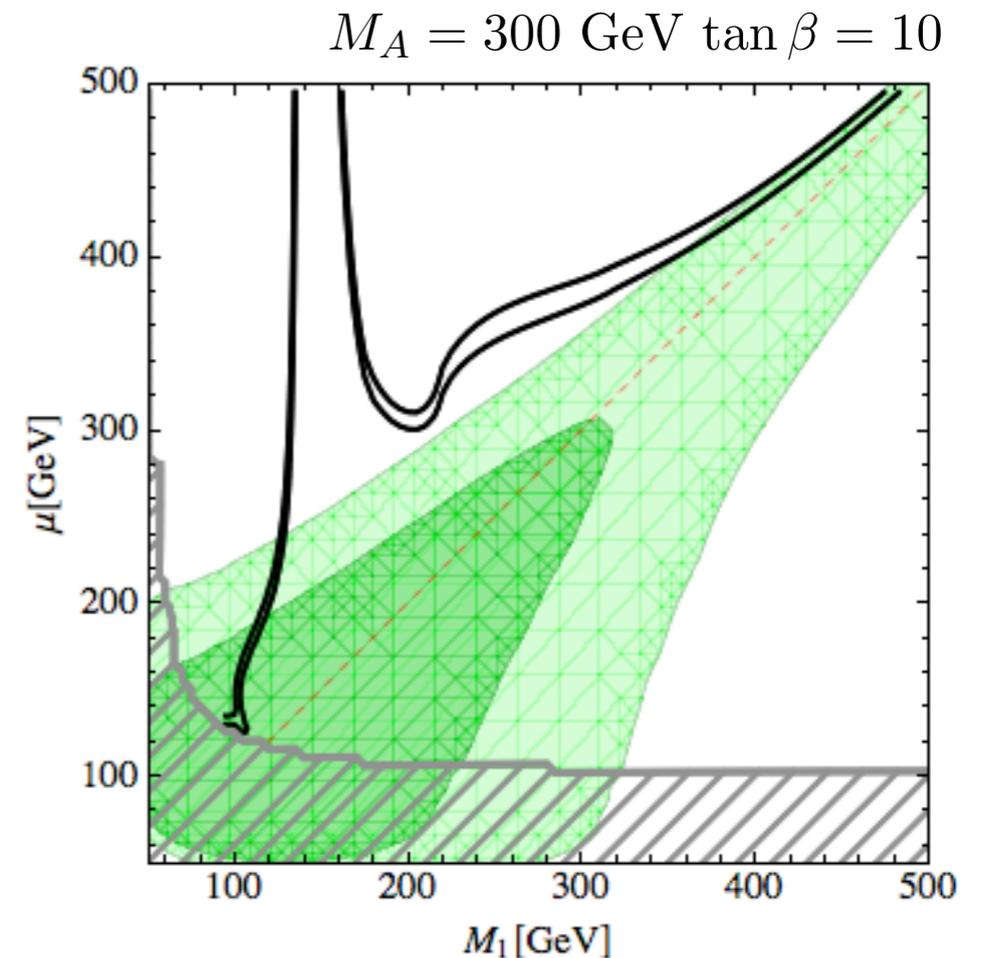
Could be harder make sure.

- For example: the “well tempered” scenario.
Nearly degenerate NLSP and LSP.

N.Arkani-Hamed, A. Delgado, G. Giudice, hep-ph/0601041



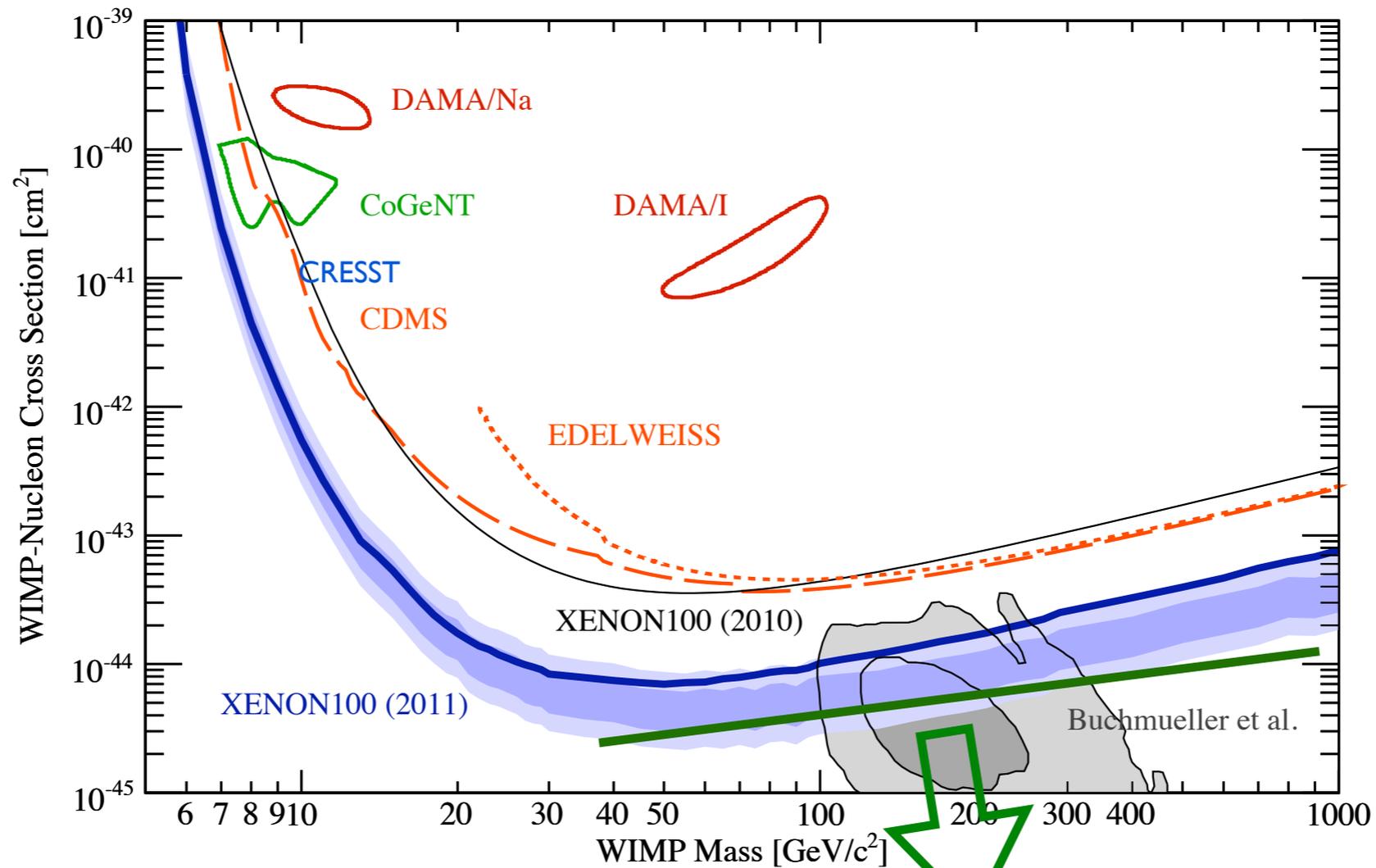
$$m_{\text{NLSP}} - m_{\text{LSP}} \sim 10 - 20 \text{ GeV}$$



S. Gori, P. Sechwall, C. Wagner, 1103.4138

Probe NP with direct detection

XENON 100, 1104.2549

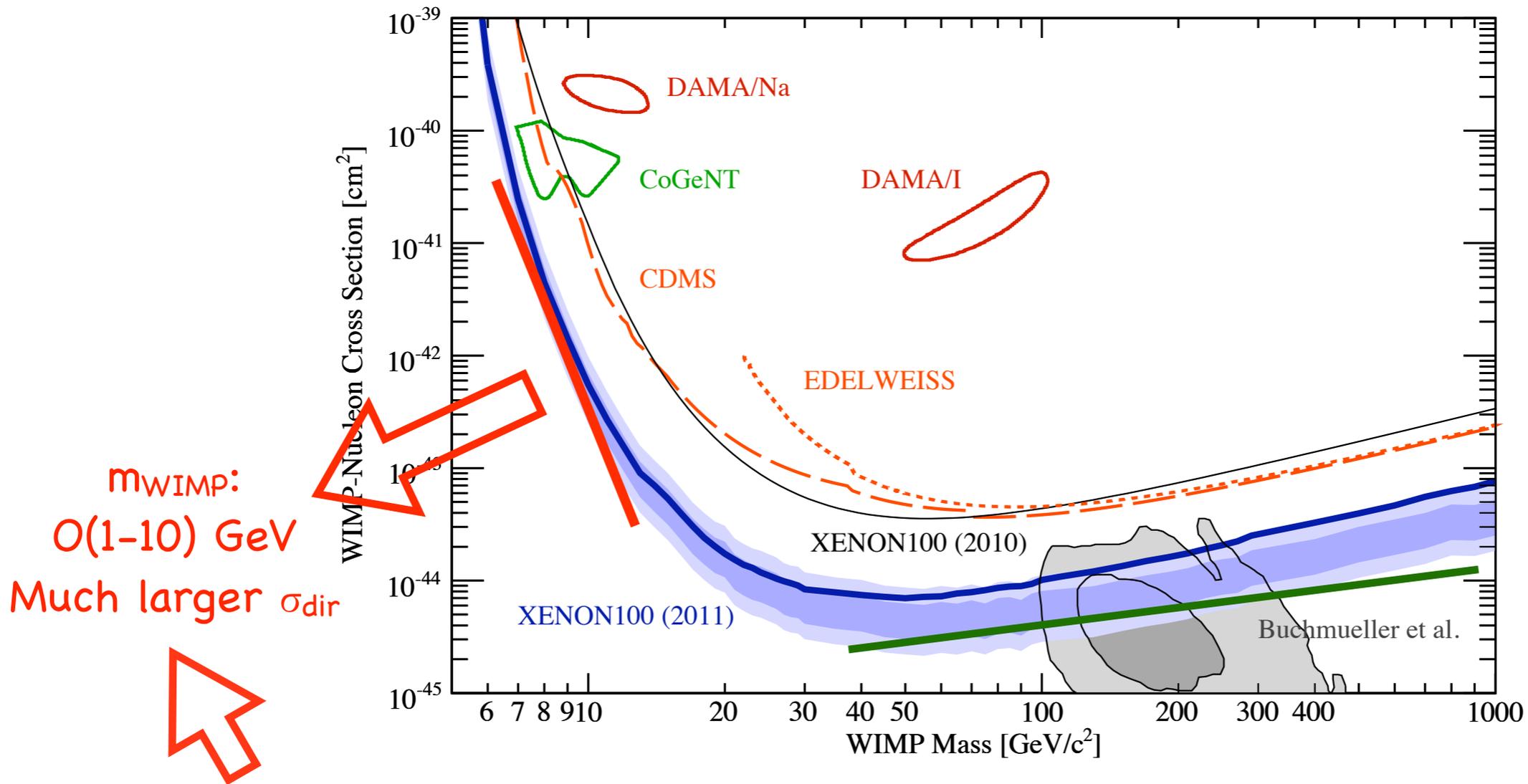


— $M_{WIMP} = O(10^2)$ GeV.

— DM of "Typical" scenarios: SUSY

Probe NP with direct detection

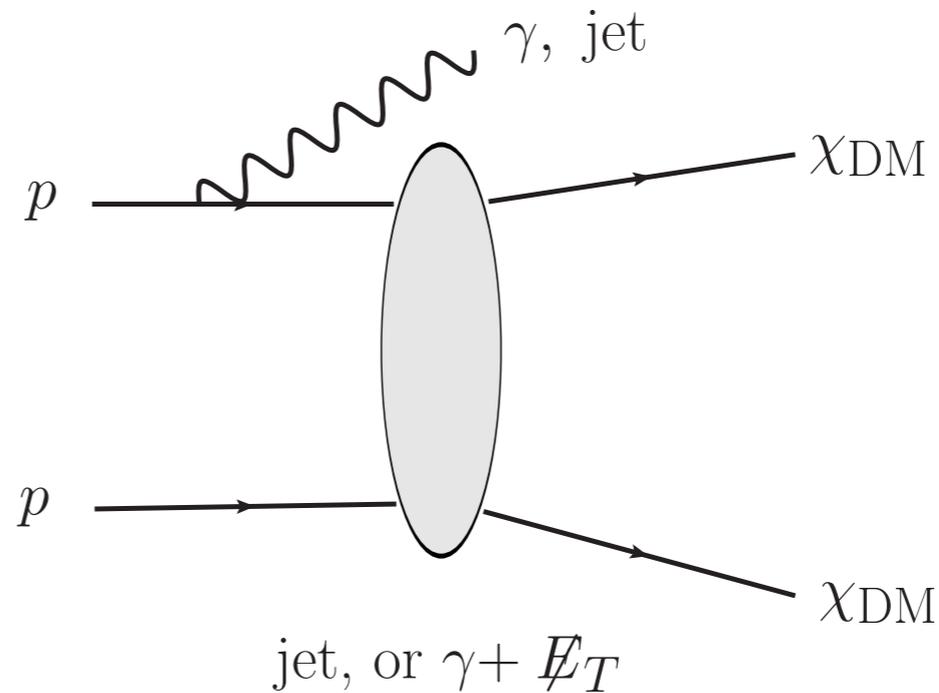
XENON 100, 1104.2549



- Collider searches provide stronger bounds/potential

Collider Signals of dark matter.

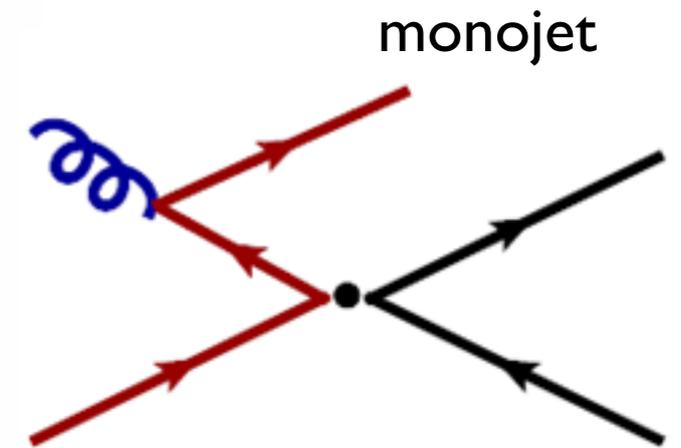
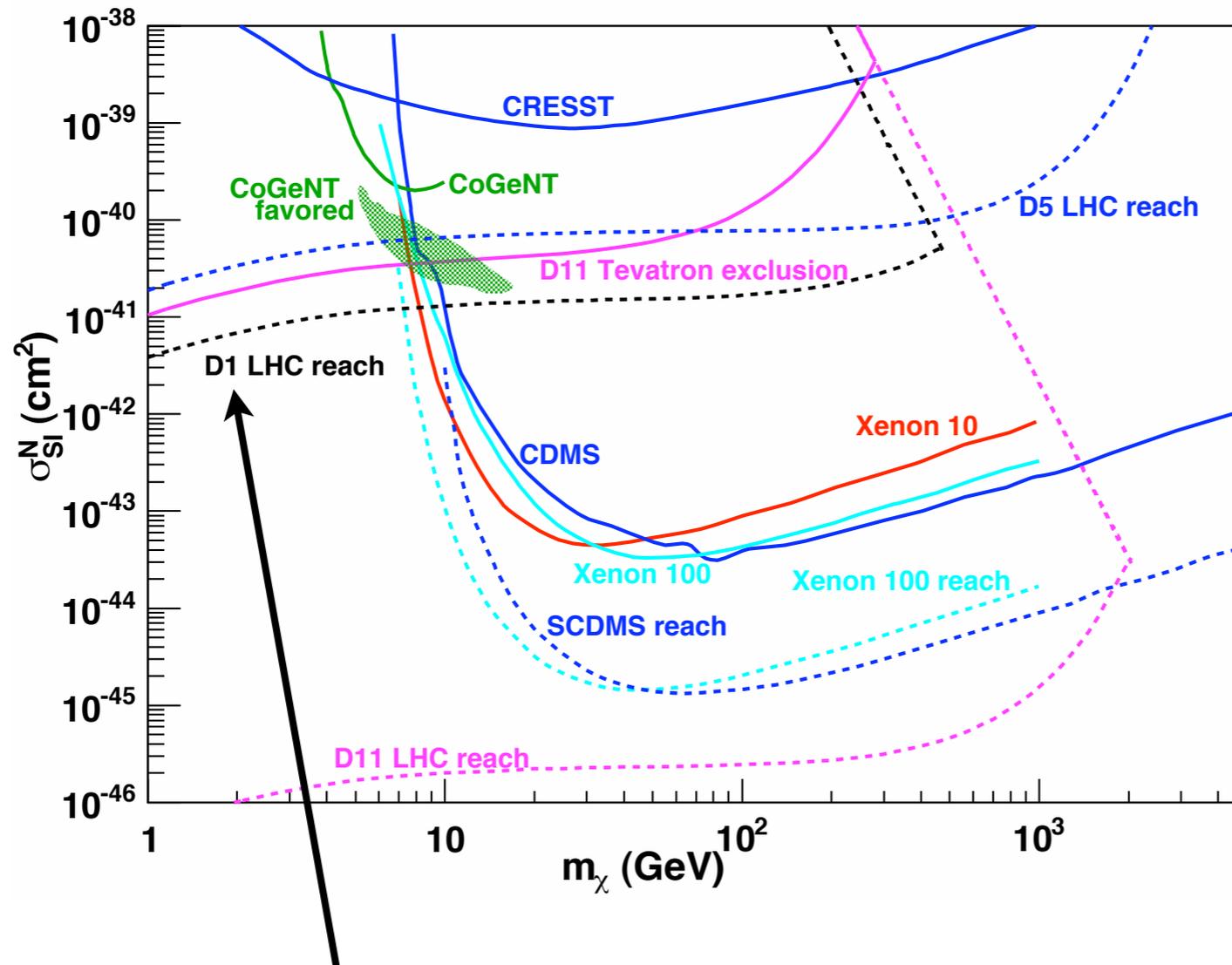
- Basic channel: pair production + additional radiation.



- Large Standard Model background, about 10 times the signal.
- Very challenging.

For example, 1008.1783

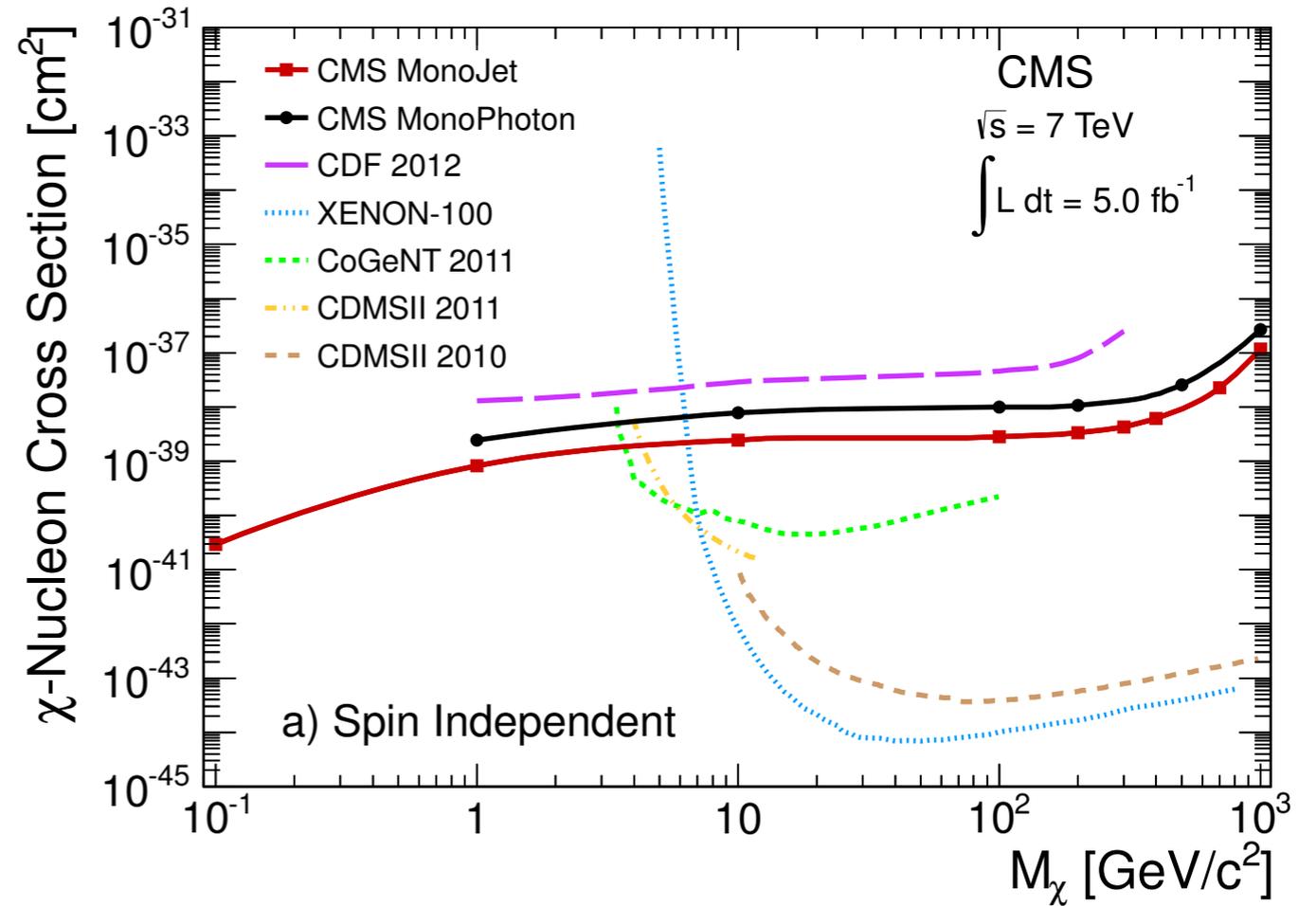
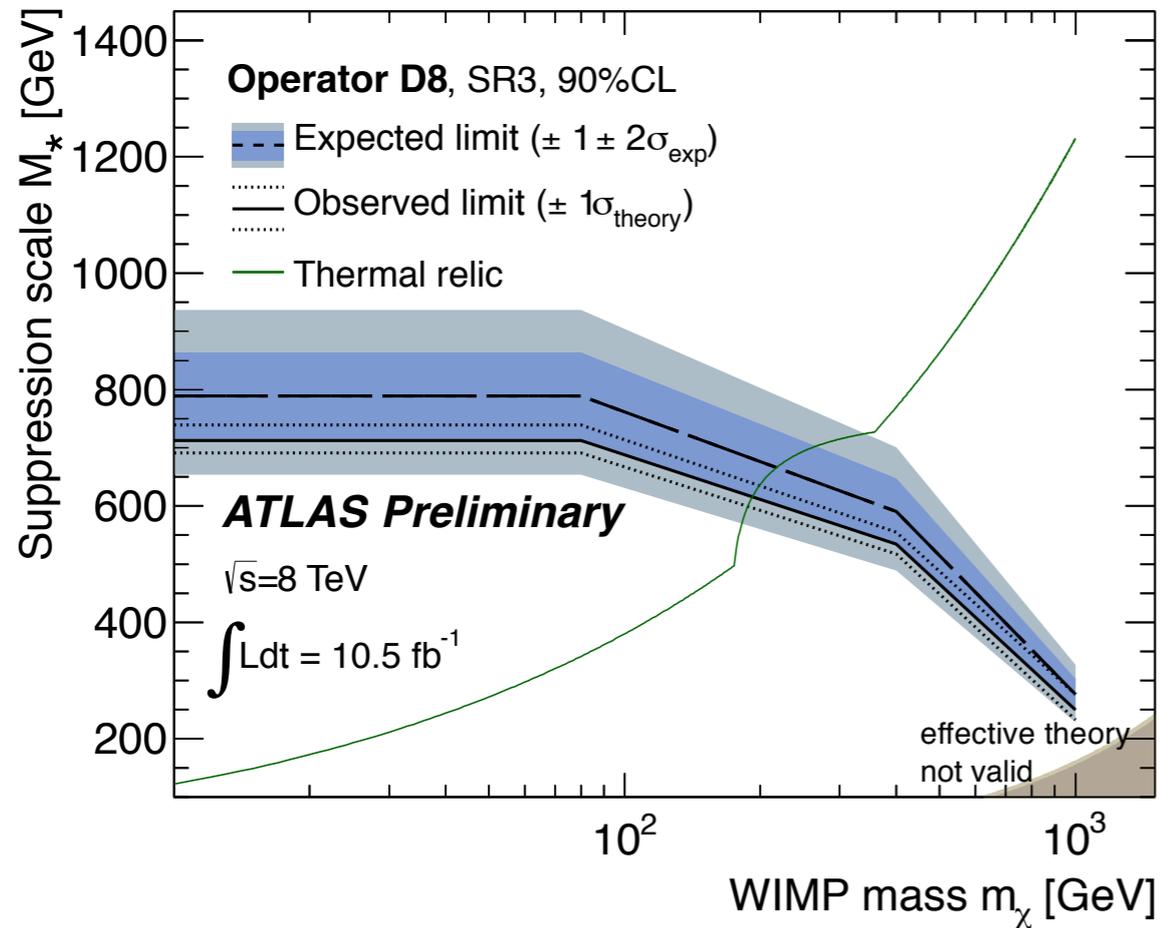
Goodman, Ibe, Rajaraman, Shepherd, Tait, Yu, 1008.1783



D1	$\bar{\chi}\chi\bar{q}q$
D5	$\bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu q$
D11	$\bar{\chi}\chi G_{\mu\nu}G^{\mu\nu}$

For small m_χ ,
collider rates controlled by larger mass scales, i.e., p_T cut;
does not depend on m_χ .
Collider bounds flat and stronger.

Recent results

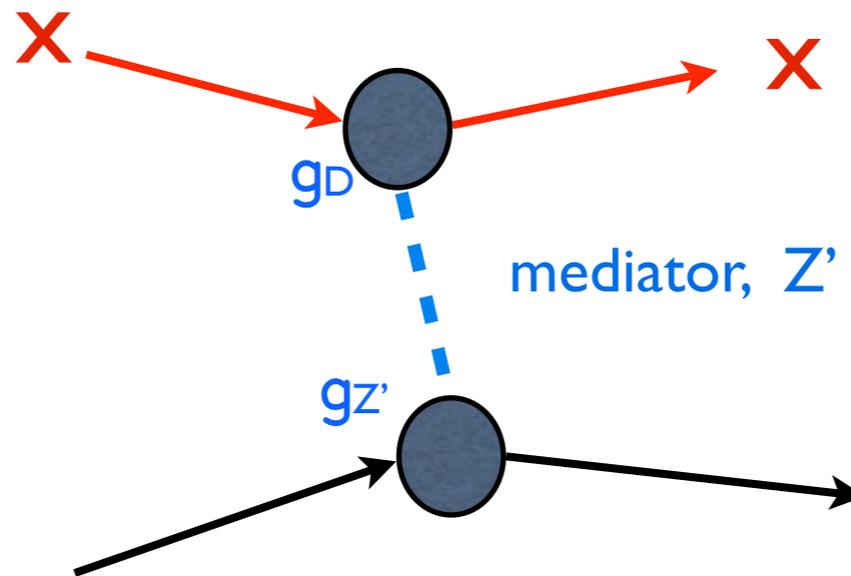


Case study: a spin-1 Z'

Xiang-Dong Ji, Haipeng An, LTW 1202.2894

$$\mathcal{L} = Z'_\mu [\bar{q}(g_{Z'}\gamma^\mu + g_{Z'5}\gamma^\mu\gamma_5)q + \bar{X}(g_D\gamma^\mu + g_{D5}\gamma^\mu\gamma_5)X]$$

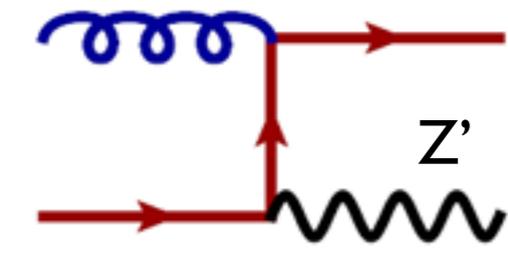
Only couples to SM quarks and DM.



$$g_D \sim g'_{Z'} \rightarrow \sigma_{\text{dir}} \propto \frac{g'^4_{Z'}}{m^4_{Z'}}$$

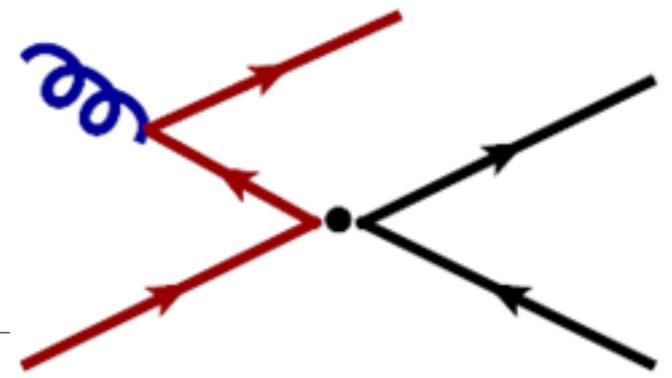
N= Ar, Ge, Xe, ...

Connection with direct detection

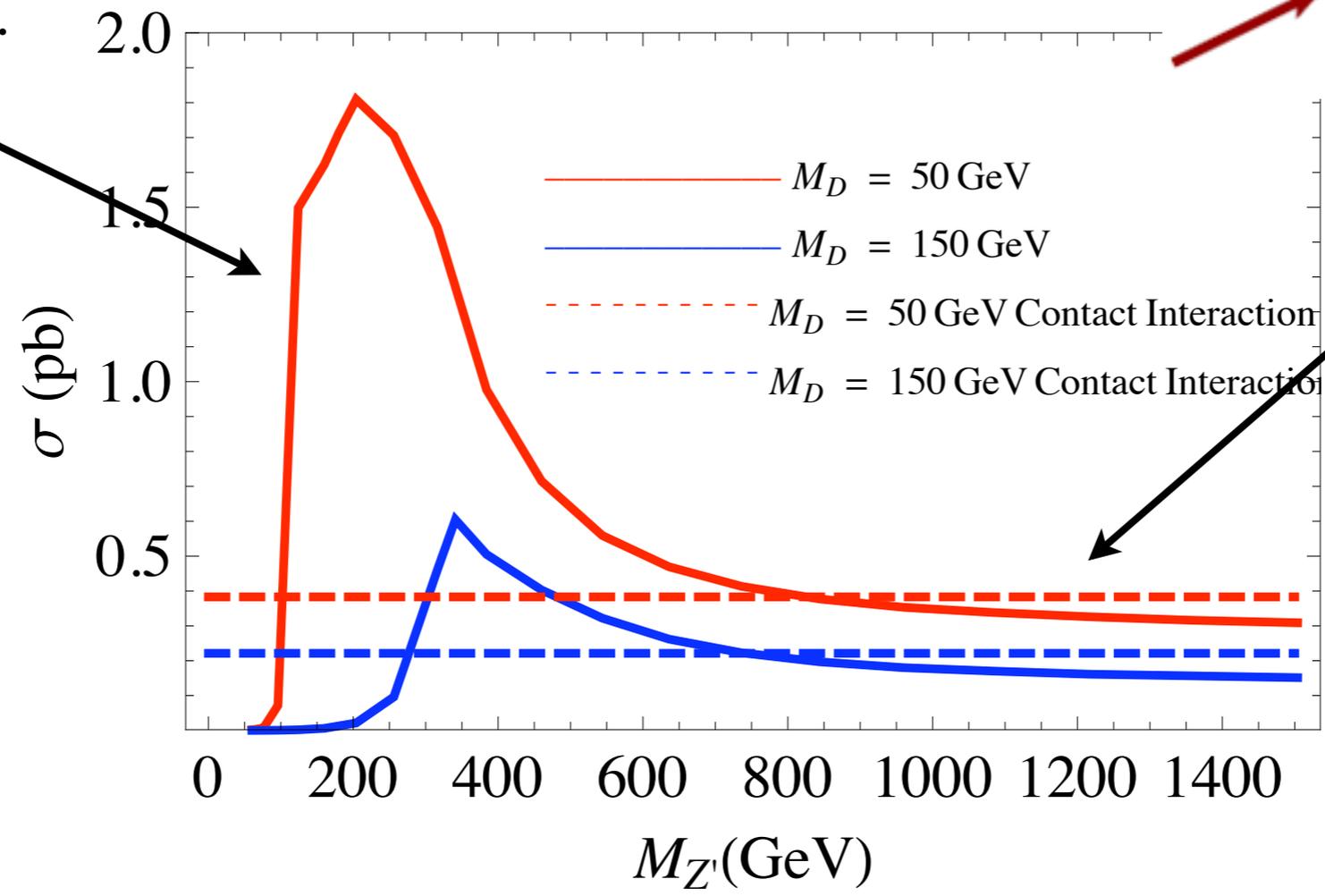


resonance prod.

Tevatron rate for
Monojet + (MET > 80 GeV)



contact-like



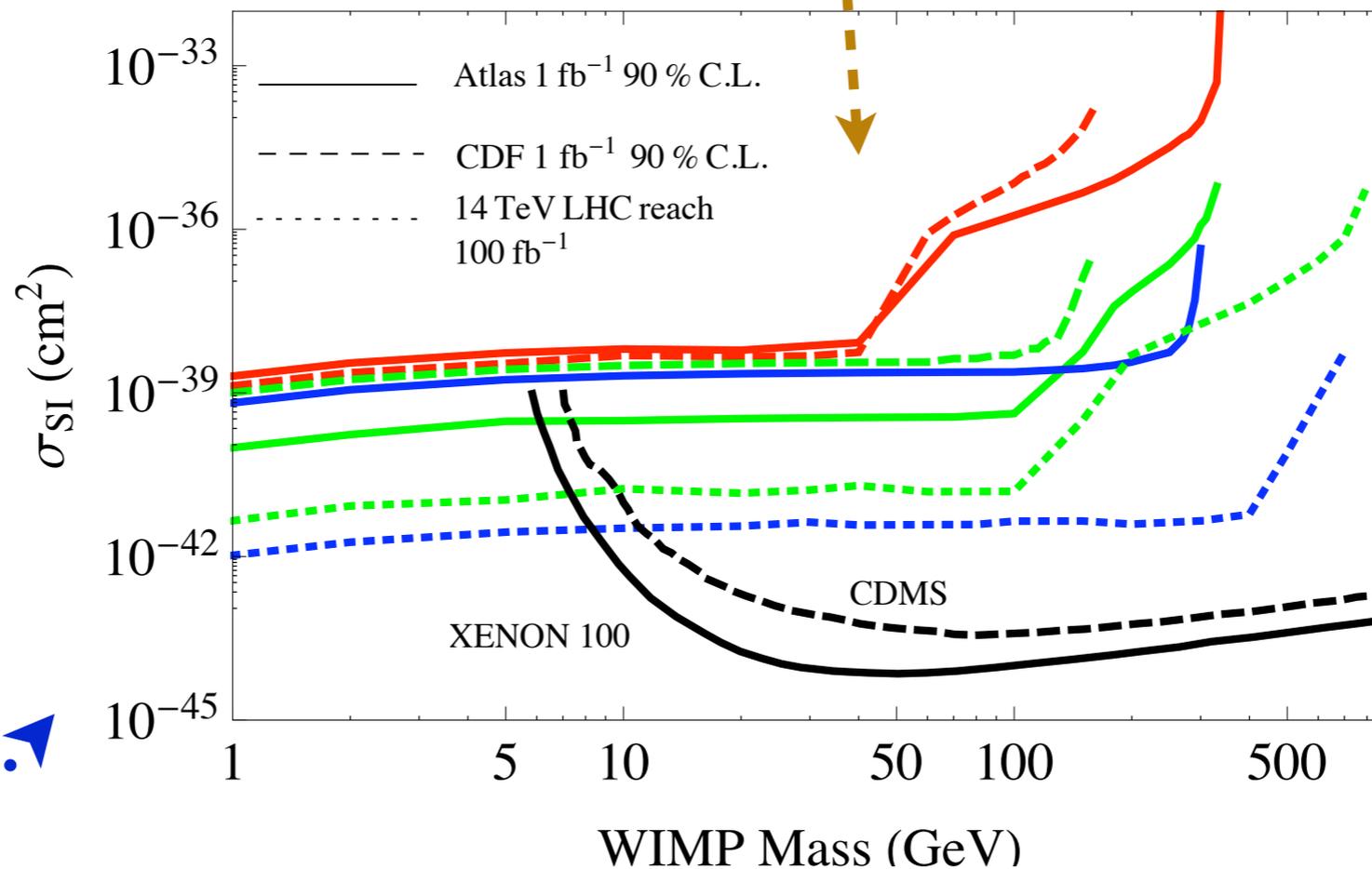
$g_D = g_{Z'}$, fixed σ_{dir}

Limits and reaches: monojet+MET

Dashed: Tevatron 1 fb^{-1} , $\text{MET} > 80 \text{ GeV}$, CDF, PRL 101, 2008

Solid:
LHC, $7 \text{ TeV } 1 \text{ fb}^{-1}$
Very High PT

Dotted:
LHC $14 \text{ TeV}, 100 \text{ fb}^{-1}$
 $\text{MET} > 500 \text{ GeV}$



$g_{Z'} = g_D, g_{Z'5} = g_{D5} = 0$

$M_{Z'} = 100 \text{ GeV}, 300 \text{ GeV}, 1 \text{ TeV}$

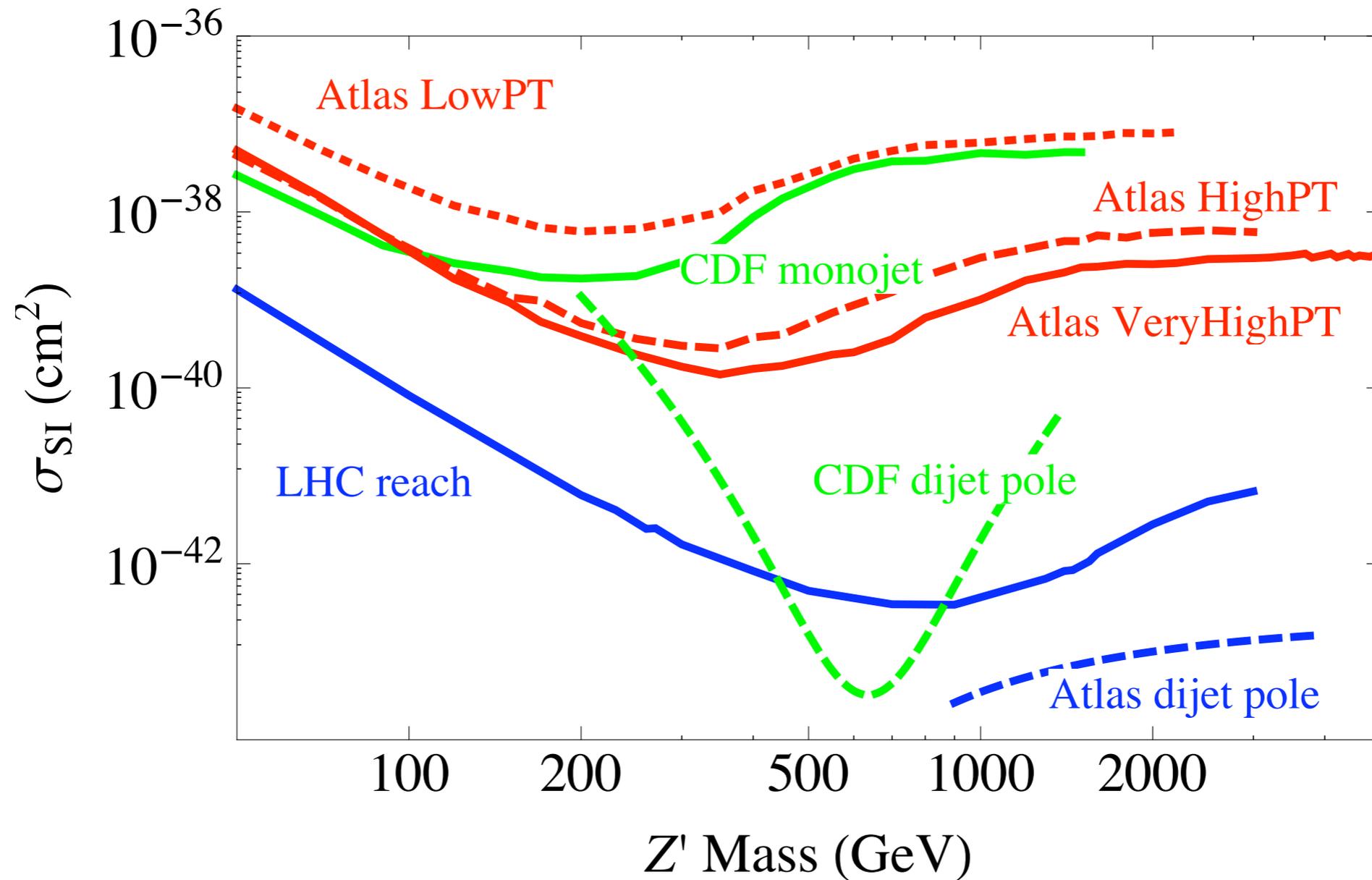
Di-jet resonance searches.

We could, and should, search for the mediator directly!

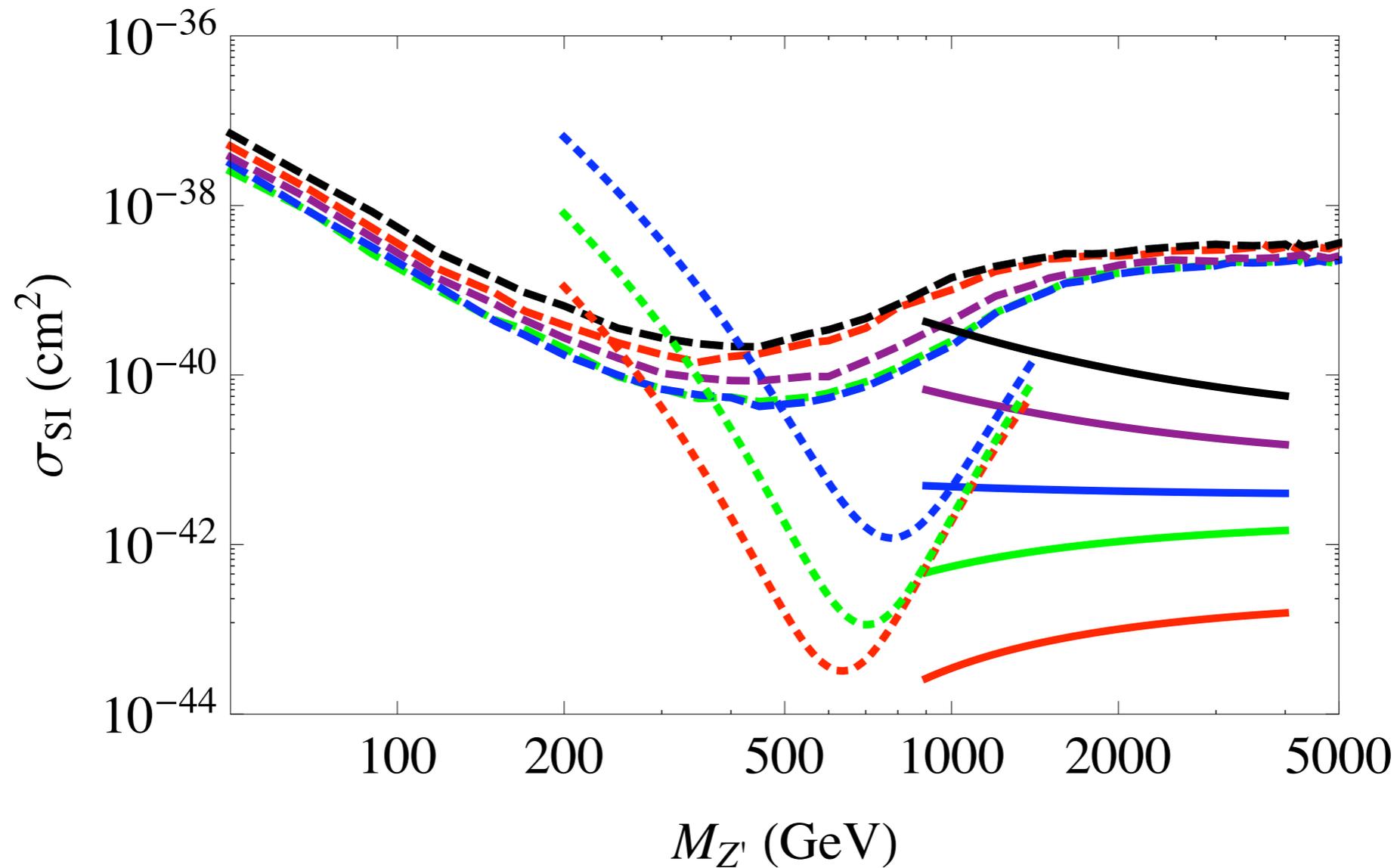
- Resonance searches.
 - ▶ ATLAS: 1 fb⁻¹ 1108.6311
 - ▶ CMS: 1 fb⁻¹ 1107.4771
 - ▶ CDF: Phys. Rev. D79 (2009).
- Compositeness.
 - ▶ CMS 36 pb⁻¹: Phys. Rev. Lett. 106 (2011)
 - ▶ Dzero: Phys. Rev. Lett. 103 (2009)

Combining di-jet with monojet

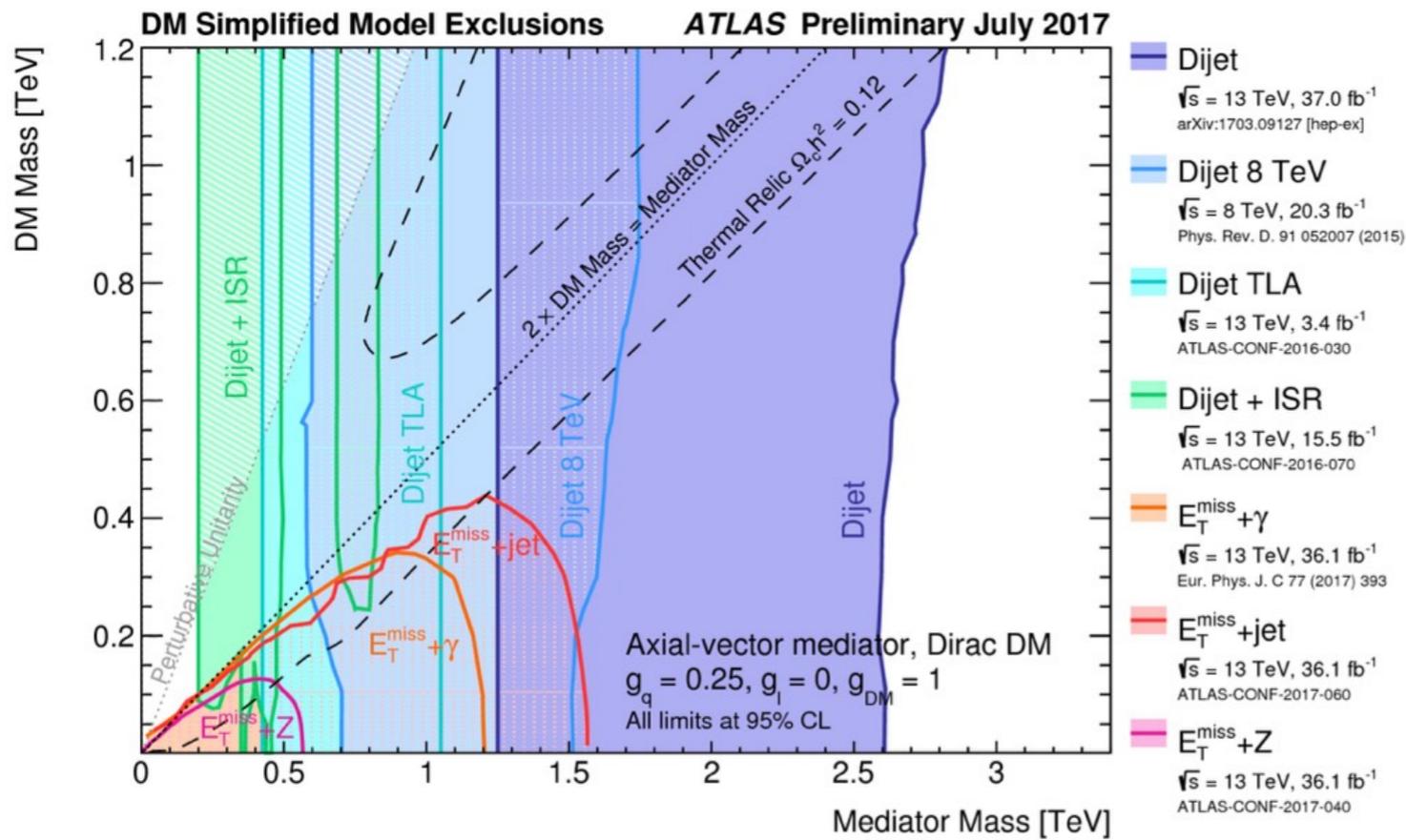
Assume $g_{Z'} = g_D$



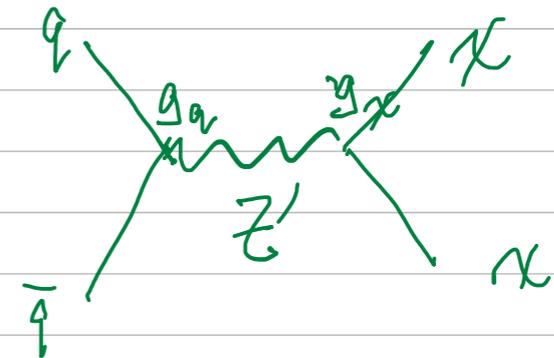
Varying $y=(g_D/g_{Z'})$



$$\sigma_{SI} \propto \frac{g_D^2 g_{Z'}^2}{m_{Z'}^4} \quad y = \frac{g_D}{g_{Z'}} \quad 1, 3, 5, 10, 20$$

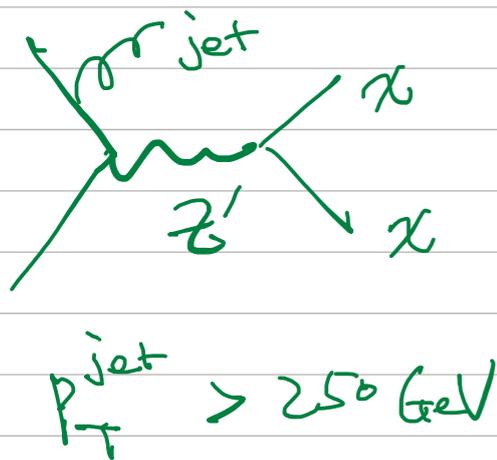


Mediator model



Monojet limit:
 $E_T > 250 \text{ GeV}$

For mediator mass $\sim 1.5 \text{ TeV}$, production rate
 σ_{calj} from z ($q\bar{q}$ pdf) $\sim \text{pb}$

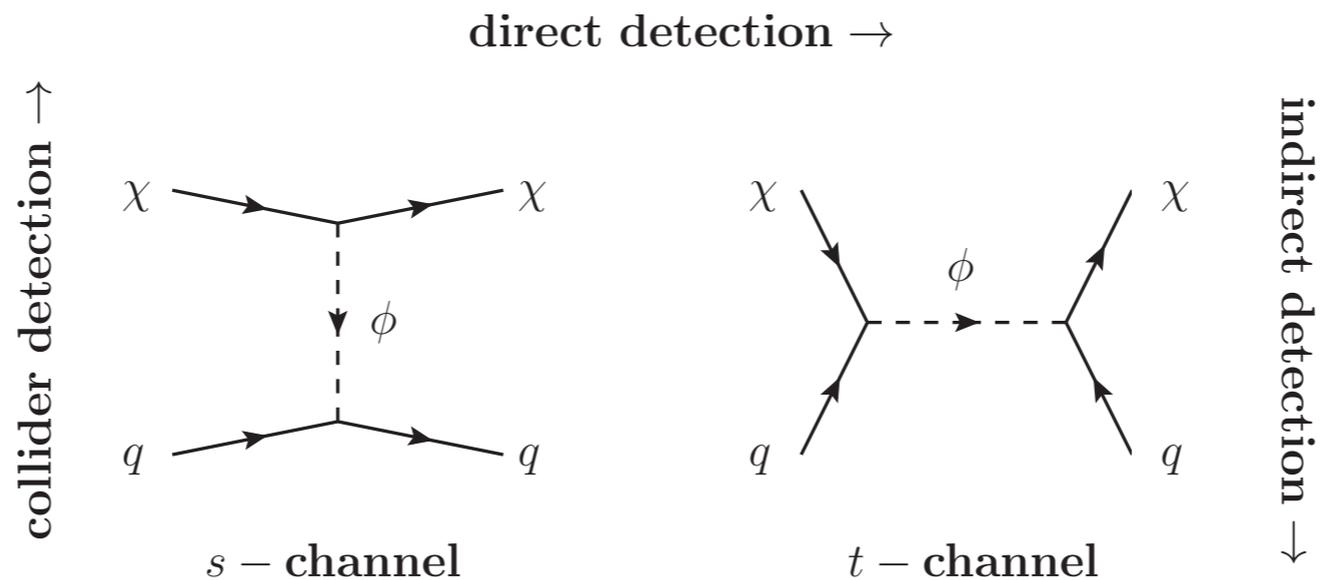


$p_T^{\text{jet}} > 250 \text{ GeV}$

Background $j + (Z \rightarrow \nu\nu)$ or $j + (W \rightarrow l\nu)$

σ_{calj} from Z or W production, a factor
of 10^{-2} for adding a jet, and a factor of
 10^{-2} for PDF at $E(\text{jet} + z) \sim 500 \text{ GeV}$.
 $\rightarrow \sim \text{pb}$.

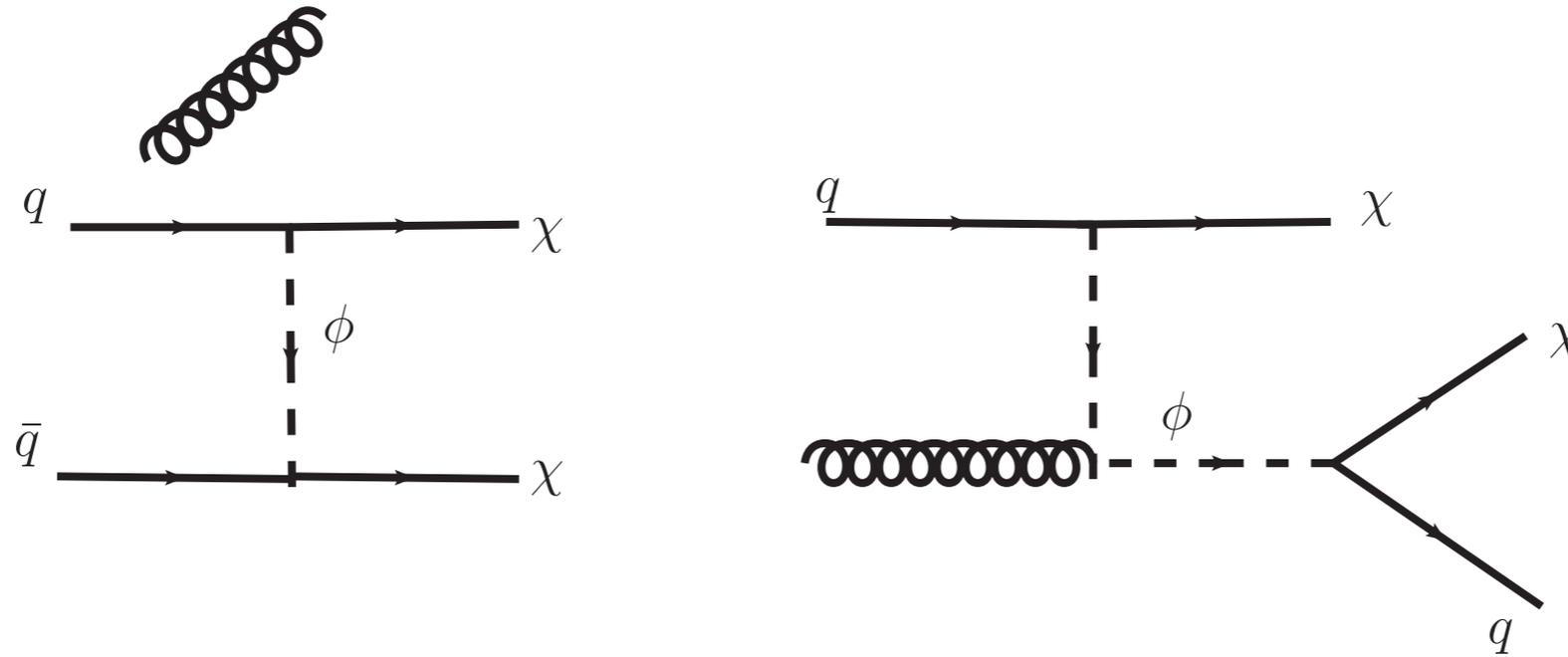
t-channel



- For fermionic (scalar) dark matter, the mediator could be scalar (fermion).
- FCNC constraints $\Rightarrow \phi$ or χ in flavor multiplet.
 - ▶ Consider the case where dark matter is singlet.
 - ▶ ϕ is 3 under $SU(3)_R$ has universal coupling to all quarks. (example: squarks with universal

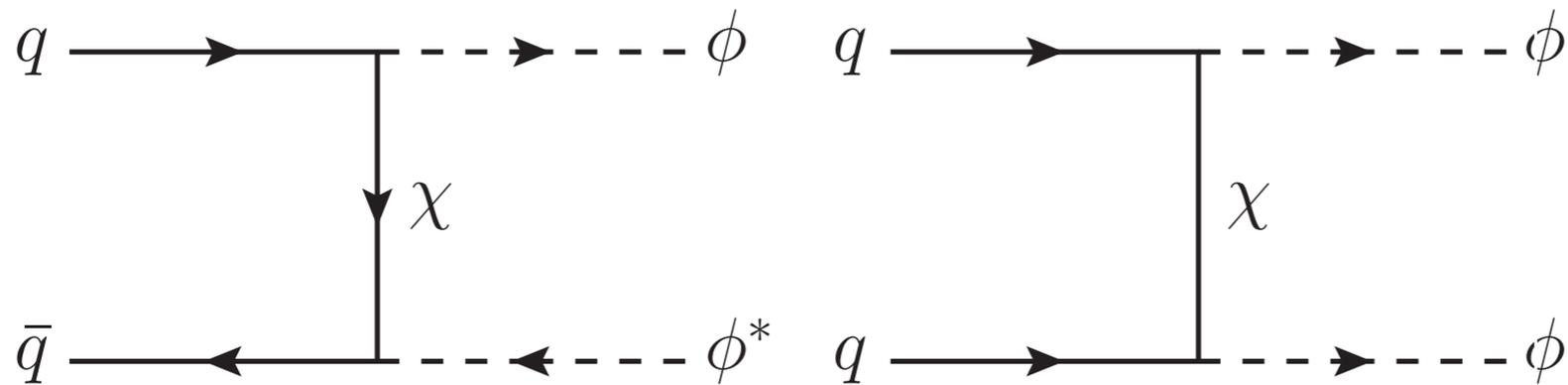
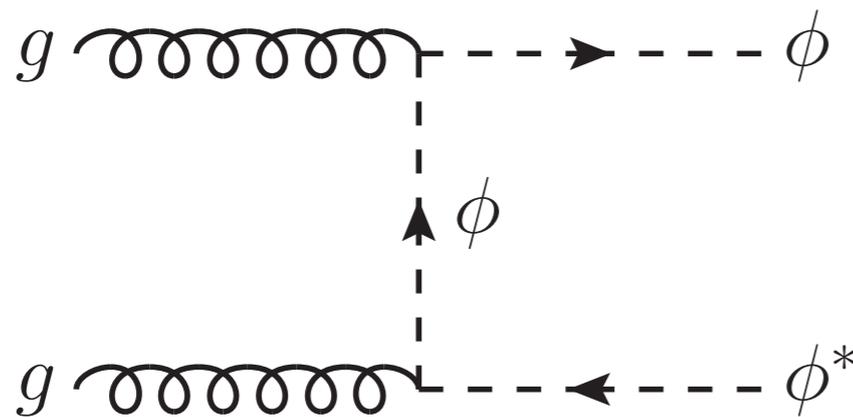
See Chacko et al for flavored DM.

Collider searches



- 2 contributions for monojet.
- $pp \rightarrow \phi\phi$, "squark" searches.
- for large m_ϕ , mono-jet could be important.

di-jet



- $pp \rightarrow \phi\phi$, "squark" searches.
- for large m_ϕ , mono-jet could be important.

